1. Given a graph with \(|V|\) vertices and \(|E|\) edges, what is the space requirement (in big-O) for representing the graph.

   As an adjacency list?

   As an adjacency matrix?

2. So far we’ve implemented Depth First Search (DFS) and Breadth First Search (BFS) using data structures to keep track of pending vertices (Stacks and Queues).

   Write pseudocode for DFS using a Stack instead of recursion.
3. Suppose you have social network data for some people (including yourself and a famous person). Write pseudocode to find the answers to the following questions:

   a. How would you represent this social network with a graph?

   b. Given two people, how would you determine if they were friends?

   c. Find the person with the most friends in the data?

   d. Find the length of the shortest path from yourself to the famous person.

   e. Find the number of people who do not know anyone you know (or anyone they know, etc).
4. Suppose you are given a graph $G$. Explain how you would figure out if it has a cycle.

   a. If the graph is undirected:

   b. If the graph is directed: