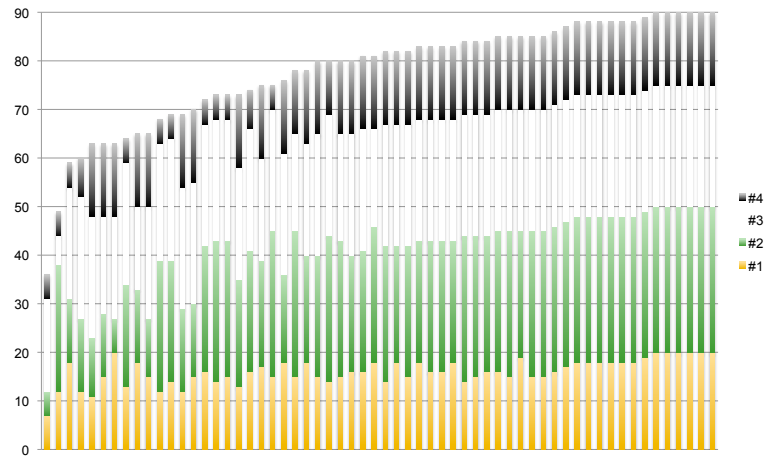


Exam 1 Results

- Average = 78; Median = 81; StDev = 11.1 (68% within 67 and 89)

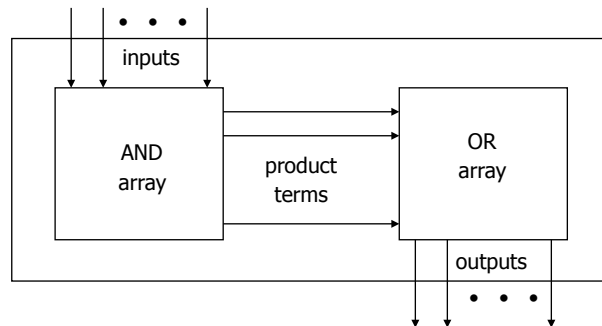


Implementation Technologies

- Standard gates (pretty much done)
 - gate packages
 - cell libraries
- Regular logic (we've been here)
 - multiplexers
 - decoders
- Two-level programmable logic (we are now here)
 - PALs, PLAs, PLDs
 - ROMs
 - FPGAs

Programmable logic arrays

- Pre-fabricated building block of many AND/OR gates
 - actually NOR or NAND
 - "personalized" by making/breaking connections among the gates
 - programmable array block diagram for sum of products form



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Enabling concept

- Shared product terms among outputs

example:

$$\begin{aligned}
 F0 &= A + B' C' \\
 F1 &= A C' + A B \\
 F2 &= B' C' + A B \\
 F3 &= B' C + A
 \end{aligned}$$

personality matrix

product term	inputs			outputs			
	A	B	C	F0	F1	F2	F3
AB	1	1	-	0	1	1	0
B'C	-	0	1	0	0	0	1
AC'	1	-	0	0	1	0	0
B'C'	-	0	0	1	0	1	0
A	1	-	-	1	0	0	1

input side:

1 = uncomplemented in term
 0 = complemented in term
 - = does not participate

output side:

1 = term connected to output
 0 = no connection to output

reuse of terms

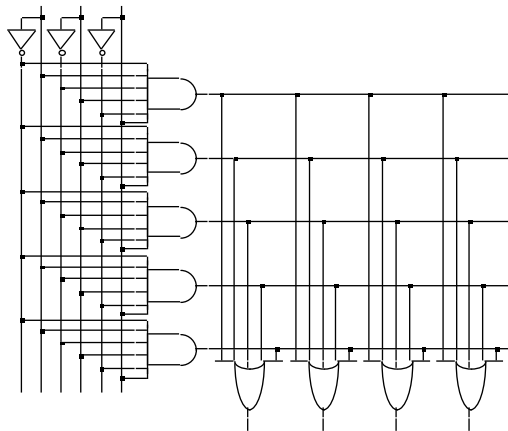
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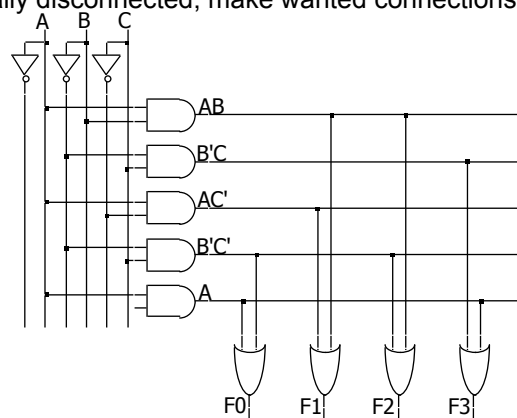
Before programming

- All possible connections are available before "programming"
 - in reality, all AND and OR gates are NANDs



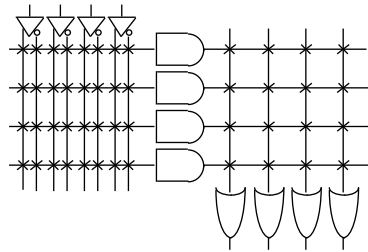
After programming

- Unwanted connections are "blown"
 - fuse (normally connected, break unwanted ones)
 - anti-fuse (normally disconnected, make wanted connections)



Alternate representation for high fan-in structures

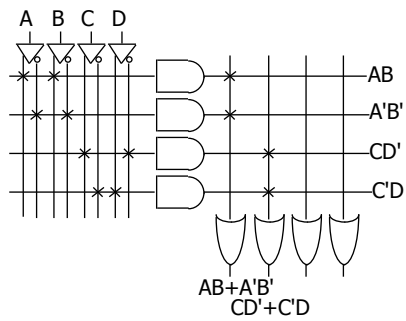
- Short-hand notation so we don't have to draw all the wires
 - \times signifies a connection is present and perpendicular signal is an input to gate



notation for implementing

$$F0 = A B + A' B'$$

$$F1 = C D' + C' D$$

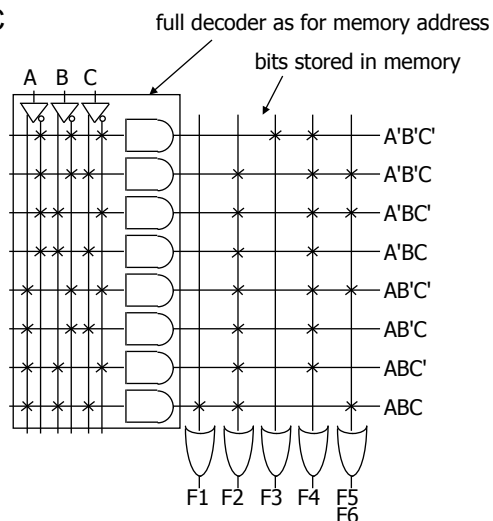


Programmable logic array example

- Multiple functions of A, B, C

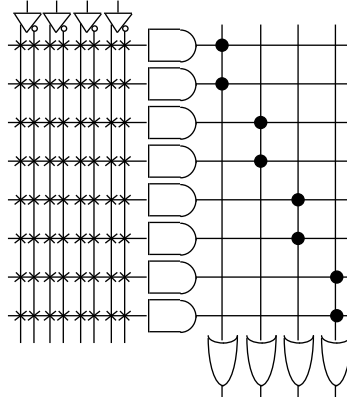
- $F1 = A B C$
- $F2 = A + B + C$
- $F3 = A' B' C'$
- $F4 = A' + B' + C'$
- $F5 = A \text{ xor } B \text{ xor } C$
- $F6 = A \text{ xnor } B \text{ xnor } C$

A	B	C	F1	F2	F3	F4	F5	F6
0	0	0	0	0	1	1	0	0
0	0	1	0	1	0	1	1	1
0	1	0	0	1	0	1	1	1
0	1	1	0	1	0	1	0	0
1	0	0	0	1	0	1	1	1
1	0	1	0	1	0	1	0	0
1	1	0	0	1	0	1	0	0
1	1	1	1	1	0	0	1	1



PALs and PLAs

- Programmable logic array (PLA)
 - what we've seen so far
 - unconstrained fully-general AND and OR arrays
- Programmable array logic (PAL)
 - constrained topology of the OR array
 - innovation by Monolithic Memories
 - faster and smaller OR plane



a given column of the OR array has access to only a subset of the possible product terms

PALs and PLAs: design example

- BCD to Gray code converter

A	B	C	D	W	X	Y	Z
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	1	1
0	0	1	1	0	0	1	0
0	1	0	0	0	1	1	0
0	1	0	1	1	1	1	0
0	1	1	0	1	0	1	0
0	1	1	1	1	0	1	1
1	0	0	0	1	0	0	1
1	0	0	1	1	0	0	0
1	0	1	-	-	-	-	-
1	1	-	-	-	-	-	-

minimized functions:

$$W = A + BD + BC$$

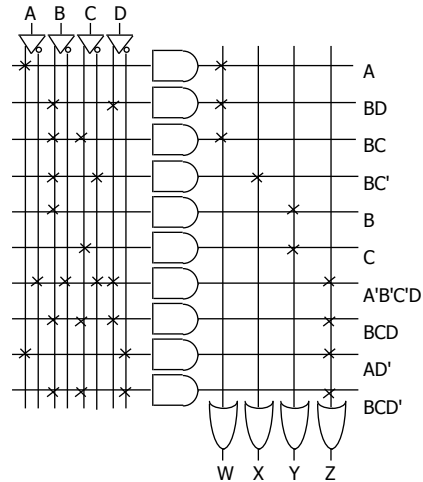
$$X = BC'$$

$$Y = B + C$$

$$Z = A'B'C'D + BCD + AD' + B'CD'$$

PALs and PLAs: design example (cont'd)

- Code converter: programmed PLA



minimized functions:

$$\begin{aligned} W &= A + BD + BC \\ X &= B C' \\ Y &= B + C \\ Z &= A'B'C'D + BCD + AD' + B'CD' \end{aligned}$$

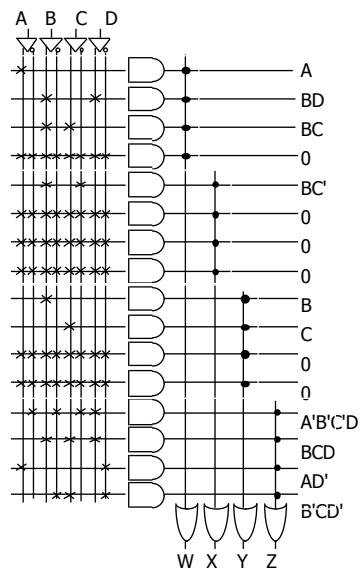
not a particularly good candidate for PAL/PLA implementation since no terms are shared among outputs

however, much more compact and regular implementation when compared with discrete AND and OR gates

PALs and PLAs: design example (cont'd)

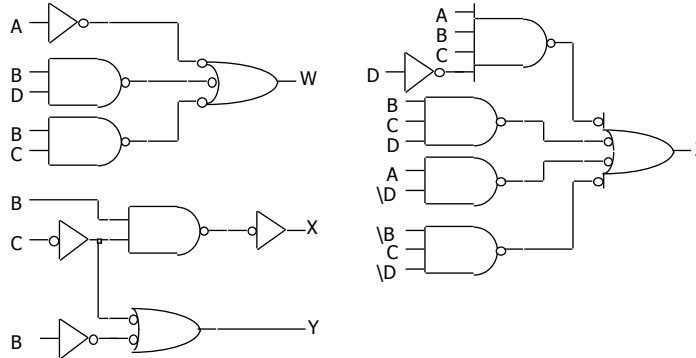
- Code converter: programmed PAL

4 product terms per each OR gate



PALs and PLAs: design example (cont'd)

- Code converter: NAND gate implementation
 - loss of regularity, harder to understand
 - harder to make changes



PALs and PLAs: another design example

- Magnitude comparator

A	B	C	D	EQ	NE	LT	GT
0	0	0	0	1	0	0	0
0	0	0	1	0	1	1	0
0	0	1	0	0	1	1	0
0	0	1	1	0	1	1	0
0	1	0	0	0	1	0	1
0	1	0	1	1	0	0	0
0	1	1	0	0	1	1	0
0	1	1	1	0	1	1	0
1	0	0	0	0	1	0	1
1	0	0	1	0	1	0	1
1	0	1	0	1	0	0	0
1	0	1	1	0	1	1	0
1	1	0	0	0	1	0	1
1	1	0	1	0	1	0	1
1	1	1	0	0	1	0	1
1	1	1	1	1	0	0	0

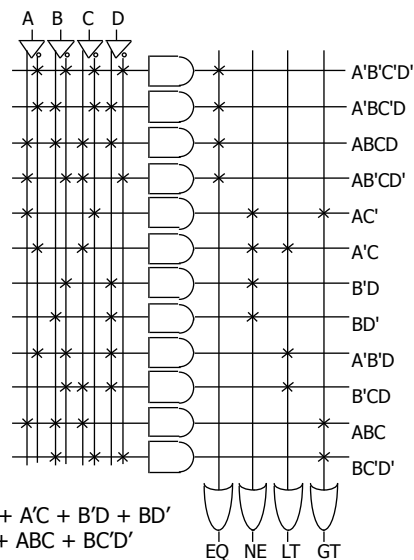
minimized functions:

$$EQ = A'B'C'D' + A'BC'D + ABCD + AB'CD'$$

$$LT = A'C + A'B'D + B'CD$$

$$NE = AC' + A'C + B'D + BD'$$

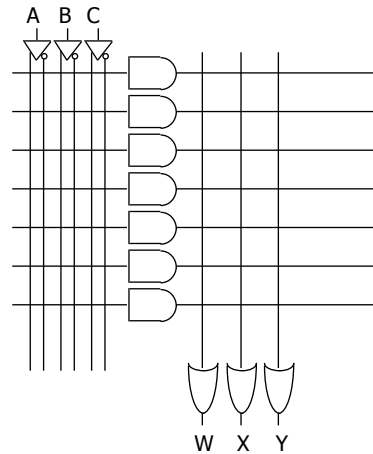
$$GT = AC' + ABC + BC'D'$$



Activity

- Map the following functions to the PLA below:

- $W = AB + A'C' + BC'$
- $X = ABC + AB' + A'B$
- $Y = ABC' + BC + B'C'$



Activity (cont'd)

- 9 terms won't fit in a 7 term PLA

- can apply consensus theorem to W to simplify to:
 $W = AB + A'C'$

- 8 terms won't fit in a 7 term PLA

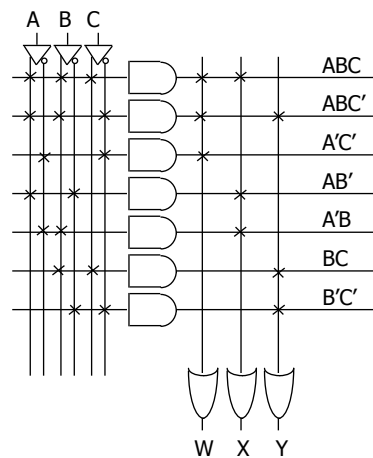
- observe that $AB = ABC + ABC'$
- can rewrite W to reuse terms:
 $W = ABC + ABC' + A'C'$

- Now it fits

- $W = ABC + ABC' + A'C'$
- $X = ABC + AB' + A'B$
- $Y = ABC' + BC + B'C'$

- This is called technology mapping

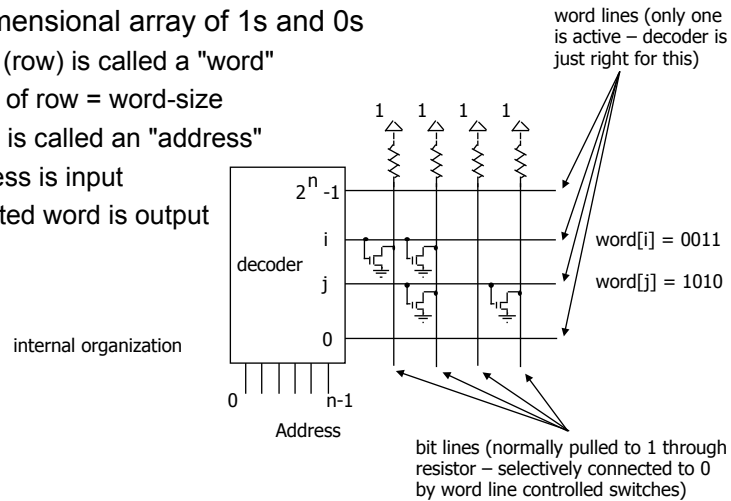
- manipulating logic functions so that they can use available resources



Read-only memories

- Two dimensional array of 1s and 0s

- entry (row) is called a "word"
- width of row = word-size
- index is called an "address"
- address is input
- selected word is output



ROMs and combinational logic

- Combinational logic implementation (two-level canonical form) using a ROM

$$F_0 = A' B' C + A' B C' + A B' C$$

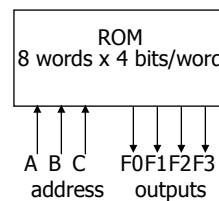
$$F_1 = A' B' C + A' B C' + A B C$$

$$F_2 = A' B' C' + A' B' C + A B' C'$$

$$F_3 = A' B C + A B' C' + A B C'$$

A	B	C	F0	F1	F2	F3
0	0	0	0	0	1	0
0	0	1	1	1	1	0
0	1	0	0	1	0	0
0	1	1	0	0	0	1
1	0	0	1	0	1	1
1	0	1	1	0	0	0
1	1	0	0	0	0	1
1	1	1	0	1	0	0

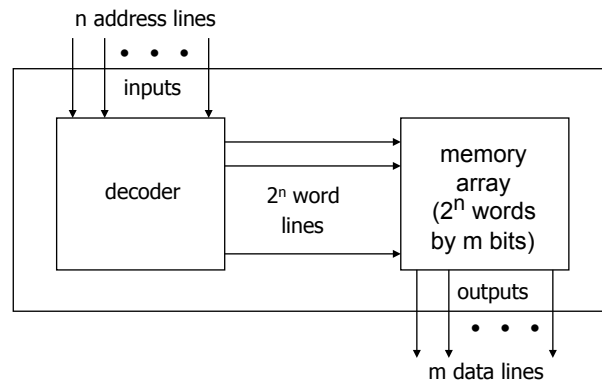
truth table



block diagram

ROM structure

- Similar to a PLA structure but with a fully decoded AND array
 - completely flexible OR array (unlike PAL)



ROM vs. PLA

- ROM approach advantageous when
 - design time is short (no need to minimize output functions)
 - most input combinations are needed (e.g., code converters)
 - little sharing of product terms among output functions
- ROM problems
 - size doubles for each additional input
 - can't exploit don't cares
- PLA approach advantageous when
 - design tools are available for multi-output minimization
 - there are relatively few unique minterm combinations
 - many minterms are shared among the output functions
- PAL problems
 - constrained fan-ins on OR plane

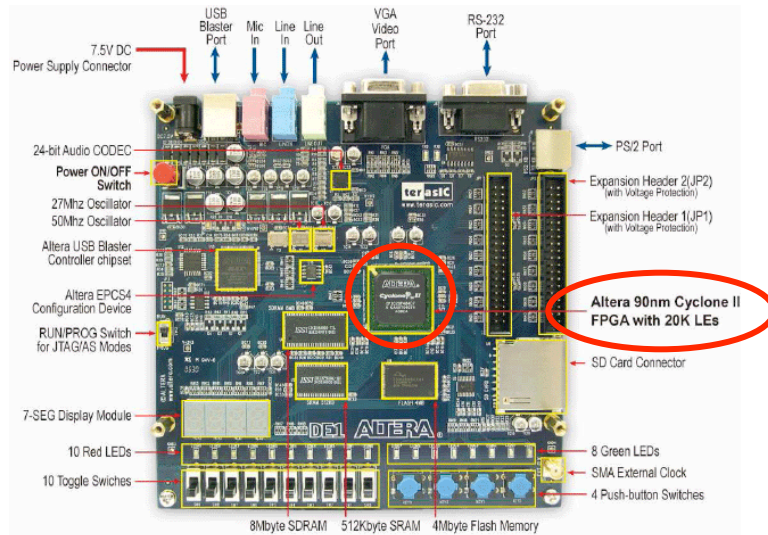
Regular logic structures for two-level logic

- ROM – full AND plane, general OR plane
 - cheap (high-volume component)
 - can implement any function of n inputs
 - medium speed
- PAL – programmable AND plane, fixed OR plane
 - intermediate cost
 - can implement functions limited by number of terms
 - high speed (only one programmable plane that is much smaller than ROM's decoder)
- PLA – programmable AND and OR planes
 - most expensive (most complex in design, need more sophisticated tools)
 - can implement any function up to a product term limit
 - slow (two programmable planes)

Regular logic structures for multi-level logic

- Difficult to devise a regular structure for arbitrary connections between a large set of different types of gates
 - efficiency/speed concerns for such a structure
 - next we'll learn about field programmable gate arrays (FPGAs) that are just such programmable multi-level structures
 - programmable multiplexers for wiring
 - lookup tables for logic functions (programming fills in the table)
 - multi-purpose cells (utilization is the big issue)
 - much more about these in CSE467
- Alternative to FPGAs: use multiple levels of PALs/PLAs/ROMs
 - output intermediate result
 - make it an input to be used in further logic
 - no longer practical approach given prevalence of FPGAs

FPGAs in CSE370



<http://www.altera.com/products/devices/cyclone2/overview/cy2-overview.html>

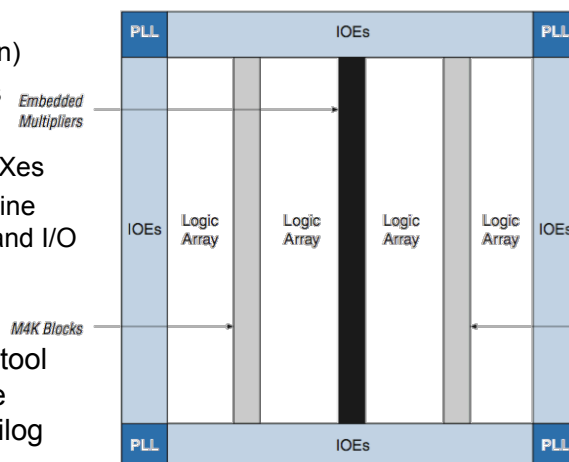
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Cyclone II architecture

- Logic array blocks (LABs)
 - 4-input lookup tables
 - MUXes for which you specify inputs (function)
- Routing rows and cols to interconnect LABs
 - also composed of MUXes
 - select settings determine wires between LABs and I/O
- Many more parts
 - more later
- You will use synthesis tool (compiler) to determine programming from Verilog



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