Dijkstra's Algorithm:

1. Consider the following graph:



a. Use Dijkstra's algorithm to find the costs of the shortest paths from **A** to each of the other vertices. Show your work at every step.

- b. Are any of the costs you computed using Dijkstra's algorithm in part (a) incorrect? Why or why not?
- c. Explain how you can use Dijkstra's algorithm the recover the actual paths from **A** to each of the vertices (rather than just the costs).

Minimum Spanning Trees:

2. Consider the following graph:



a. Find an MST of this graph using Prim's algorithm. Show your work.

b. Find an MST of this graph using Kruskal's algorithm. Show your work.

- c. Does this graph have multiple MSTs? Why or why not?
- d. What are the asymptotic runtimes of Prim's and Kruskal's algorithms?

3. Draw an undirected graph with at least 5 nodes and 6 edges that has exactly three Minimum Spanning Trees

4. Consider the following graph:



- a. Draw the adjacency list representation of this graph.
- b. Write pseudocode for deleting an edge on a directed graph implemented using an adjacency list.
- c. What is the asymptotic runtime of your pseudocode?