



# CSE 373

## Data Structures and Algorithms

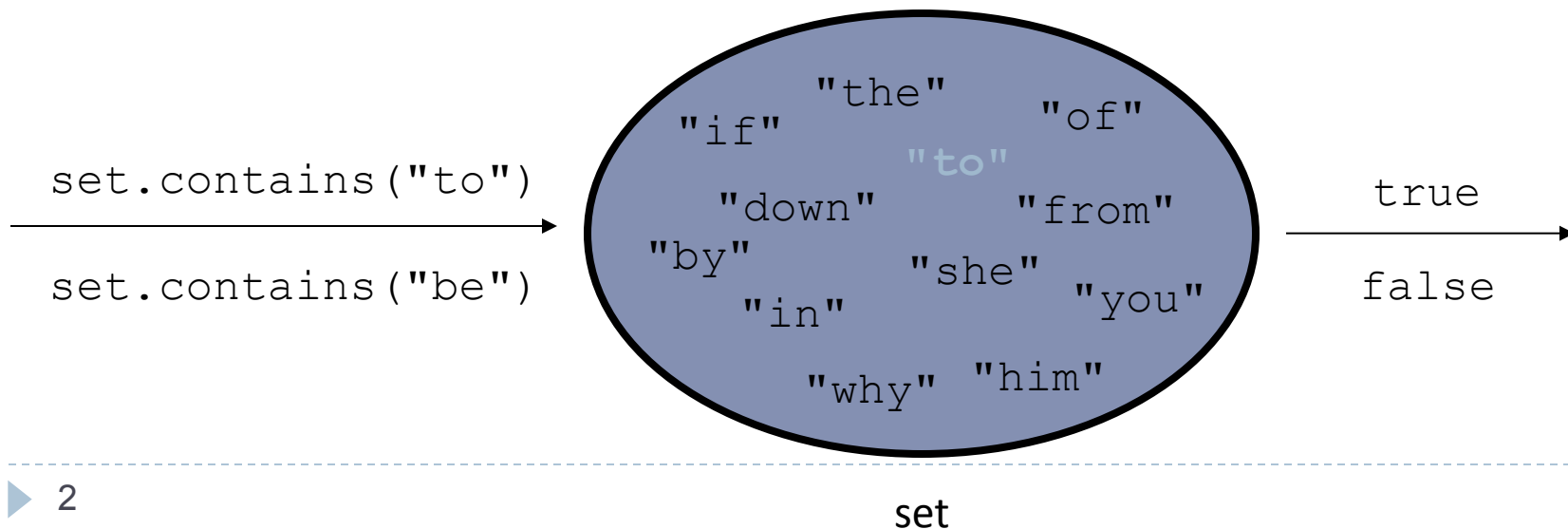


Lecture 9: Set ADT / Trees

# Set ADT

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- ▶ **set:** A collection that does not allow duplicates
  - ▶ We don't think of a set as having indices or any order
- ▶ **Basic set operations:**
  - ▶ **insert:** Add an element to the set (order doesn't matter).
  - ▶ **remove:** Remove an element from the set.
  - ▶ **search:** Efficiently determine if an element is a member of the set.



# Sets in computer science

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- ▶ **Databases:**

- ▶ Set of records in a table

- ▶ **Search engines:**

- ▶ Set of URLs/webpages on the Internet

- ▶ **Real world examples:**

- ▶ Set of all products for sale in a store inventory
  - ▶ Set of friends on Facebook
  - ▶ Set of email addresses

# Using Sets

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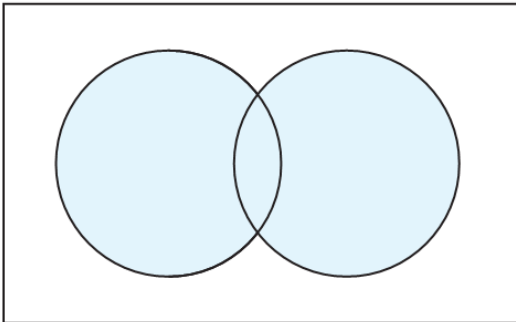
<code>add(<b>value</b>)</code>	adds the given value to the set
<code>contains(<b>value</b>)</code>	returns <code>true</code> if the given value is found in this set
<code>remove(<b>value</b>)</code>	removes the given value from the set
<code>clear()</code>	removes all elements of the set
<code>size()</code>	returns the number of elements in list
<code>isEmpty()</code>	returns <code>true</code> if the set's size is 0
<code>toString()</code>	returns a string such as " <code>[3, 42, -7, 15]</code> "

```
List<String> list = new ArrayList<String>();  
...  
Set<Integer> set = new TreeSet<Integer>();           // empty  
Set<String> set2 = new HashSet<String>(list);
```

- ▶ Can construct an empty set, or one based on a given collection

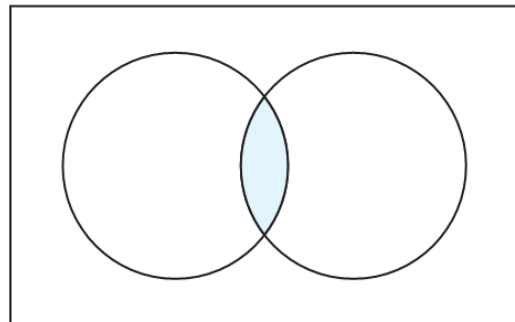
# More Set operations

$A \cup B$  Union



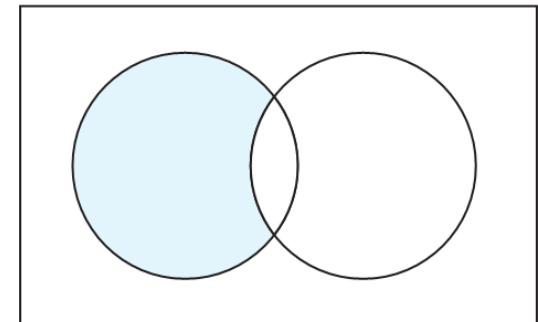
`addAll`

$A \cap B$  Intersection



`retainAll`

$A - B$  Difference



`removeAll`

<code>addAll (<b>collection</b>)</code>	adds all elements from the given collection to this set
<code>containsAll (<b>coll</b>)</code>	returns <code>true</code> if this set contains every element from given set
<code>equals (<b>set</b>)</code>	returns <code>true</code> if given other set contains the same elements
<code>iterator()</code>	returns an object used to examine set's contents
<code>removeAll (<b>coll</b>)</code>	removes all elements in the given collection from this set
<code>retainAll (<b>coll</b>)</code>	removes elements <i>not</i> found in given collection from this set
<code>toArray()</code>	returns an array of the elements in this set

# Accessing elements in a Set

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```
for (type name : collection) {  
    statements;  
}
```

- ▶ Provides a clean syntax for looping over the elements of a Set, List, array, or other collection

```
Set<Double> grades = new TreeSet<Double>();  
...
```

```
for (double grade : grades) {  
    System.out.println("Student grade: " + grade);  
}
```

- ▶ needed because sets have no indexes; can't get element i

# Sets and ordering

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- ▶ **HashSet** : elements are stored in an unpredictable order

```
Set<String> names = new HashSet<String>();  
names.add("Jake");  
names.add("Robert");  
names.add("Marisa");  
names.add("Kasey");  
System.out.println(names);  
// [Kasey, Robert, Jake, Marisa]
```

- ▶ **TreeSet** : elements are stored in their "natural" sorted order

```
Set<String> names = new TreeSet<String>();  
...  
// [Jake, Kasey, Marisa, Robert]
```

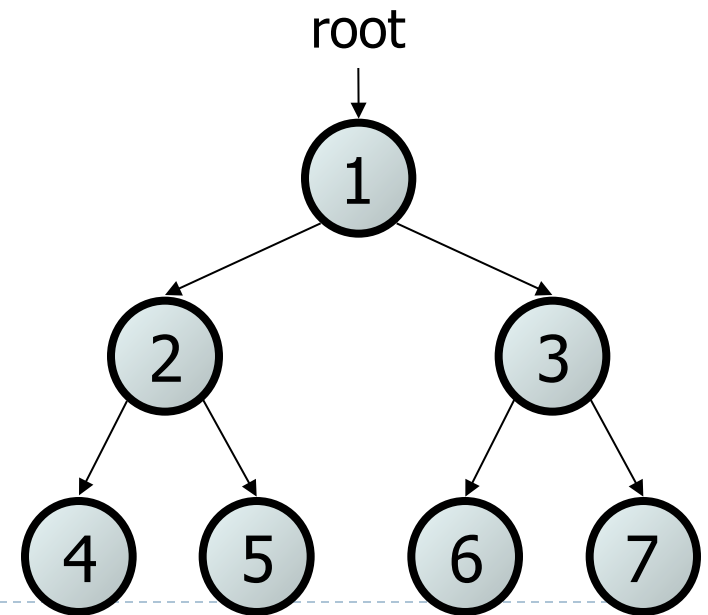
# Set Implementation Runtimes

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	Insert	Remove	Search
Unsorted array	$\Theta(n)$	$\Theta(n)$	$\Theta(n)$
Sorted array	$\Theta(\log(n)+n)$	$\Theta(\log(n) + n)$	$\Theta(\log(n))$
Linked list	$\Theta(n)$	$\Theta(n)$	$\Theta(n)$

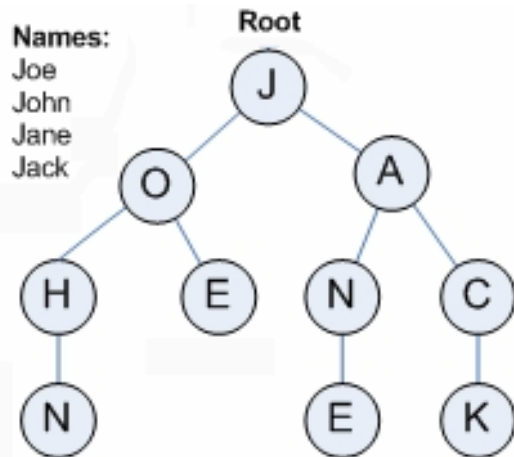
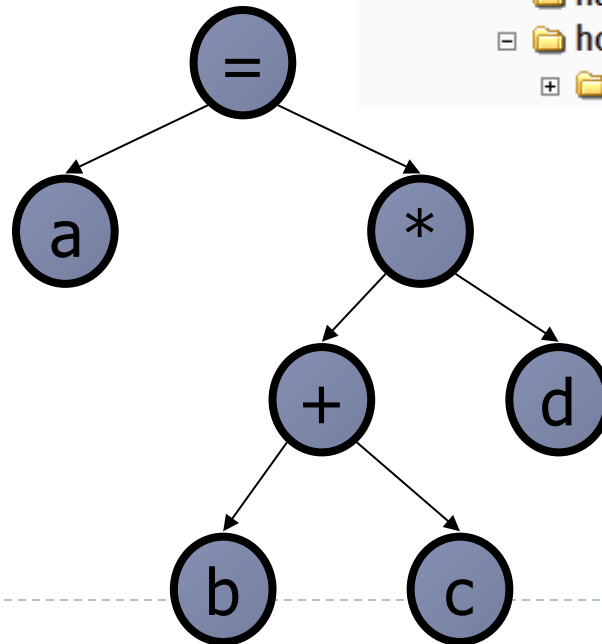
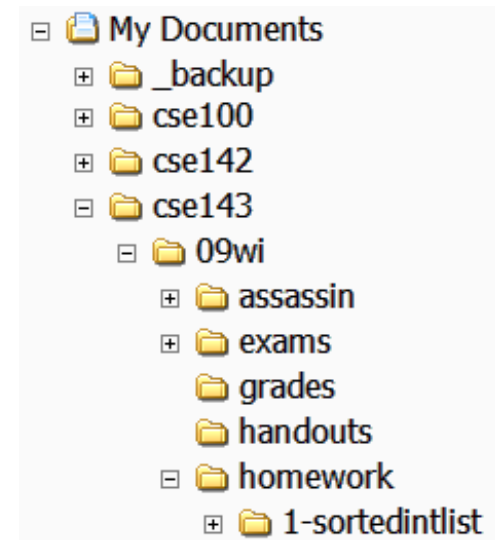
# Trees

- ▶ **tree**: A directed, acyclic structure of linked nodes.
  - ▶ *directed*: Has one-way links between nodes.
  - ▶ *acyclic*: No path wraps back around to the same node twice.
  - ▶ **binary tree**: One where each node has at most two children.
- ▶ A binary tree can be defined as either:
  - ▶ empty (`null`), or
  - ▶ a **root** node that contains:
    - ▶ **data**
    - ▶ a **left** subtree and a **right** subtree
      - Either (or both) subtrees could be empty.



# Trees in computer science

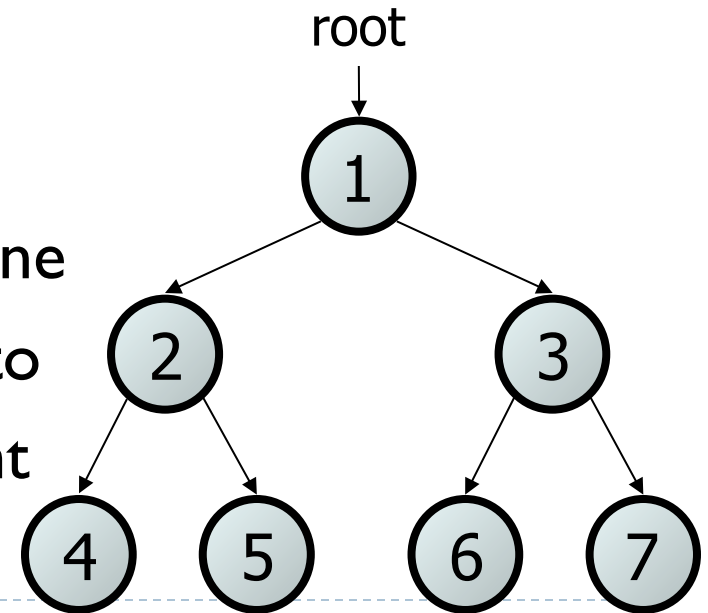
- ▶ folders/files on a computer
- ▶ family genealogy; organizational charts
- ▶ AI: decision trees
- ▶ compilers: parse tree
  - ▶  $a = (b + c) * d$ ;
- ▶ cell phone T9



# Terminology

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- ▶ **node**: an object containing a data value and left/right children
- ▶ **root**: topmost node of a tree
- ▶ **leaf**: a node that has no children
- ▶ **branch**: any internal node; neither the root nor a leaf
- ▶ **parent**: a node that refers to this one
- ▶ **child**: a node that this node refers to
- ▶ **sibling**: a node with common parent



# StringTreeNode class

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**// A StringTreeNode object is one node in a binary tree of Strings.**

```
public class StringTreeNode {
    public String data;           // data stored at this node
    public StringTreeNode left;   // reference to left subtree
    public StringTreeNode right;  // reference to right subtree

    // Constructs a leaf node with the given data.
    public StringTreeNode(String data) {
        this(data, null, null);
    }

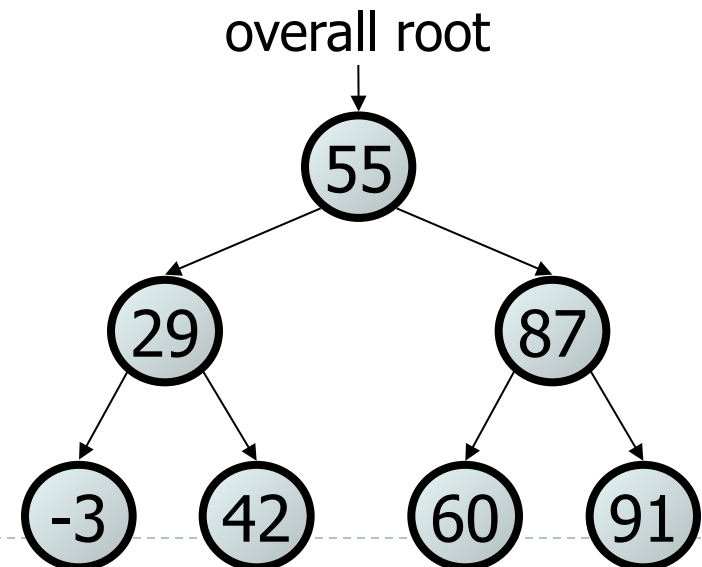
    // Constructs a leaf or branch node with the given data and links.
    public StringTreeNode(String data, StringTreeNode left,
        StringTreeNode right) {
        this.data = data;
        this.left = left;
        this.right = right;
    }
}
```

# Binary search trees

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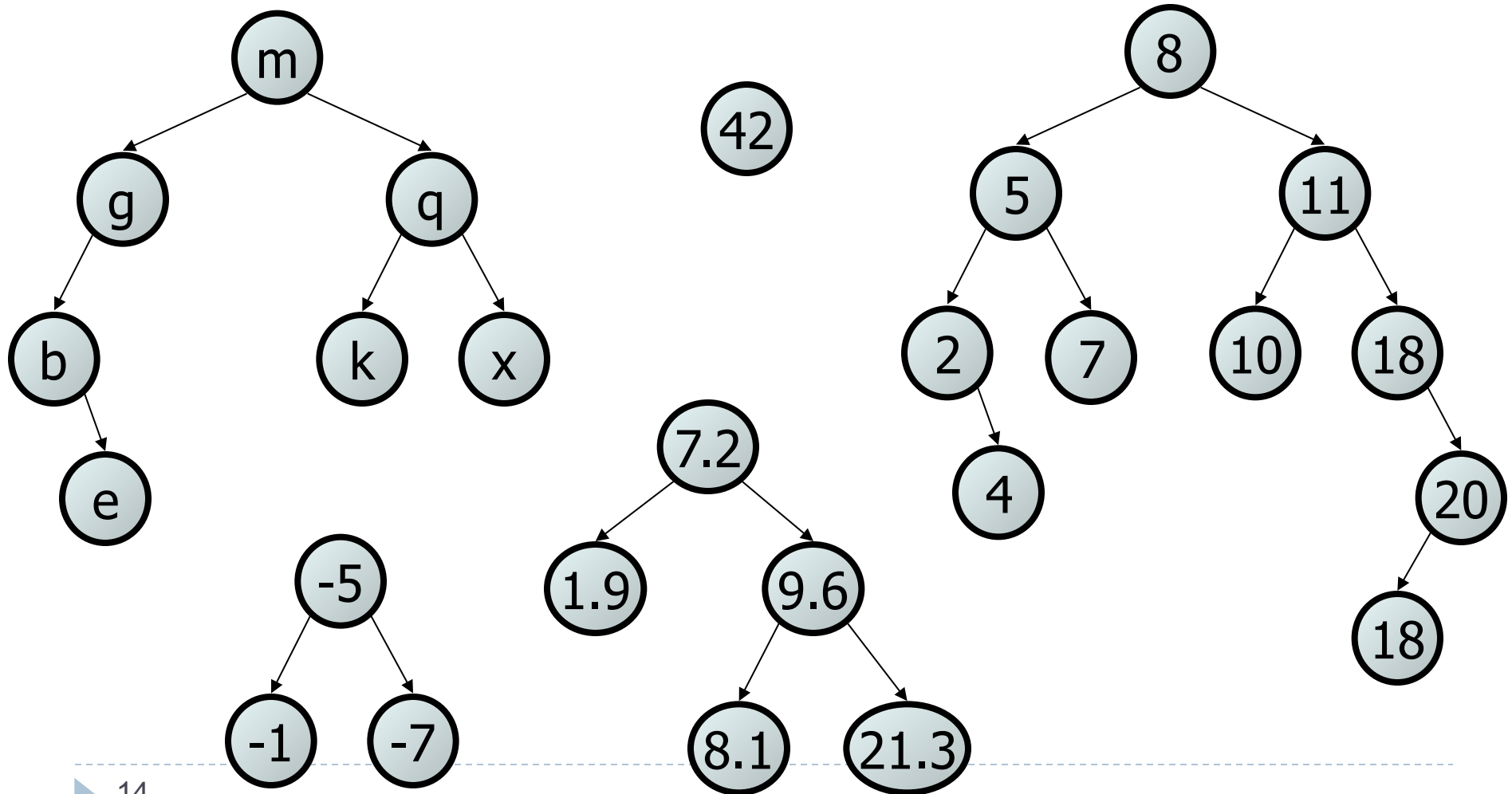
- ▶ binary search tree ("BST"): a binary tree that is either:
  - ▶ empty (`null`), or
  - ▶ a root node `R` such that:
    - ▶ every element of `R`'s left subtree contains data "less than" `R`'s data,
    - ▶ every element of `R`'s right subtree contains data "greater than" `R`'s,
    - ▶ `R`'s left and right subtrees are also binary search trees.

- ▶ BSTs store their elements in sorted order, which is helpful for searching/sorting tasks.



# Exercise

- ▶ Which of the trees shown are legal binary search trees?



# Programming with Binary Trees

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- ▶ Many tree algorithms are recursive
  - ▶ Process current node, recurse on subtrees
  - ▶ Base case is usually empty tree (`null`)
- ▶ **traversal**: An examination of the elements of a tree.
  - ▶ A pattern used in many tree algorithms and methods
- ▶ Common orderings for traversals:
  - ▶ **pre-order**: process root node, then its left/right subtrees
  - ▶ **in-order**: process left subtree, then root node, then right
  - ▶ **post-order**: process left/right subtrees, then root node

# Tree Traversal (in order)

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```
// Returns a String representation of StringTreeSet with elements in
// their "natural order" (e.g., [Jake, Kasey, Marisa, Robert]).
public String toString() {
    String str = "[" + toString(root);
    if (str.length() > 1) { str = str.substring(0, str.length()-2); }
    return str + "]";
}

// recursive helper; in-order traversal
private String toString(StringTreeNode root) {
    String str = "";
    if (root != null) {
        str += toString(root.left);
        str += root.data + ", ";
        str += toString(root.right);
    }
    return str;
}
```