

# Lecture 4: Introduction to Code Analysis

CSE 373: Data Structures and Algorithms

### Warm Up

Read through the code on the worksheet given

Come up with a test case for each of the described test categories

Expected Behavior add(1)

Forbidden Input add(null)

Empty/Null Add into empty list

**Boundary/Edge** Add enough values to trigger internal array double and copy

Scale Add 1000 times in a row

#### Socrative:

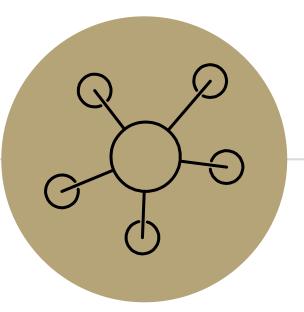
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Please enter your name as: Last, First

## Administrivia

- Fill out HW 2 Partner form
  - Posted on class webpage at top
  - Due TONIGHT Monday 4/8 by 11:59pm
- Fill out Student Background Survey, on website announcements
- Read Pair Programming Doc (on readings for Wednesday on calendar)



### **Algorithm Analysis**

# Code Analysis

How do we compare two pieces of code?

- -Time needed to run
- -Memory used 🖛
- -Number of network calls
- -Amount of data saved to disk
- -Specialized vs generalized
- -Code reusability
- -Security

### Comparing Algorithms with Mathematical Models

Consider overall trends as inputs increase

- Computers are fast, small inputs don't differentiate
- Must consider what happens with large inputs

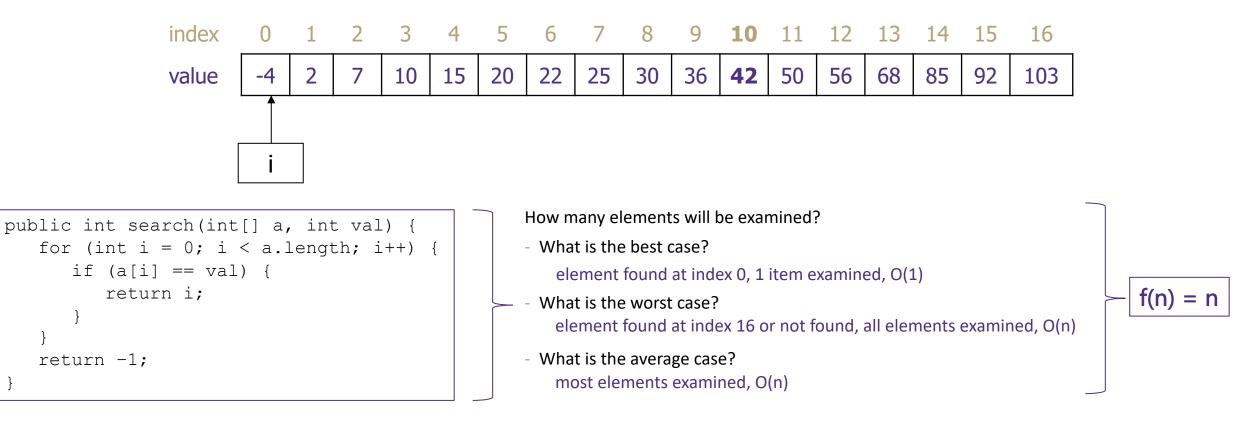
Identify trends without investing in testing

Model performance across multiple possible scenarios

- Worst case what is the most expensive or least performant an operation can be
- Average case what functions are most likely to come up?
- Best case if we understand the ideal conditions can increase the likelihood of those conditions?

## **Review:** Sequential Search

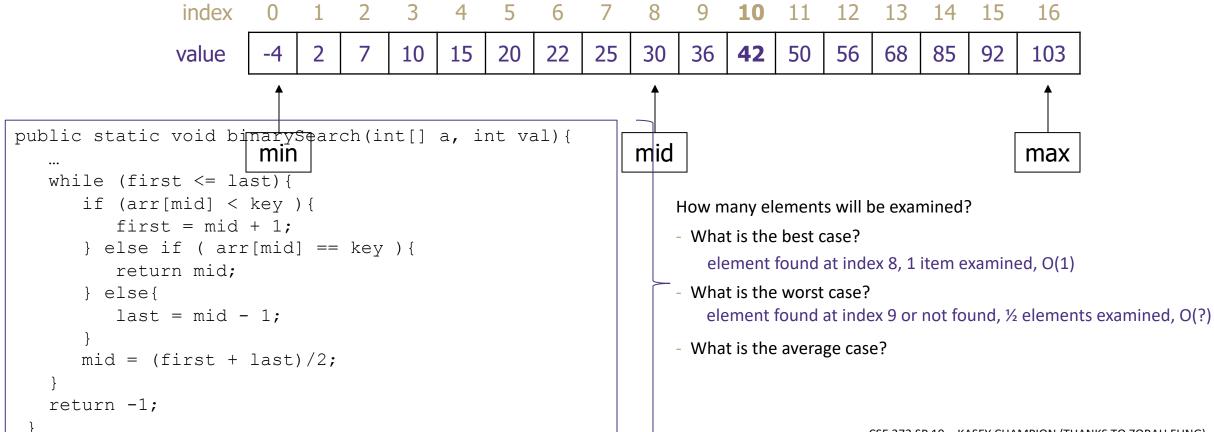
sequential search: Locates a target value in a collection by examining each element sequentially
Example: Searching the array below for the value 42:



### **Review:** Binary Search

**binary search**: Locates a target value in a *sorted* array or list by successively eliminating half of the array from consideration.

- Example: Searching the array below for the value 42:



# Analyzing Binary Search

What is the pattern?

At each iteration, we eliminate half of the remaining elements

### How long does it take to finish?

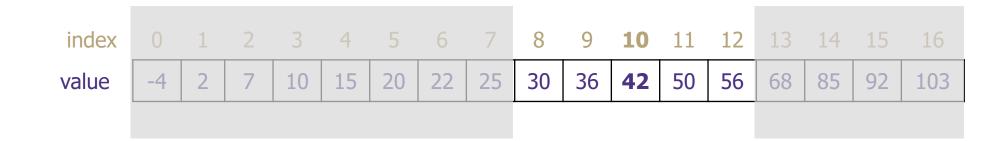
- $1^{st}$  iteration N/2 elements remain
- 2<sup>nd</sup> iteration N/4 elements remain
- Kth iteration N/2<sup>k</sup> elements remain

Finishes when  $\frac{n}{2^k} = 1$  $\frac{n}{2^k} = 1$ -> multiply right side by 2<sup>K</sup>

N = 2<sup>K</sup>

-> isolate K exponent with logarithm

 $\log_2 N = k$ 



# Asymptotic Analysis

**asymptotic analysis** – the process of mathematically representing runtime of a algorithm in relation to the number of inputs and how that relationship changes as the number of inputs grow

Two step process

- 1. Model reduce code run time to a mathematical relationship with number of inputs
- 2. Analyze compare runtime/input relationship across multiple algorithms



# Code Modeling

**code modeling** – the process of mathematically representing how many operations a piece of code will run in relation to the number of inputs n

Examples:

- Sequential search f(n) = n
- Binary search  $f(n) = log_2 n$

#### What counts as an "operation"?

### **Basic operations**

- Adding ints or doubles
- Variable assignment
- Variable update
- Return statement
- Accessing array index or object field

#### **Consecutive statements**

- Sum time of each statement

### Assume all operations run in equivalent time

#### **Function calls**

- Count runtime of function body

### Conditionals

- Time of test + worst case scenario branch

#### Loops

 Number of iterations of loop body x runtime of loop body

## Modeling Case Study

**Goal:** return 'true' if a sorted array of ints contains duplicates

#### Solution 1: compare each pair of elements

```
public boolean hasDuplicate1(int[] array) {
   for (int i = 0; i < array.length; i++) {
      for (int j = 0; j < array.length; j++) {
         if (i != j && array[i] == array[j]) {
            return true;
         }
      }
      return false;
}</pre>
```

#### Solution 2: compare each consecutive pair of elements

```
public boolean hasDuplicate2(int[] array) {
  for (int i = 0; i < array.length - 1; i++) {
      if (array[i] == array[i + 1]) {
         return true;
      }
   }
  return false;
}</pre>
```

## Modeling Case Study: Solution 2

Goal: produce mathematical function representing runtime f(n) where n = array.length

```
Solution 2: compare each consecutive pair of elements
public boolean hasDuplicate2(int[] array) {
     for (int i = 0; i < array.length - 1; i++) { loop = (n-1)(body)
         if (array[i] == array[i + 1]) {+4
                                                               If statement = 5
                  return true; +1
     return false;
                        +1
                                  Approach
f(n) = 5(n-1) + 1
                                  -> start with basic operations, work inside out for control structures
                                  - Each basic operation = +1
linear \rightarrow O(n)
                                    Conditionals = worst case test operations + branch
                                    Loop = iterations (loop body)
```

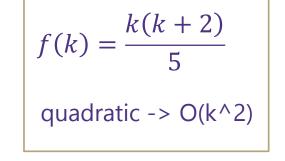
## Modeling Case Study: Solution 1

```
Solution 1: compare each consecutive pair of elements
public boolean hasDuplicate1(int[] array) {
     for (int i = 0; i < array.length; i++) { x n</pre>
         for (int j = 0; j < array.length; j++) { x n</pre>
             if (i != j && array[i] == array[j]) {+5 ]
                                                                                    6n<sup>2</sup>
                                                                              6n
                 return true; +1
     return false; +1
                                 Approach
                                 -> start with basic operations, work inside out for control structures
f(n) = 5(n-1) + 1
                                 - Each basic operation = +1
quadratic -> O(n^2)
                                   Conditionals = worst case test operations + branch
                                   Loop = iterations (loop body)
```

### Your turn!

Write the specific mathematical code model for the following code and indicate the big o runtime.

```
public void foobar (int k) {
    int j = 0;+1
    while (j < k) { +k/5(body)
        for (int i = 0; i < k; i++) { +k(body)
            System.out.println("Hello world");+1
        }
        j = j + 5;+2
    }
</pre>
```



Approach	
	start with basic operations, work inside out for control structures
-	Each basic operation $= +1$
-	Conditionals = worst case test operations + branch
-	Loop = iterations (loop body)