

# Disjoint Set ADT

- what are disjoint sets?
- what are the disjoint set methods and what do they do?
- why would you use disjoint sets?

# Tree Disjoint Set implementation

- how could we implement this with existing means?
- what is the data structure people have invented?
- how do the methods work for this internal structure?
- what are the optimizations for these methods?
- what are its runtimes for the methods?

# Optimization rules

## Union-by-rank!

- let  $\text{rank}(x)$  be a number representing the upper bound of the height of  $x$  so  $\text{rank}(x) \geq \text{height}(x)$
- Keep track of rank of all trees
- When unioning make the tree with larger rank the root
- If it's a tie, pick one randomly and increase rank by one

## Path Compression

- Collapse tree into fewer levels by updating parent pointer of each node you visit
- Whenever you call  $\text{findSet}()$  update each node you touch's parent pointer to point directly to overallRoot