Graphs

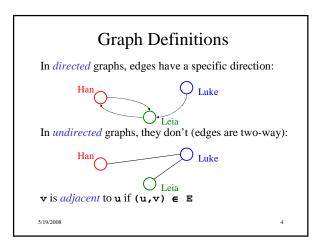
Chapter 9 in Weiss

5/19/2008

Today's Outline

- Announcements
 - HW#5 due NOW
 - Midterm #2 this Friday
 - · Topics, sample exam posted
- Graphs

Graph... ADT? • Not quite an ADT... operations not clear · A formalism for representing relationships between objects Graph g = (v, E)- Set of vertices: $V = \{v_1, v_2, ..., v_n\}$ {Han, Leia, Luke} {(Luke, Leia), Set of edges: (Han, Leia), (Leia, Han)} $E = \{e_1, e_2, ..., e_m\}$ where each $\mathbf{e_i}$ connects two vertices (v_{i1}, v_{i2})



More Definitions: Simple Paths and Cycles

A simple path repeats no vertices (except that the first can be the last):

p = {Seattle, Salt Lake City, San Francisco, Dallas}

p = {Seattle, Salt Lake City, Dallas, San Francisco, Seattle}

A *cycle* is a path that starts and ends at the same node:

p = {Seattle, Salt Lake City, Dallas, San Francisco, Seattle}

p = {Seattle, Salt Lake City, Seattle, San Francisco, Seattle}

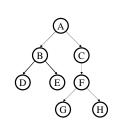
A simple cycle is a cycle that repeats no vertices except that the first vertex is also the last (in undirected graphs, no edge can be repeated)

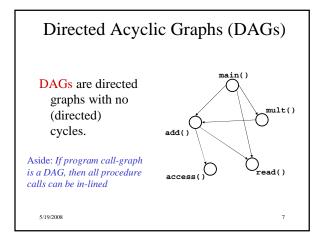
Trees as Graphs

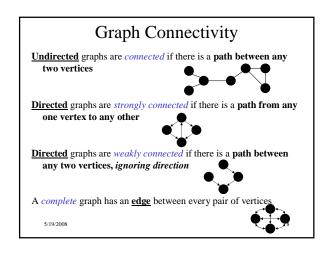
- Every tree is a graph!
- Not all graphs are trees!

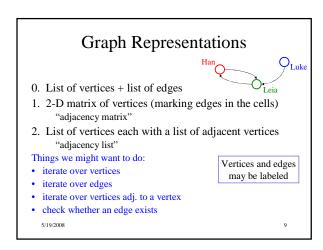
A graph is a tree if

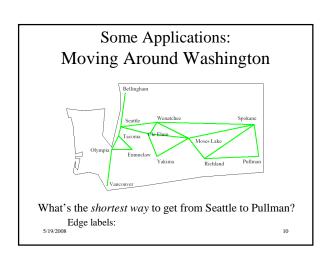
- There are no cycles (directed or undirected)
- There is a *path* from the root to every node

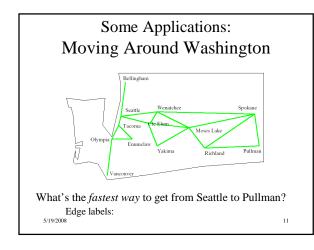


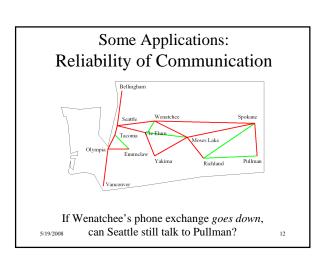


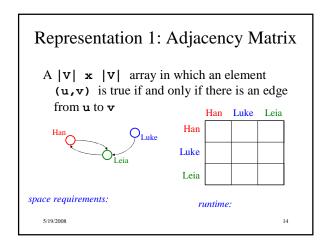


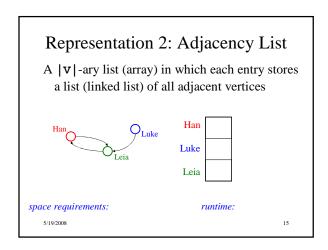


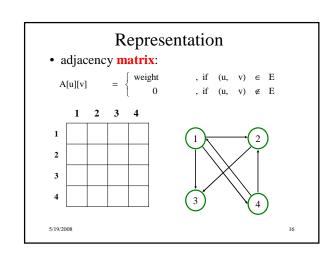


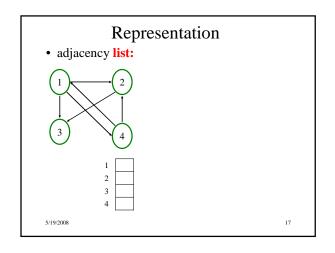


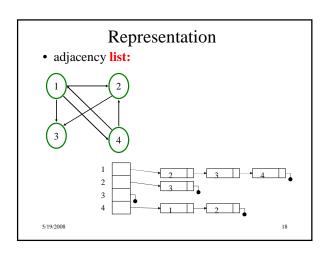




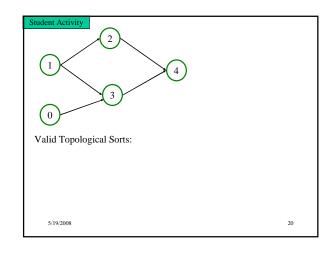








Application: Topological Sort Given a directed graph, G = (V, E), output all the vertices in v such that no vertex is output before any other vertex with an edge to it. CSE 403 CSE 321) CSE 322 CSE 421) (CSE 142)→(CSE 143) CSE 341) CSE 451) (CSE 370) CSE 467) CSE 378 Is the output unique? 19



```
void Graph::topsort(){
   Vertex v, w;

labelEachVertexWithItsIn-degree();

for(int count=0; count<NUM_VERTICES; count++){
   v = findNewVertexOfDegreeZero();

   v.topoNum = count;
   for each w adjacent to v
        w.indegree--;
   }
}</pre>
```

```
roid Graph::topsort(){
   Queue q(NUM_VERTICES); int counter = 0; Vertex v, w;
   labelEachVertexWithItsIn-degree();
  q.makeEmpty();
                                intialize the
   for each vertex v
                                  queue
    if (v.indegree == 0)
       q.enqueue(v);
  while (!q.isEmpty()){ | get a vertex with
     v = q.dequeue();
                                indegree 0
     v.topologicalNum = ++counter;
     for each \boldsymbol{w} adjacent to \boldsymbol{v}
       if (--w.indegree == 0)
                                     insert new
         q.enqueue(w);
                                      eligible
                                      vertices
}
                                     Runtime:
    5/19/2008
                                                            23
```