

EX1: Algorithmic Analysis I

Due date: Friday October 16, 2020 at 11:59 pm PDT

Instructions:

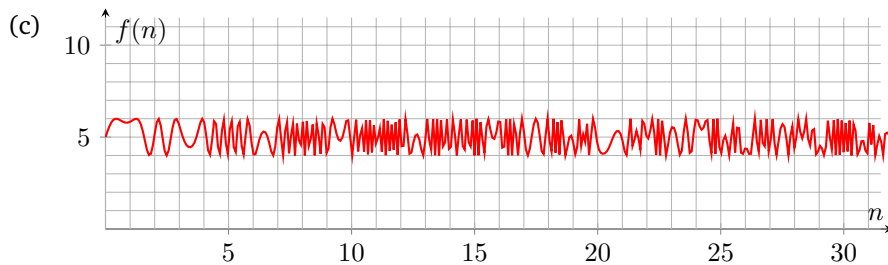
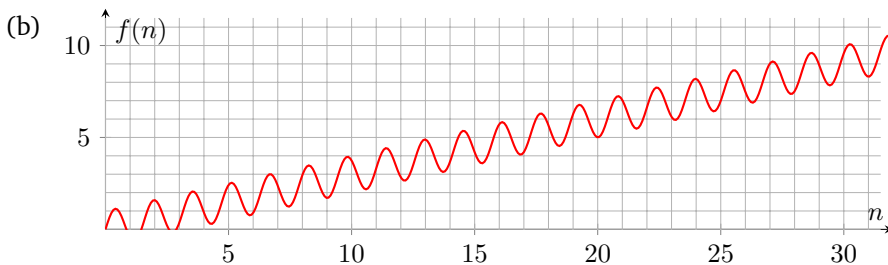
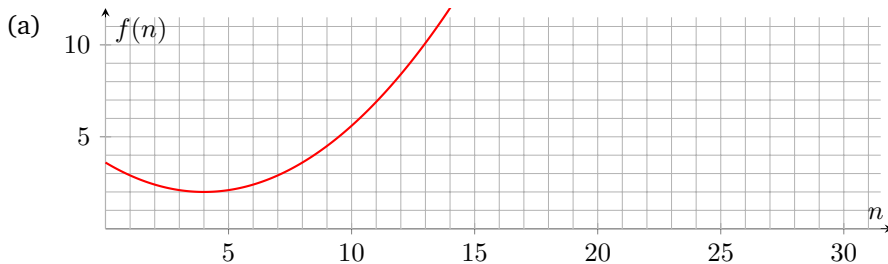
Submit your responses to the “EX1: Algorithmic Analysis I” assignment on Gradescope here: <https://www.gradescope.com/courses/156996/assignments/711761>. Make sure to log in to your Gradescope account using your UW email to access our course.

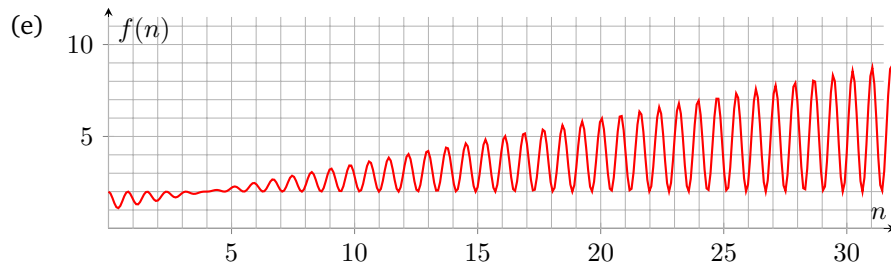
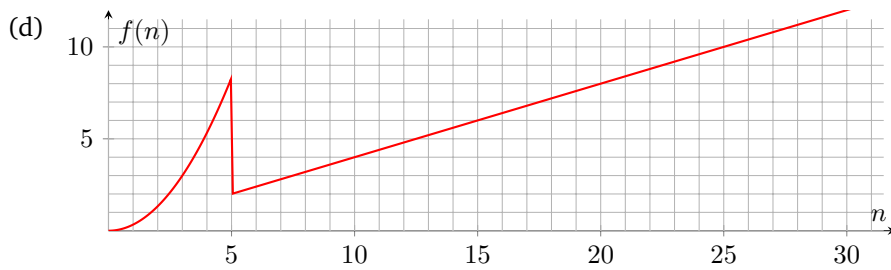
These problems are meant to be done **individually**. If you do want to discuss problems with a partner or group, make sure that you’re writing your answers individually later on. Check our course’s collaboration policy if you have questions.

1. Asymptotic analysis: Visually

For each of the following plots, provide a tight big- \mathcal{O} bound, a tight big- Ω bound, and a big- Θ bound. You do not need to show your work; just list the bounds. If a particular bound doesn’t exist for a given plot, briefly explain why. Assume that the plotted functions continue to follow the same trend shown in the plots as n increases. Each provided bound must either be a constant or a simple polynomial, **from the following possible answers**.

$$n^2, 1, n, \log(n), \frac{1}{n}$$





2. Case and Asymptotic Analysis

In this problem we will analyze code in the `printSmilies` method below. The code is not particularly efficient (i.e. you should not use this code snippet as a model for how to use data structures). You should assume that this code uses the Java implementations of `ArrayList` and `LinkedList` – in particular, that `add` on a `LinkedList` takes constant time because the object stores a reference to the back of the list.

```

1 public void printSmilies(ArrayList<Integer> input, int target) {
2     LinkedList<Integer> products = new LinkedList<>();
3     for (int i = 0; i < input.size(); i++) {
4         for (int j = 0; j < input.size(); j++) {
5             products.add(input.get(i) * input.get(j));
6         }
7     }
8
9     LinkedList<Integer> occurrencesOfToFind = new LinkedList<>();
10
11     while (products.size() != 0) {
12         int next = products.remove(0); // remove the value at index 0
13         if (next == target) {
14             occurrencesOfToFind.add(next);
15         }
16     }
17
18     for (int i = 0; i < occurrencesOfToFind.size(); i++) {
19         for (int j = 0; j < occurrencesOfToFind.size(); j++) {
20             System.out.println(":D");
21         }
22     }
23 }

```

Answer the following questions about the runtime of the `printSmilies` method. In this problem, `input` is defined to have n elements. For each of the problems asking for asymptotic bounds, if your answer uses a variable, your answers should be in terms of n . All big- \mathcal{O} , big- Ω , and big- Θ bounds should be simplified. You can assume `System.out.println` calls will always run in constant time.

Remember that “best/worst-case” refer to the *inputs* that yield the fastest or slowest possible runtime functions, respectively.

- (a) Give the simplified big- Θ bound for runtime of the first loop on lines 3-7. (Note: the runtime bound is the same across all cases). If your answer uses a variable, it should be in terms of n , the size of the input.
- (b) Note that the runtime for last loop is based on the size of occurrencesOfToFind (note: this is not the same variable as n , the input size to this method). To figure out that last loop's runtime, let's break it down by analyzing the previous loop on lines 11-16:
- What sort of state of the parameters `input` and `target` will trigger the worst case where `occurrencesOfToFind` is as big as possible? Give an example 5-element list value for `input` and an example value for `target` that would trigger the worst case. Then, describe the general pattern that would trigger the worst case in no more than 1 sentence.
 - Give a simplified big- Θ bound for the size of `occurrencesOfToFind` in this worst case. If your answer uses a variable, it should be in terms of n , the size of input.
 - What sort of state of the parameters `input` and `target` will trigger the best case where `occurrencesOfToFind` is as small as possible? Give an example 5-element list value for `input` and an example value for `target` that would trigger the best case. Then, describe the general pattern that would trigger the best case in no more than 1 sentence.
 - Give a simplified big- Θ bound for the size of `occurrencesOfToFind` in this best case. If your answer uses a variable, it should be in terms of n , the size of input.
- (c) Consider the worst case runtime situation discussed in the previous question for the loop on lines 18-22 for the following problems.
- Give a tight big- \mathcal{O} for the runtime of lines 18-22. If your answer uses a variable, it should be in terms of n , the size of input.
 - Give a tight big- Ω for the runtime of lines 18-22. If your answer uses a variable, it should be in terms of n , the size of input.
- (d) Consider the best case runtime situation discussed in the previous question for the loop on lines 18-22 for the following problems.
- Give a tight big- \mathcal{O} for the runtime of lines 18-22. If your answer uses a variable, it should be in terms of n , the size of input.

- Give a tight big- Ω for the runtime of lines 18-22. If your answer uses a variable, it should be in terms of n , the size of input.