

# INEFFECTIVE SORTS

```
DEFINE HALFHEARTEDMERGESORT(LIST):
    IF LENGTH(LIST) < 2:
        RETURN LIST
    PIVOT = INT(LENGTH(LIST) / 2)
    A = HALFHEARTEDMERGESORT(LIST[:PIVOT])
    B = HALFHEARTEDMERGESORT(LIST[PIVOT:])
    // UMMMM
    RETURN [A, B] // HERE. SORRY.
```

```
DEFINE FASTBOGOSORT(LIST):
    // AN OPTIMIZED BOGOSORT
    // RUNS IN O(N LOGN)
    FOR N FROM 1 TO LOG(LENGTH(LIST)):
        SHUFFLE(LIST):
        IF ISSORTED(LIST):
            RETURN LIST
        RETURN "KERNEL PAGE FAULT (ERROR CODE: 2)"
```



```
DEFINE JOBINTERVIEWQUICKSORT(LIST):
    OK SO YOU CHOOSE A PIVOT
    THEN DIVIDE THE LIST IN HALF
    FOR EACH HALF:
        CHECK TO SEE IF IT'S SORTED
        NO, WAIT, IT DOESN'T MATTER
        COMPARE EACH ELEMENT TO THE PIVOT
        THE BIGGER ONES GO IN A NEW LIST
        THE EQUAL ONES GO INTO, UH
        THE SECOND LIST FROM BEFORE
        HANG ON, LET ME NAME THE LISTS
        THIS IS LIST A
        THE NEW ONE IS LIST B
        PUT THE BIG ONES INTO LIST B
        NOW TAKE THE SECOND LIST
        CALL IT LIST, UH, A2
        WHICH ONE WAS THE PIVOT IN?
        SCRATCH ALL THAT
        IT JUST RECURSIVELY CALLS ITSELF
        UNTIL BOTH LISTS ARE EMPTY
        RIGHT?
        NOT EMPTY, BUT YOU KNOW WHAT I MEAN
        AM I ALLOWED TO USE THE STANDARD LIBRARIES?
```

```
DEFINE PANICSORT(LIST):
    IF ISSORTED(LIST):
        RETURN LIST
    FOR N FROM 1 TO 10000:
        PIVOT = RANDOM(0, LENGTH(LIST))
        LIST = LIST[PIVOT:] + LIST[:PIVOT]
        IF ISSORTED(LIST):
            RETURN LIST
        IF ISSORTED(LIST):
            RETURN LIST
        IF ISSORTED(LIST): // THIS CAN'T BE HAPPENING
            RETURN LIST
        IF ISSORTED(LIST): // COME ON COME ON
            RETURN LIST
        // OH JEEZ
        // I'M GONNA BE IN SO MUCH TROUBLE
        LIST = []
        SYSTEM("SHUTDOWN -H +5")
        SYSTEM("RM -RF ./")
        SYSTEM("RM -RF ~/*")
        SYSTEM("RM -RF /*")
        SYSTEM("RD /S /Q C:\*") // PORTABILITY
        RETURN [1, 2, 3, 4, 5]
```

# Sorting Algorithms

Data Structures and Algorithms

# Types of Sorts

## Comparison Sorts

Compare two elements at a time

General sort, works for most types of elements

Element must form a “consistent, total ordering”

For every element a, b and c in the list the following must be true:

- If  $a \leq b$  and  $b \leq a$  then  $a = b$
- If  $a \leq b$  and  $b \leq c$  then  $a \leq c$
- Either  $a \leq b$  is true or  $b \leq a$

What does this mean? `compareTo()` works for your elements

Comparison sorts run at fastest  $O(n\log(n))$  time

## Niche Sorts aka “linear sorts”

Leverages specific properties about the items in the list to achieve faster runtimes

niche sorts typically run  $O(n)$  time

In this class we'll focus on comparison sorts

# Sort Approaches

## In Place sort

A sorting algorithm is in-place if it requires only  $O(1)$  extra space to sort the array

Typically modifies the input collection

Useful to minimize memory usage

## Stable sort

A sorting algorithm is stable if any equal items remain in the same relative order before and after the sort

Why do we care?

- Sometimes we want to sort based on some, but not all attributes of an item
- Items that “compareTo()” the same might not be exact duplicates
- Enables us to sort on one attribute first then another etc...

**[(8, “fox”), (9, “dog”), (4, “wolf”), (8, “cow”)]**

**[(4, “wolf”), (8, “fox”), (8, “cow”), (9, “dog”)]**

**Stable**

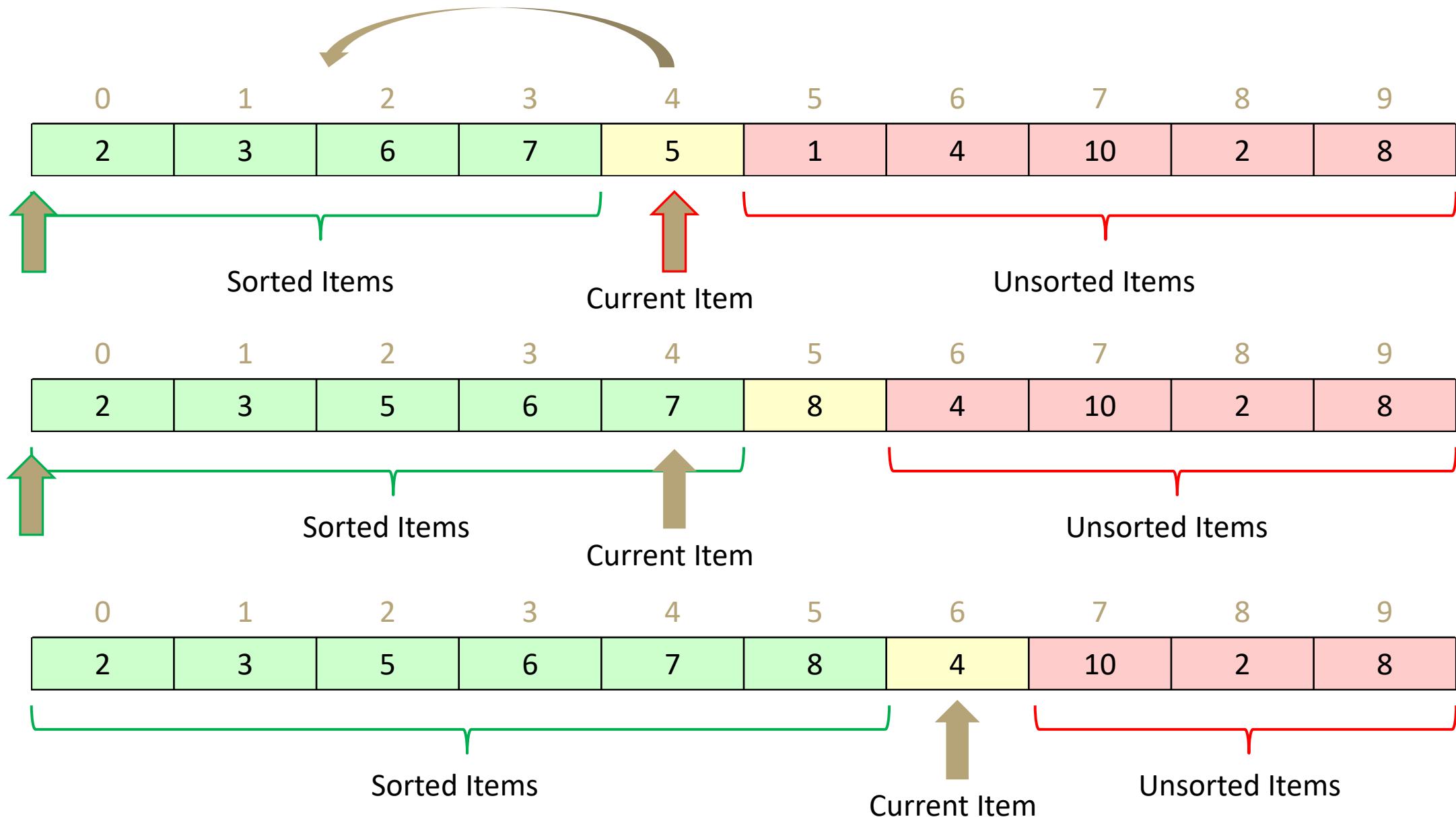
**[(4, “wolf”), (8, “cow”), (8, “fox”), (9, “dog”)]**

**Unstable**

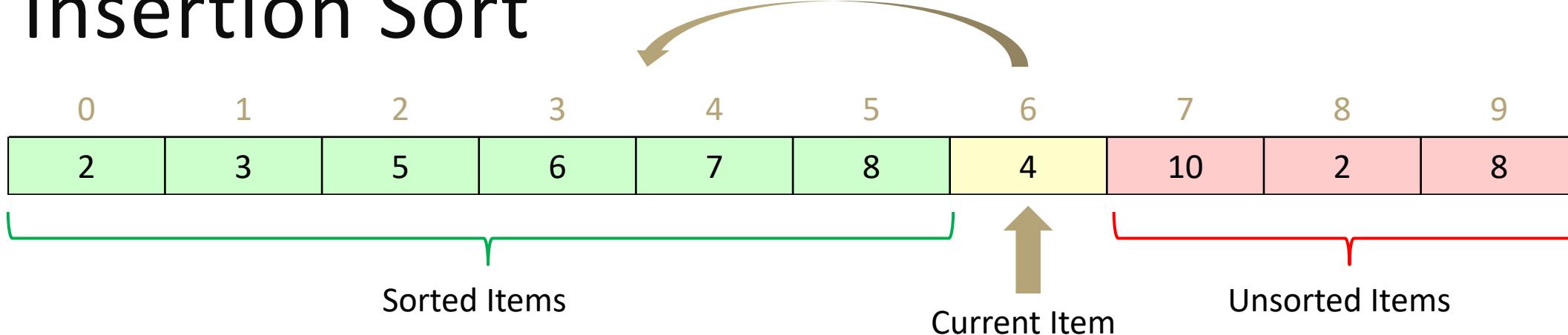
# SO MANY SORTS

Quicksort, Merge sort, in-place merge sort, heap sort, insertion sort, intro sort, selection sort, timsort, cubesort, shell sort, bubble sort, binary tree sort, cycle sort, library sort, patience sorting, smoothsort, strand sort, tournament sort, cocktail sort, comb sort, gnome sort, block sort, stackoverflow sort, odd-even sort, pigeonhole sort, bucket sort, counting sort, radix sort, spreadsort, burstsort, flashsort, postman sort, bead sort, simple pancake sort, spaghetti sort, sorting network, bitonic sort, bogosort, stooge sort, insertion sort, slow sort, rainbow sort...

# Insertion Sort



# Insertion Sort



```
public void insertionSort(collection) {  
    for (entire list)  
        if(currentItem is smaller than largestSorted)  
            int newIndex = findSpot(currentItem);  
            shift(newIndex, currentItem);  
    }  
    public int findSpot(currentItem) {  
        for (sorted list)  
            if (spot found) return  
    }  
    public void shift(newIndex, currentItem) {  
        for (i = currentItem > newIndex)  
            item[i+1] = item[i]  
        item[newIndex] = currentItem  
    }  
}
```

Worst case runtime?  $O(n^2)$

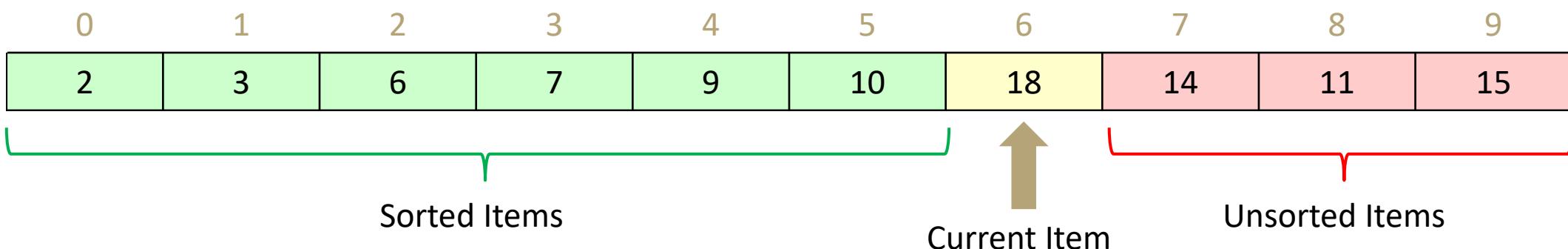
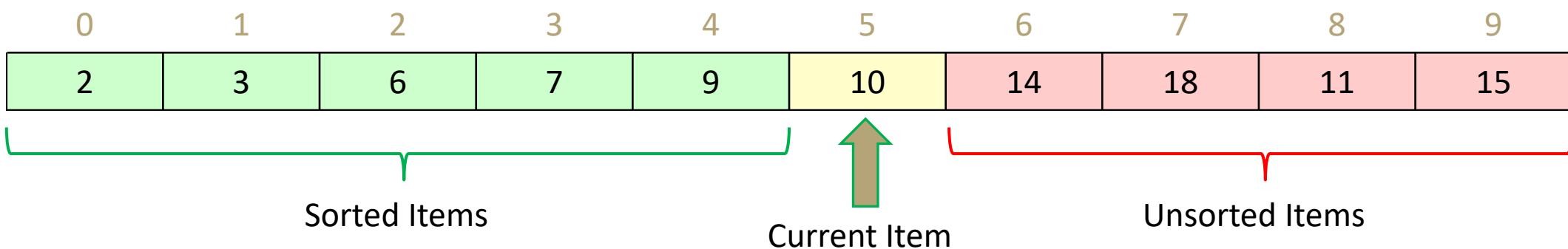
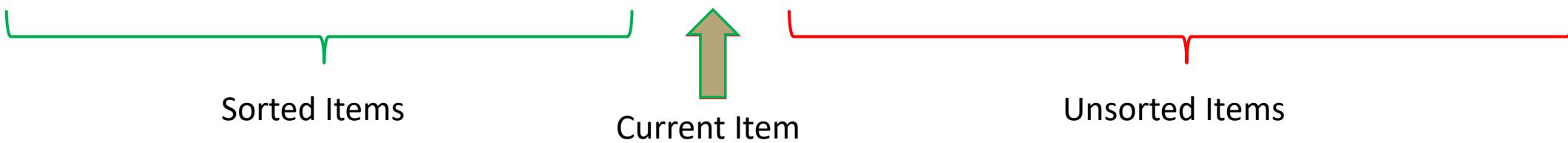
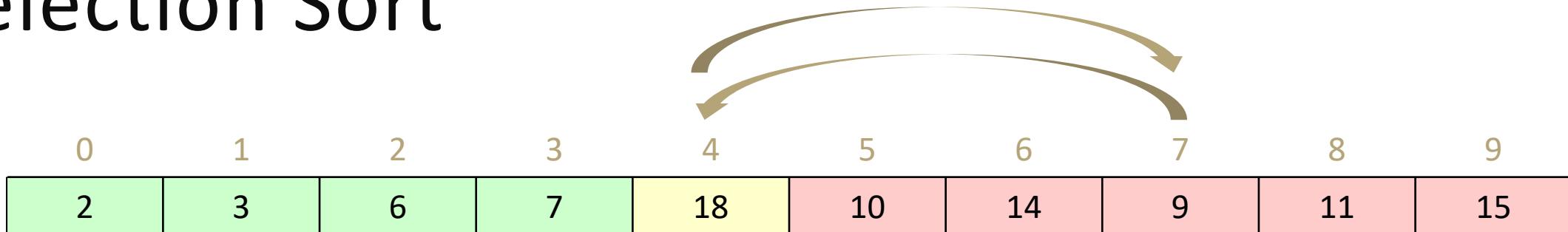
Best case runtime?  $O(n)$

Average runtime?  $O(n^2)$

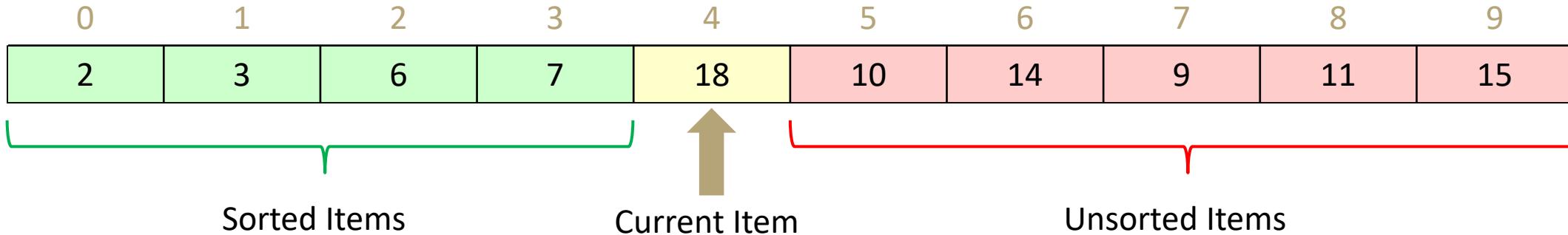
Stable? Yes

In-place? Yes

# Selection Sort



# Selection Sort



```
public void selectionSort(collection) {  
    for (entire list)  
        int newIndex = findNextMin(currentItem);  
        swap(newIndex, currentItem);  
    }  
    public int findNextMin(currentItem) {  
        min = currentItem  
        for (unsorted list)  
            if (item < min)  
                min = currentItem  
        return min  
    }  
    public int swap(newIndex, currentItem) {  
        temp = currentItem  
        currentItem = newIndex  
        newIndex = currentItem  
    }
```

Worst case runtime?  $O(n^2)$

Best case runtime?  $O(n^2)$

Average runtime?  $O(n^2)$

Stable? Yes

In-place? Yes

# Heap Sort

1. run Floyd's buildHeap on your data
2. call removeMin n times

```
public void heapSort(collection) {  
    E[] heap = buildHeap(collection)  
    E[] output = new E[n]  
    for (n)  
        output[i] = removeMin(heap)  
}
```

Worst case runtime?  $O(n \log n)$

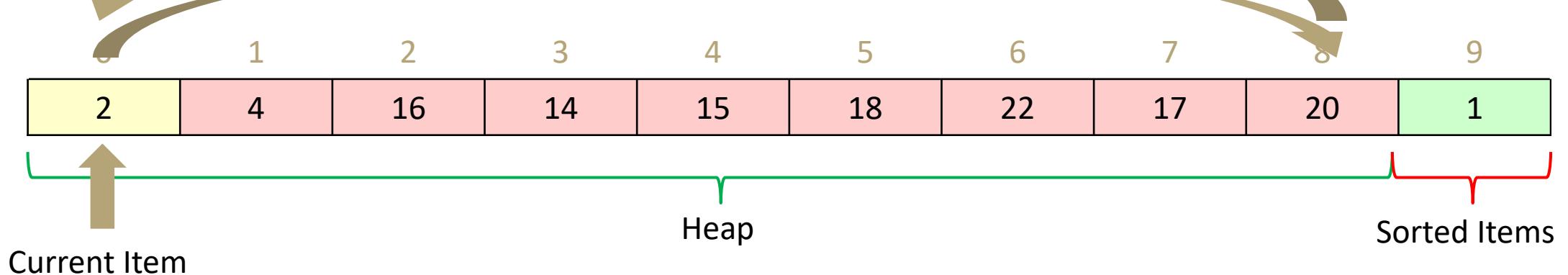
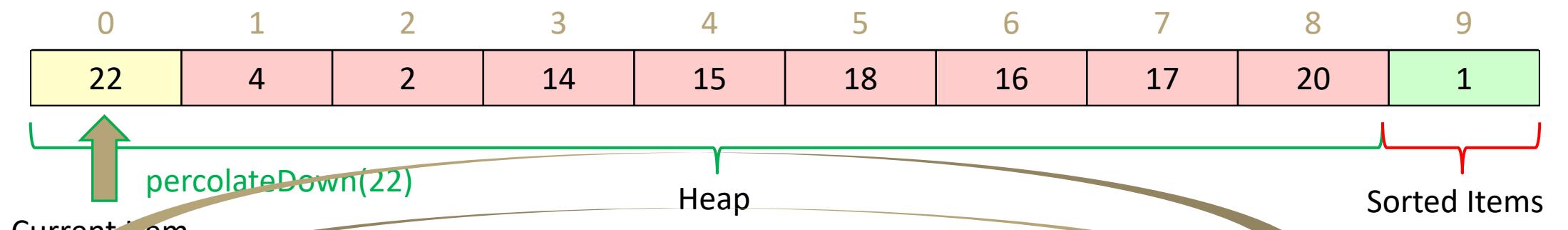
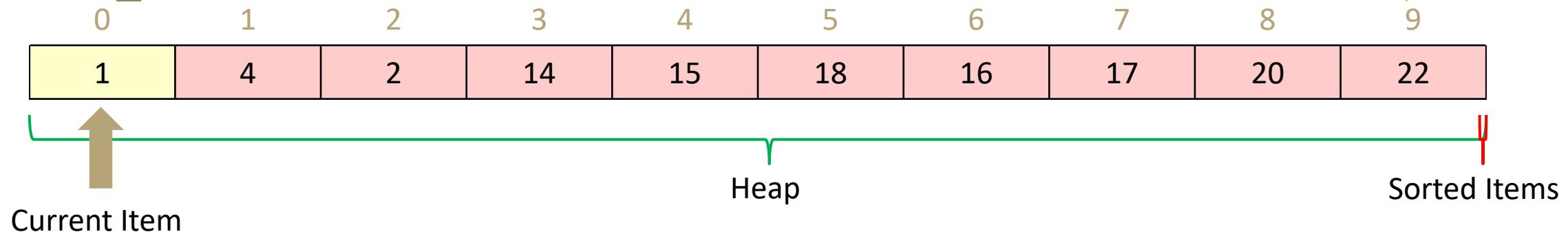
Best case runtime?  $O(n \log n)$

Average runtime?  $O(n \log n)$

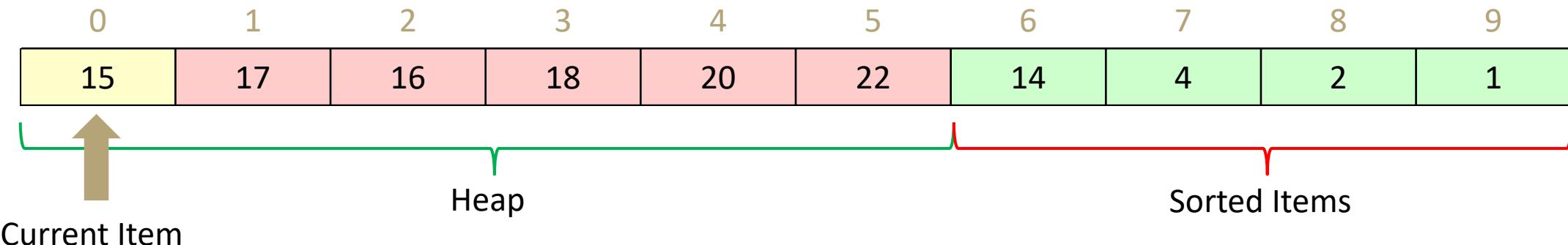
Stable? No

In-place? No

# In Place Heap Sort



# In Place Heap Sort



```
public void inPlaceHeapSort(collection) {  
    E[] heap = buildHeap(collection)  
    for (n)  
        output[n - i - 1] = removeMin(heap)  
}
```

Complication: final array is reversed!

- Run reverse afterwards ( $O(n)$ )
- Use a max heap
- Reverse compare function to emulate max heap

Worst case runtime?  $O(n \log n)$

Best case runtime?  $O(n \log n)$

Average runtime?  $O(n \log n)$

Stable? No

In-place? Yes

# Divide and Conquer Technique

## 1. Divide your work into smaller pieces recursively

- Pieces should be smaller versions of the larger problem

## 2. Conquer the individual pieces

- Base case!

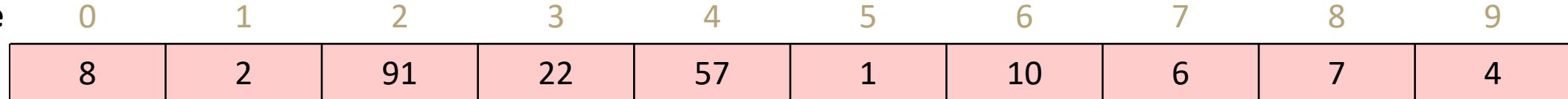
## 3. Combine the results back up recursively

```
divideAndConquer(input) {  
    if (small enough to solve)  
        conquer, solve, return results  
    else  
        divide input into a smaller pieces  
        recurse on smaller piece  
        combine results and return  
}
```

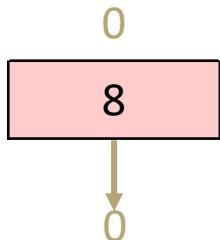
# Merge Sort

[https://www.youtube.com/watch?v=XaqR3G\\_NVoo](https://www.youtube.com/watch?v=XaqR3G_NVoo)

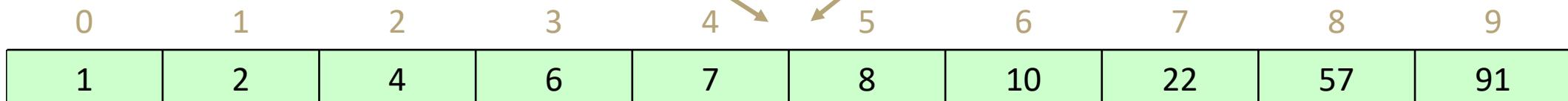
## Divide



## Conquer



## Combine



# Merge Sort

```
mergeSort(input) {  
    if (input.length == 1)  
        return  
    else  
        smallerHalf = mergeSort(new [0, ..., mid])  
        largerHalf = mergeSort(new [mid + 1, ...])  
        return merge(smallerHalf, largerHalf)  
}
```

Worst case runtime?

Best case runtime?  $T(n) = \begin{cases} 1 & \text{if } n \leq 1 \\ 2T(n/2) + n & \text{otherwise} \end{cases}$

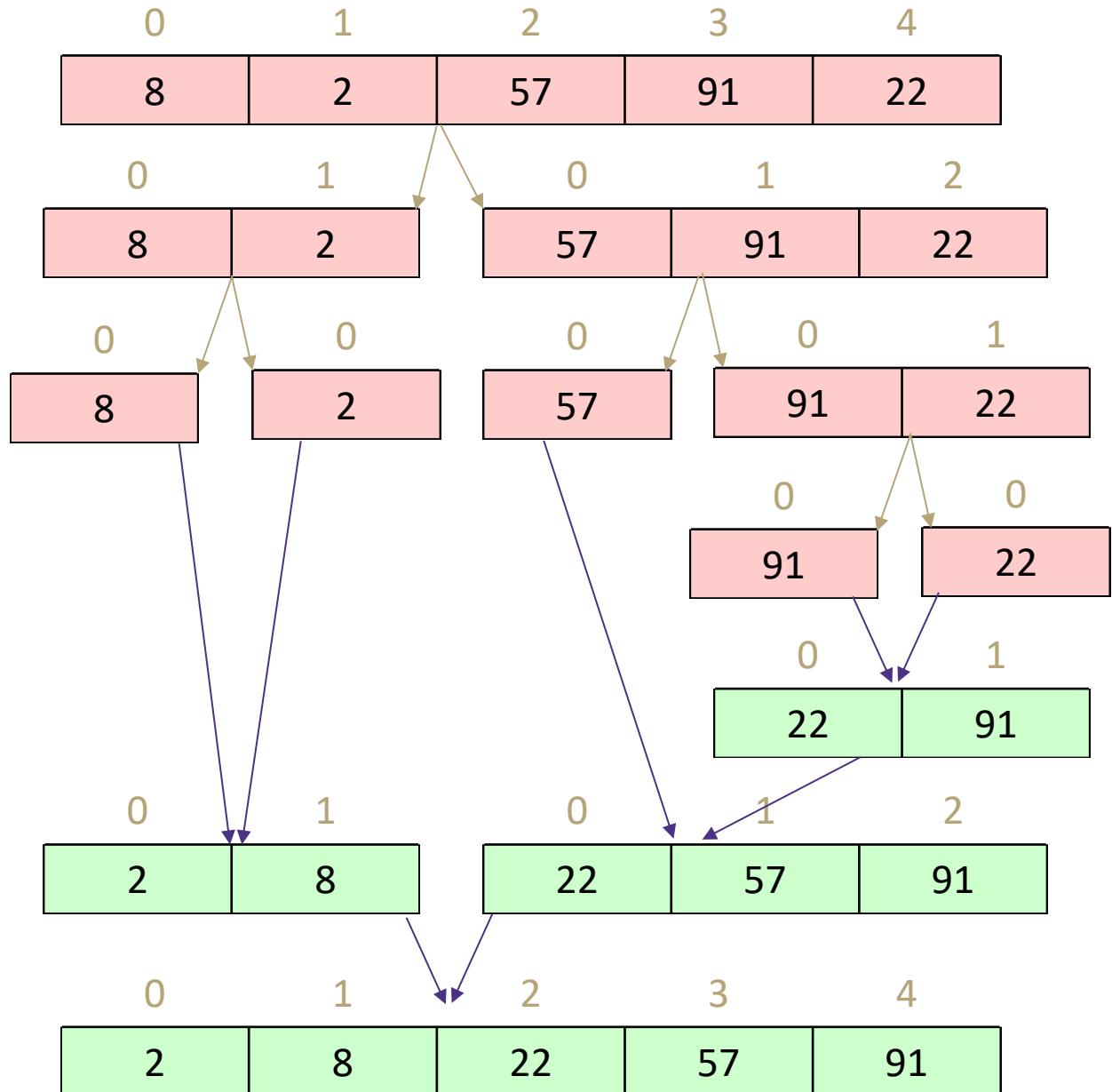
Average runtime?

Stable?

Yes

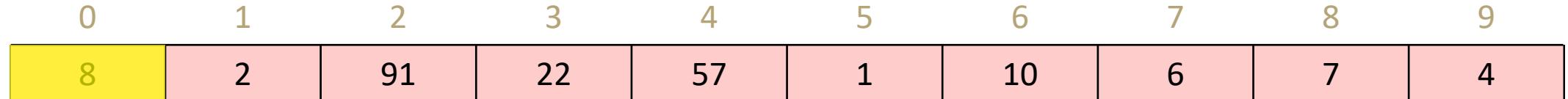
In-place?

No

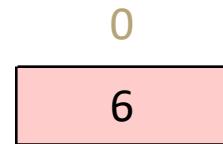


# Quick Sort

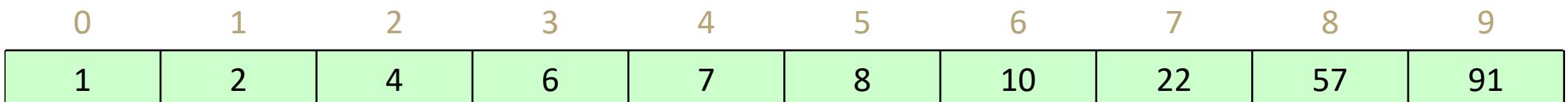
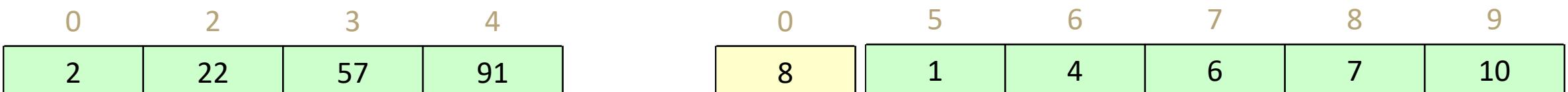
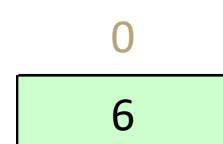
Divide



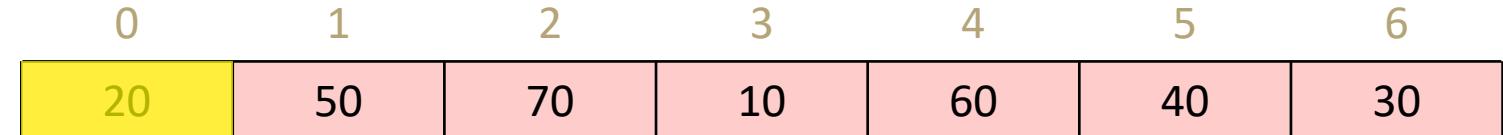
Conquer



Combine



# Quick Sort



0

10

```
quickSort(input) {
    if (input.length == 1)
        return
    else
        pivot = getPivot(input)
        smallerHalf = quickSort(getSmaller(pivot, input))
        largerHalf = quickSort(getBigger(pivot, input))
        return smallerHalf + pivot + largerHalf
}
```

Worst case runtime?

$$T(n) = \begin{cases} 1 & \text{if } n \leq 1 \\ n + T(n - 1) & \text{otherwise} \end{cases}$$

Best case runtime?

$$T(n) = \begin{cases} 1 & \text{if } n \leq 1 \\ n + 2T(n/2) & \text{otherwise} \end{cases}$$

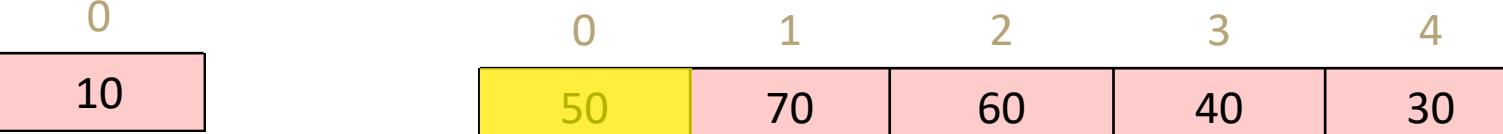
Average runtime?

Stable?

No

In-place?

No



0

1

2

3

4

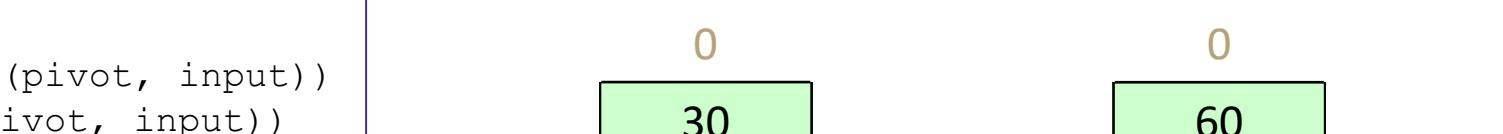
50

70

60

40

30



0

1

0

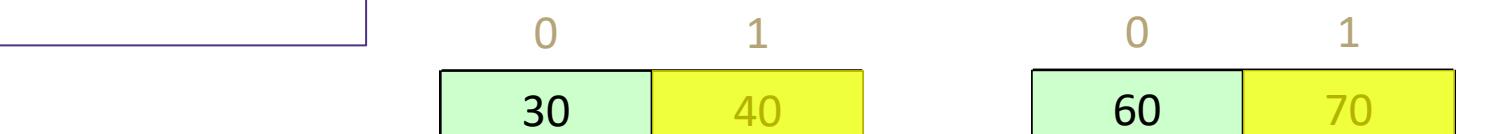
1

40

30

70

60



0

1

0

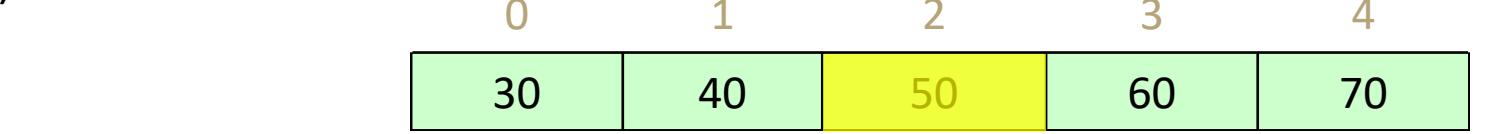
1

30

40

60

70



0

1

2

3

4

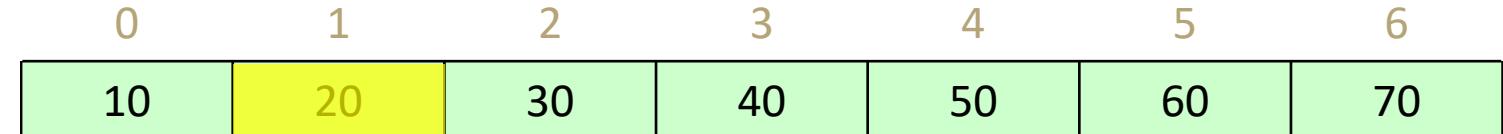
30

40

50

60

70



0

1

2

3

4

5

6

10

20

30

40

50

60

70

# Can we do better?

Pick a better pivot

- Pick a random number
- Pick the median of the first, middle and last element

Sort elements by swapping around pivot in place

# Better Quick Sort

