

CSE 373

MAY 3RD – HASHING & GRAPHS

ASSORTED MINUTIAE

- **Exams are in my office, you can pick them up during any of my office hours.**
- **HW4 out tomorrow morning**
- **Regrade requests processed**
- **H2P2 and H3P1 will be back next week**
- **Finishing discussion on hashing today, so section tomorrow will be all examples.**

MAKE UP ASSIGNMENT

- **Make up assignment end of Week 7**
 - Choose **either** a coding assignment or a write-up assignment
 - Will overwrite your lowest grade for either
 - EC will be possible on these assignments, so it could give bonus points

TODAYS LECTURE

- **Hashing considerations**
- **Introduction to graphs**

HASH FUNCTION

- **In reality, good hash functions are difficult to produce**
 - We want a hash that distributes our data evenly throughout the space
 - Usually, our hash function returns some integer, which must then be modded to our table size
 - Needs to incorporate all the data in the keys

HASH FUNCTION

- **You will not have to produce hash functions, but you should recognize good ones**
 - They run in constant time
 - They evenly distribute the data
 - They return an integer
- **These hash functions are chosen in advance, you should not pick a hash function relative to your data**

COLLISIONS

- **Hash table methods are defined by how they handle collisions**
- **Two main approaches**
 - Probing
 - Chaining

COLLISIONS

- **Probing**

- Linear probing
 - Try the appropriate hash table row first
 - Increase the index by one until a spot is found
 - Guaranteed to find a spot if it is available
 - If the array is too full, its operations reach $O(n)$ time

COLLISIONS

- **Probing**

- Quadratic Probing

- Rather than increasing by one each time, we increase by the squares
 - $k+1, k+4, k+9, k+16, k+25$
 - Certain tables can cause **secondary clustering**
 - Can fail to insert if the table is over half full

COLLISIONS

- **Probing**

- Secondary Hashing

- If two keys collide in the hash table, then a secondary hash indicates the probing size
 - Need to be careful, possible for infinite loops with a very empty array

COLLISIONS

- **Chaining**

- Rather than probing for an open position, we could just save multiple objects in the same position
- Some data structure is necessary here
- Commonly a linked list, AVL tree or secondary hash table.
- Resizing isn't **necessary**, but if you don't, you will get $O(n)$ runtime.

PRIMALITY

- **Array sizes**

- We normally choose our hash tables to have prime size
- This is because for any number we pick, so long as it is not a multiple of our table size, they must be coprime
- Two numbers x and y are **coprime** if they do not share any common factors.
- If the hash table size and the secondary hash value are coprime, then the search will succeed if there is space available
- However, many primes cause secondary clustering when used with quadratic probing

LOAD FACTOR

- When discussing hash table efficiency, we call the proportion of stored data to table size the *load factor*. It is represented by the Greek character lambda (λ).
 - We've discussed this a bit implicitly before
 - What are good load-factor (λ) values for each of our collision techniques?

LOAD FACTOR

- **Linear Probing?**
- **Quadratic Probing?**
- **Secondary Hashing?**
- **Chaining?**
- **What are the tradeoffs?**
 - Memory efficiency
 - Failure rate
 - Access times?

LOAD FACTOR

- **Linear Probing?** $0.25 < \lambda < 0.5$
- **Quadratic Probing?** $0.10 < \lambda < 0.30$
- **Secondary Hashing?** $0.25 < \lambda < 0.5$
- **Chaining?** $3.0 < \lambda < 10$
 - Because we allow multiple items in each space, we can increase memory efficiency by taking advantage
 - As long as there are a constant number in each space, we get $O(1)$ runtimes.

LOAD FACTOR

- **As with most array data structures, you will need to resize when they get too full**
 - Here, these resizes are often for performance, rather than failure.
 - Hash table maintenance is important
 - Resizing is costly (but still $O(n)$) because you have to resize the array and rehash every element into the new table.

HASH TABLES

- Hash tables are a good overall data structure
 - Can provide $O(1)$ access times
 - Can be memory inefficient
 - Probing can fail, and delete with probing mechanisms is difficult
 - Chaining can be a good balance, but there is a lot of overhead maintaining all those data structures

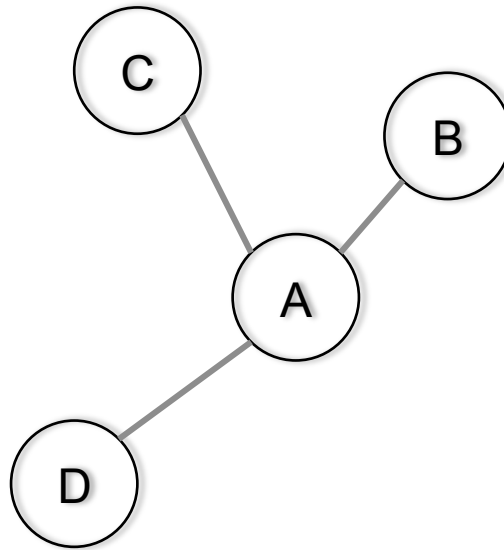
HASH TABLES

- **Understand these tradeoffs and how these implementations work**
- **Section tomorrow will provide practice problems for each of these hash table methods**

GRAPHS

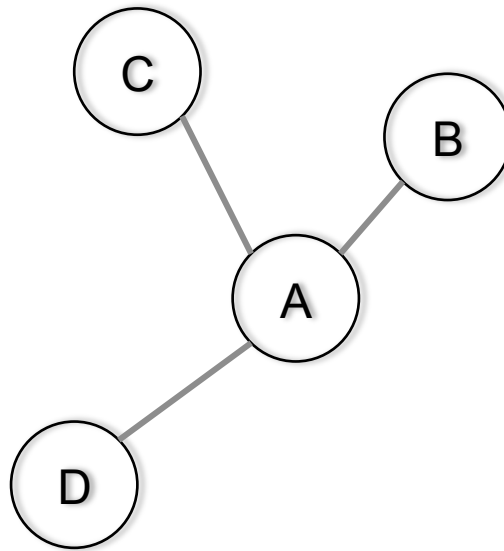
- **A graph is composed of two things**
 - A set of vertices
 - A set of edges (which are vertex tuples)
- **Trees are types of graphs**
 - Each of the nodes is a vertex
 - Each pointer from parent to child is an edge
- **Represented as $G(V,E)$ to indicate that V is the set of vertices and E is the set of edges**

GRAPHS



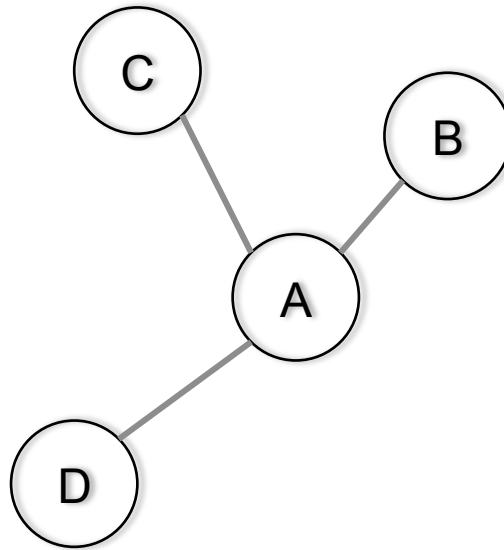
- What this graphs vertices and edges?

GRAPHS



- What this graphs vertices and edges?
 - $V = \{A, B, C, D\}$
 - $E = \{(A,B), (A,C), (A,D)\}$

GRAPHS

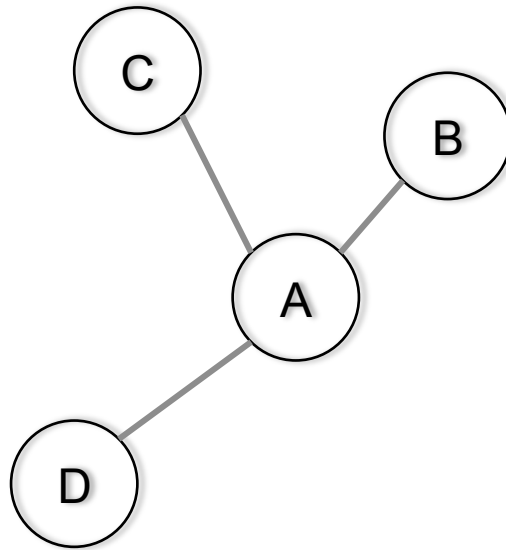


- What this graphs vertices and edges?
 - $V = \{A, B, C, D\}$
 - $E = \{(B,A), (C,A), (D,A)\}$?

GRAPHS

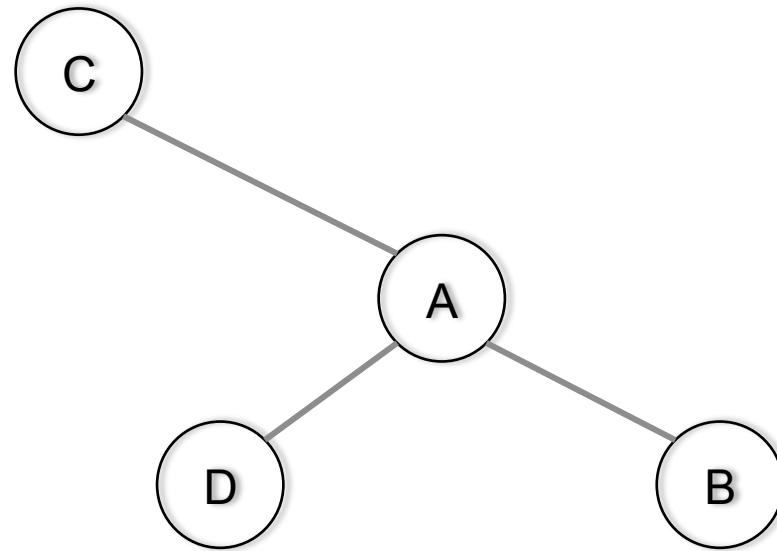
- In that graph, the order did not matter
- This is called an undirected graph
 - In undirected graphs, an edge from (A,B) means that there must be an edge from (B,A)
 - In implementation, both of these edges need to be present, but if you indicate that a graph is undirected, you do not need to indicate both in your list of edges

GRAPHS



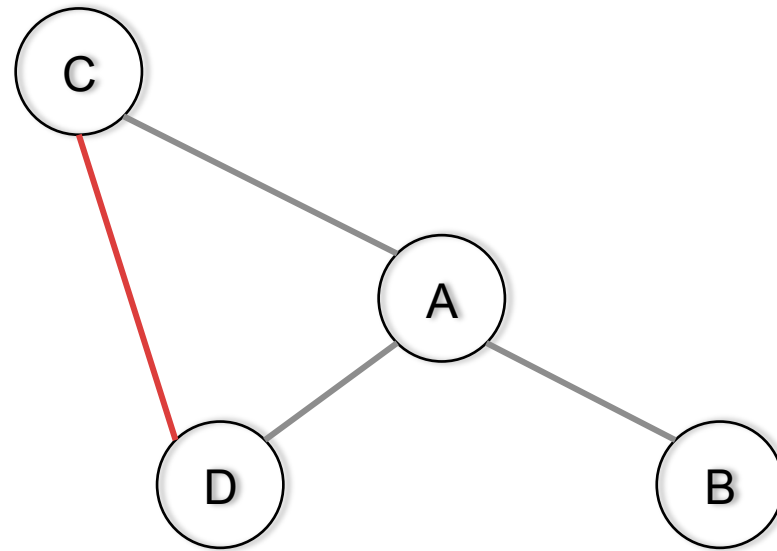
- Is this graph a tree?

GRAPHS



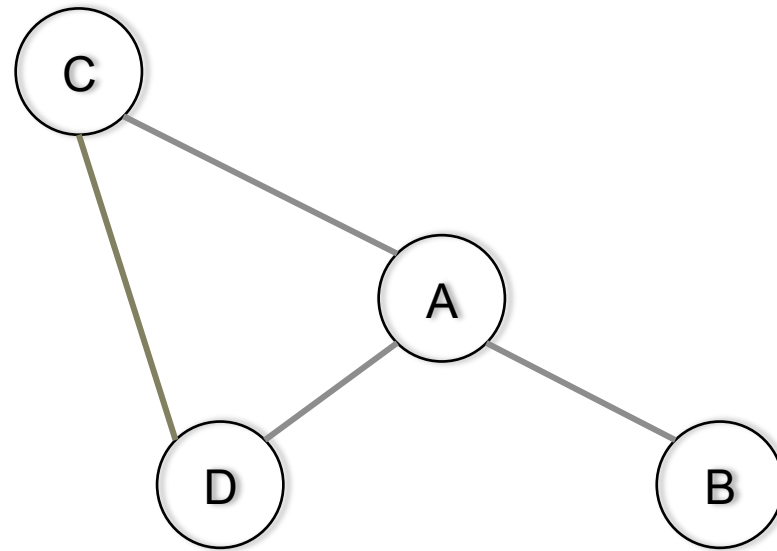
- **Is this graph a tree?**
 - Yes, you can make the shape by moving vertices around

GRAPHS



- Is this graph a tree?

GRAPHS

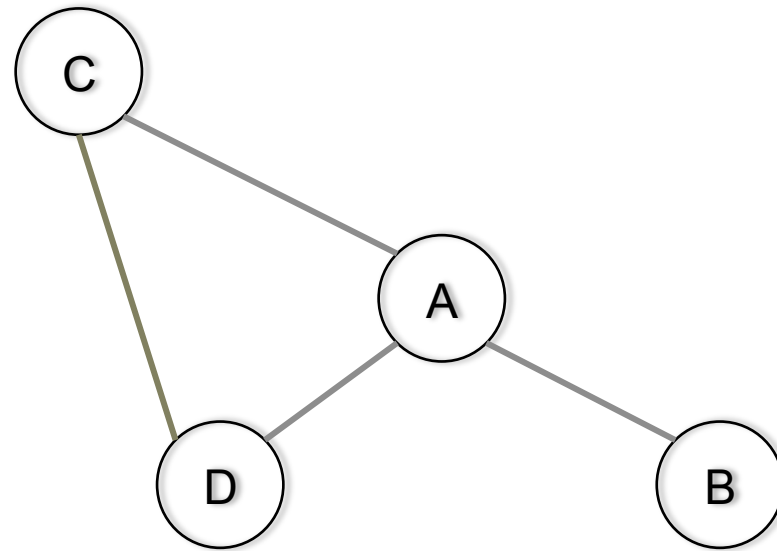


- Is this graph a tree?
 - No, there is no way to rearrange these vertices because there is a **cycle**

GRAPHS

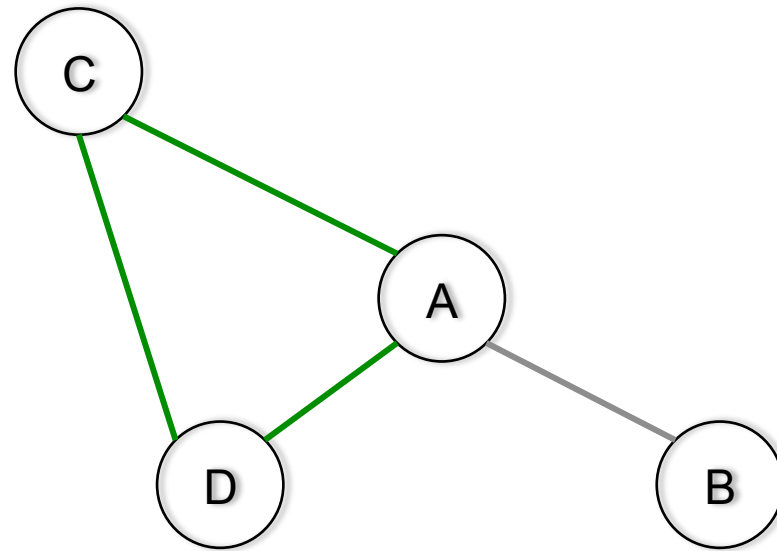
- A path is a set of edges which goes from one vertex to another in a graph
- A cycle is a path that starts and ends on the same vertex.
- A graph is *acyclic* if no cycles exist in the graph

GRAPHS



- What is the cycle here?

GRAPHS



- What is the cycle here?
 - (A,D) (D,C) (C,A)

GRAPHS

- In paths and cycles, the sets of edges must pass from one vertex to another, i.e. each edge must share a vertex with some other edge.
 - $(A,B) (B,C)$ is a path from A to C, while $(A,B) (D,C)$ is not.
 - There is no way to get from B to D

GRAPHS

- **Trees are acyclic graphs**
- **Graphs can be traversed**
 - Breadth-first
 - Depth-first
- **Edges can also have weights**
 - Path finding on a map
 - Route-optimization problems

NEXT CLASS

- **More graphs!**
- **Discuss implementation approaches**
- **Prepare for path finding problem for next week**