

## Priority Queues: Binary Min Heaps

CSE 373  
Data Structures and Algorithms

1/27/2012

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## Today's Outline

- **Announcements**
  - Midterm #1, Monday Jan 30.
  - Assignment #3 coming soon, due until Mon Feb 6.
- **Today's Topics:**
  - **Dictionary**
    - Balanced Binary Search Trees - (AVL Trees)
  - **Priority Queues**
    - Binary Min Heap

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## Priority Queue ADT

1. **PQueue data** : collection of data with priority
2. **PQueue operations**
  - insert
  - deleteMin(also: create, destroy, is\_empty)
3. **PQueue property**: for two elements in the queue,  $x$  and  $y$ , if  $x$  has a **lower** priority value than  $y$ ,  $x$  will be deleted before  $y$

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## Applications of the Priority Q

- Select print jobs in order of decreasing **length**
- Forward packets on network routers in order of **urgency**
- Select most **frequent** symbols for compression
- Sort numbers, picking **minimum** first
- **Anything greedy**

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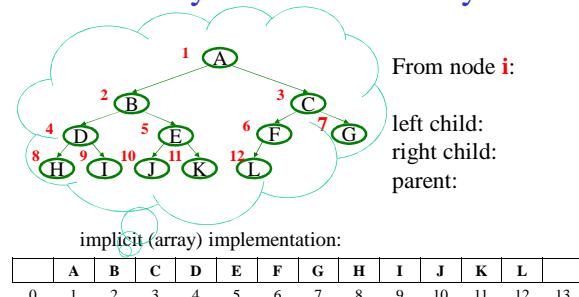
## Implementations of Priority Queue ADT

	insert	deleteMin
Unsorted list (Array)		
Unsorted list (Linked-List)		
Sorted list (Array)		
Sorted list (Linked-List)		
Binary Search Tree (BST)		

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## Representing Complete Binary Trees in an Array



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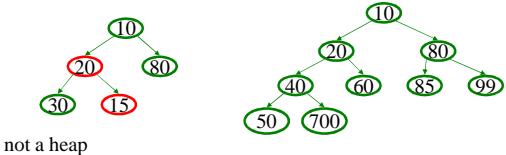
## Why better than tree with pointers?

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## Heap Order Property

**Heap order property:** For every non-root node X, the value in the parent of X is less than (or equal to) the value in X.

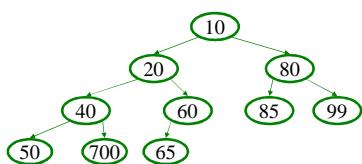


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## Heap Operations

- findMin:
- insert(val): percolate up.
- deleteMin: percolate down.



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## Heap – Insert(val)

Basic Idea:

1. Put val at “next” leaf position
2. Repeatedly exchange node with its parent if needed

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## Insert pseudo Code (optimized)

```
void insert(Object o) {
    assert(!isFull());
    size++;
    newPos =
        percolateUp(size,o);
    Heap[newPos] = o;
}
```

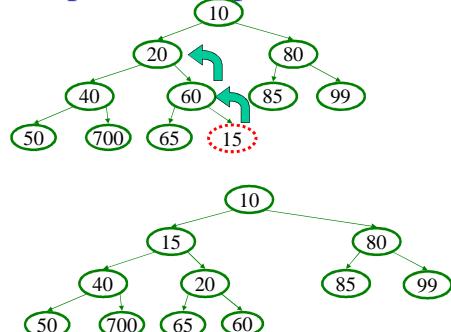
runtime:

(Java code in book)

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## Insert: percolate up



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## Heap – DeleteMin

Basic Idea:

1. Remove root (that is always the min!)
2. Put “last” leaf node at root
3. Find smallest child of node
4. Swap node with its smallest child if needed.
5. Repeat steps 3 & 4 until no swaps needed.

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## DeleteMin pseudo Code (Optimized)

```

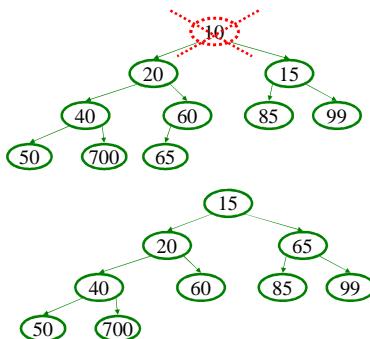
Object deleteMin() {
    assert(!isEmpty());
    returnVal = Heap[1];
    size--;
    newPos =
        percolateDown(1,
                      Heap[size+1]);
    Heap[newPos] =
        Heap[size + 1];
    return returnVal;
}

runtime:
    (Java code in book)
}
    
```

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## DeleteMin: percolate down



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Insert: 16, 32, 4, 69, 105, 43, 2

0	1	2	3	4	5	6	7	8

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## Other Priority Queue Operations

### • decreaseKey

- given a pointer to an object in the queue, reduce its priority value

Solution: change priority and \_\_\_\_\_

### • increaseKey

- given a pointer to an object in the queue, increase its priority value

Solution: change priority and \_\_\_\_\_

**Why do we need a pointer? Why not simply data value?**

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## Other Heap Operations

**decreaseKey(objPtr, amount):** raise the priority of a object, percolate up

**increaseKey(objPtr, amount):** lower the priority of a object, percolate down

**remove(objPtr):** remove a object, move to top, them delete.

- 1) decreaseKey(**objPtr**,  $\infty$ )

- 2) deleteMin()

Worst case Running time for all of these:

FindMax?

ExpandHeap – when heap fills, copy into new space.

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## Binary Min Heaps (summary)

- **insert:** percolate up.  $\Theta(\log N)$  time.
- **deleteMin:** percolate down.  $\Theta(\log N)$  time.
- **Build Heap?**

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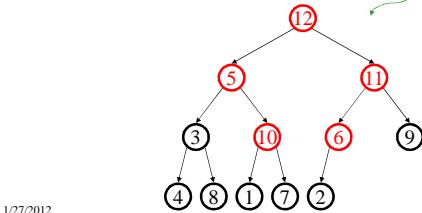
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## BuildHeap: Floyd's Method

12	5	11	3	10	6	9	4	8	1	7	2
----	---	----	---	----	---	---	---	---	---	---	---

Add elements arbitrarily to form a complete tree.

Pretend it's a heap and fix the heap-order property!



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## Buildheap pseudocode

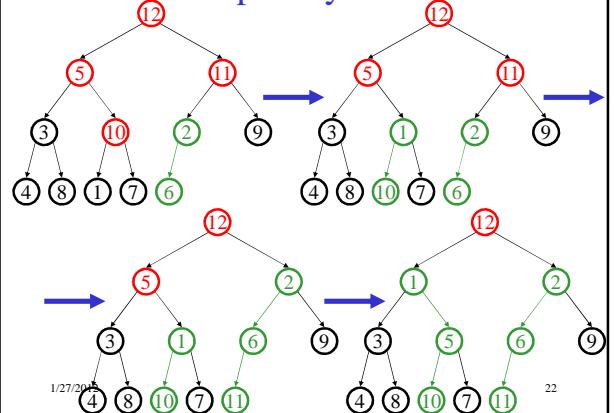
```
private void buildHeap() {
    for ( int i = currentSize/2; i > 0; i-- )
        percolateDown( i );
}
```

runtime:

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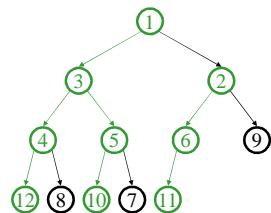
## BuildHeap: Floyd's Method



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Finally...



runtime:

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