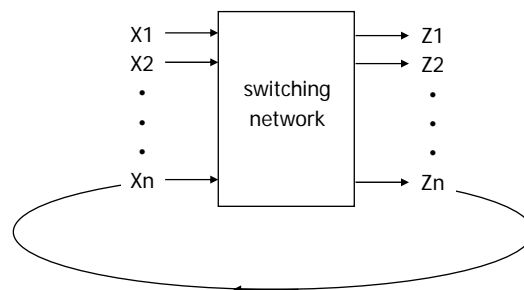


## Sequential logic

- Sequential circuits
  - simple circuits with feedback
  - latches
  - edge-triggered flip-flops
- Timing methodologies
  - cascading flip-flops for proper operation
  - clock skew
- Basic registers
  - shift registers
  - simple counters
- Hardware description languages and sequential logic

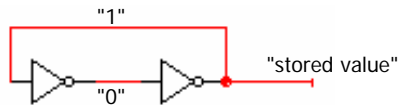
## Circuits with feedback

- How to control feedback?
  - what stops values from cycling around endlessly

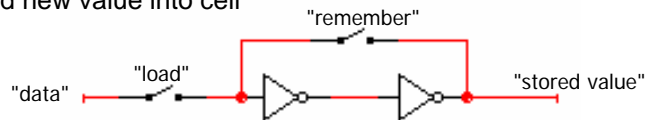


## Simplest circuits with feedback

- Two inverters form a static memory cell
  - will hold value as long as it has power applied



- How to get a new value into the memory cell?
  - selectively break feedback path
  - load new value into cell



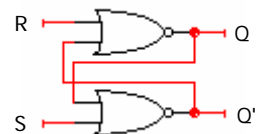
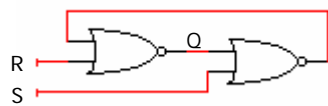
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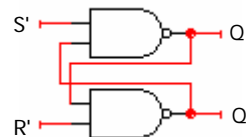
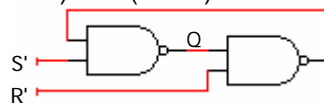
3

## Memory with cross-coupled gates

- Cross-coupled NOR gates
  - similar to inverter pair, with capability to force output to 0 (reset=1) or 1 (set=1)



- Cross-coupled NAND gates
  - similar to inverter pair, with capability to force output to 0 (reset=0) or 1 (set=0)

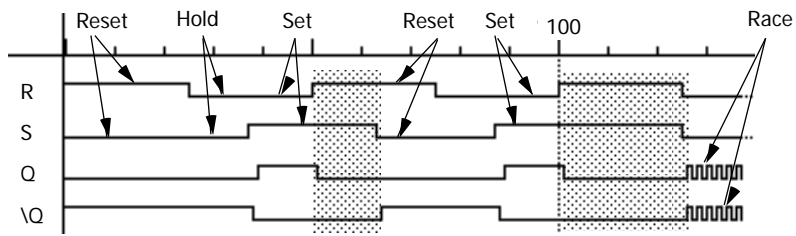
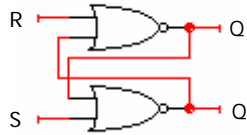


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4

## Timing behavior

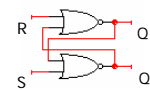


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5

## State behavior of R-S latch



- Truth table of R-S latch behavior

S	R	Q
0	0	hold
0	1	0
1	0	1
1	1	unstable

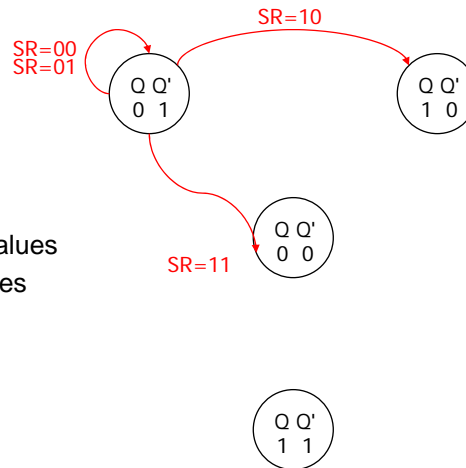
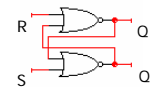


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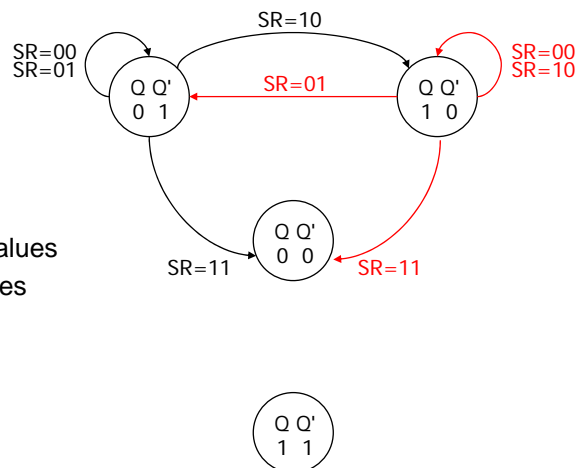
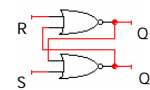
6

## Theoretical R-S latch behavior



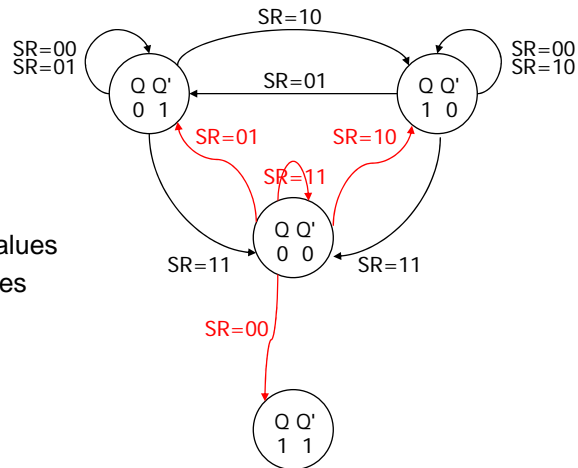
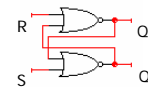
- State diagram
  - states: possible values
  - transitions: changes based on inputs

## Theoretical R-S latch behavior



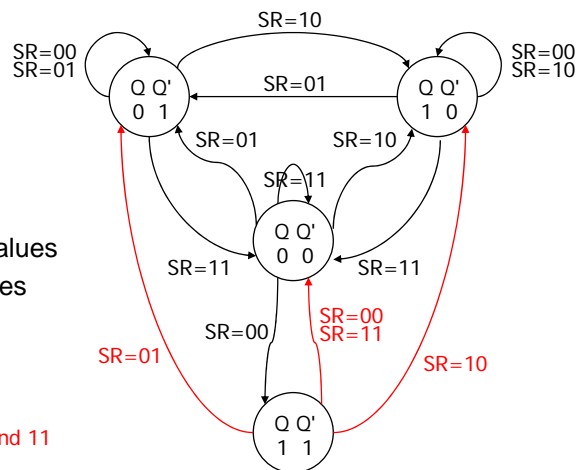
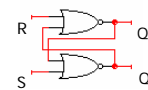
- State diagram
  - states: possible values
  - transitions: changes based on inputs

## Theoretical R-S latch behavior



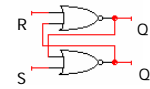
- State diagram
  - states: possible values
  - transitions: changes based on inputs

## Theoretical R-S latch behavior

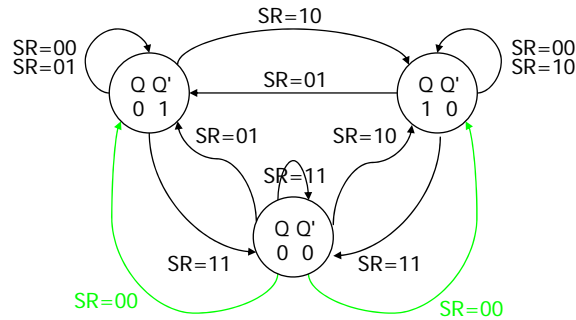


- State diagram
  - states: possible values
  - transitions: changes based on inputs

## Observed R-S latch behavior



- Very difficult to observe R-S latch in the 1-1 state
  - one of R or S usually changes first
- Ambiguously returns to state 0-1 or 1-0
  - a so-called "race condition"
  - or non-deterministic transition



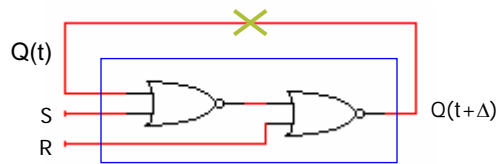
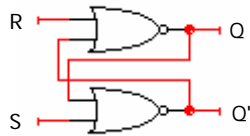
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11

## R-S latch analysis

- Break feedback path



S	R	Q(t)	Q(t+Δ)	
0	0	0	0	hold
0	0	1	1	
0	1	0	0	reset
0	1	1	0	
1	0	0	1	set
1	0	1	1	
1	1	0	X	not allowed
1	1	1	X	

		S	
Q(t)	0	0	1
	1	0	1
		R	

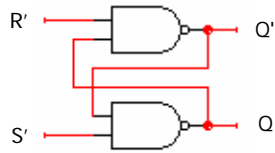
characteristic equation  
 $Q(t+\Delta) = S + R' Q(t)$

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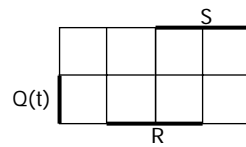
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12

## Activity: R-S latch using NAND gates

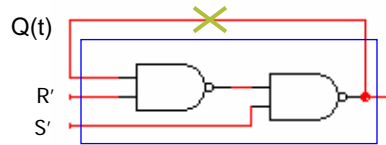
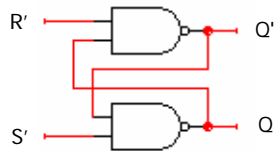


S	R	S'	R'	Q(t)	Q(t+Δ)
0	0	1	1	0	
0	0	1	1	1	
0	1	1	0	0	
0	1	1	0	1	
1	0	0	1	0	
1	0	0	1	1	
1	1	0	0	0	
1	1	0	0	1	

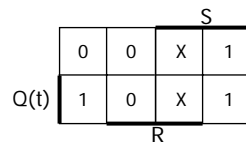


characteristic equation  
 $Q(t+\Delta) =$

## Activity: R-S latch using NAND gates



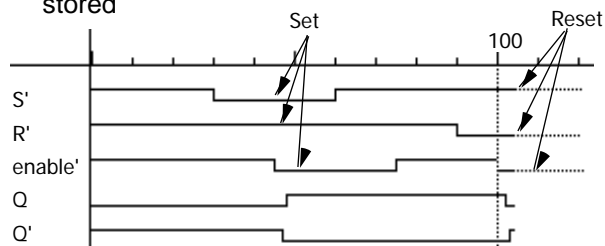
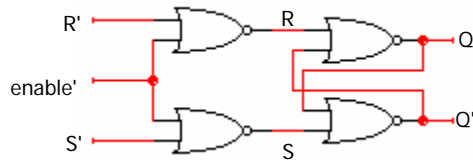
S	R	S'	R'	Q(t)	Q(t+Δ)	
0	0	1	1	0	0	hold
0	0	1	1	1	1	
0	1	1	0	0	0	reset
0	1	1	0	1	0	
1	0	0	1	0	1	set
1	0	0	1	1	1	
1	1	0	0	0	X	not allowed
1	1	0	0	1	X	



characteristic equation  
 $Q(t+\Delta) = S + R' Q(t)$

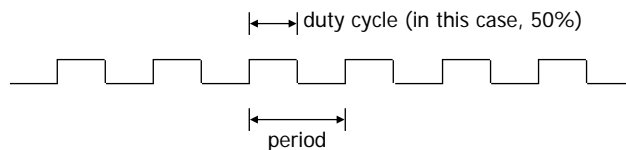
## Gated R-S latch

- Control when R and S inputs matter
  - otherwise, the slightest glitch on R or S while enable is low could cause change in value stored



## Clocks

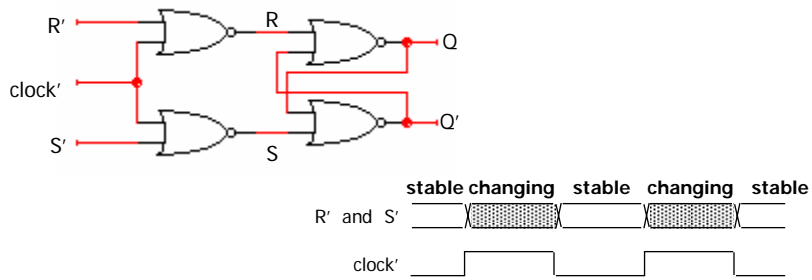
- Used to keep time
  - wait long enough for inputs (R' and S') to settle
  - then allow to have effect on value stored
- Clocks are regular periodic signals
  - period (time between ticks)
  - duty-cycle (time clock is high between ticks - expressed as % of period)





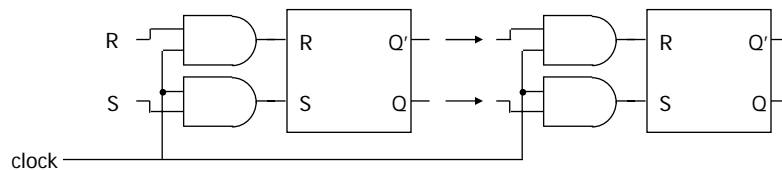
## Clocks (cont'd)

- Controlling an R-S latch with a clock
  - can't let R and S change while clock is active (allowing R and S to pass)
  - only have half of clock period for signal changes to propagate
  - signals must be stable for the other half of clock period



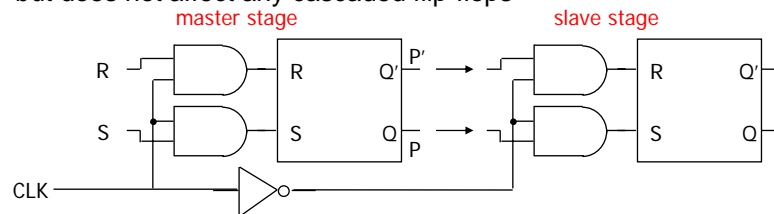
## Cascading latches

- Connect output of one latch to input of another
- How to stop changes from racing through chain?
  - need to be able to control flow of data from one latch to the next
  - move one latch per clock period
  - have to worry about logic between latches (arrows) that is too fast



## Master-slave structure

- Break flow by alternating clocks (like an air-lock)
  - use positive clock to latch inputs into one R-S latch
  - use negative clock to change outputs with another R-S latch
- View pair as one basic unit
  - master-slave flip-flop
  - twice as much logic
  - output changes a few gate delays after the falling edge of clock but does not affect any cascaded flip-flops



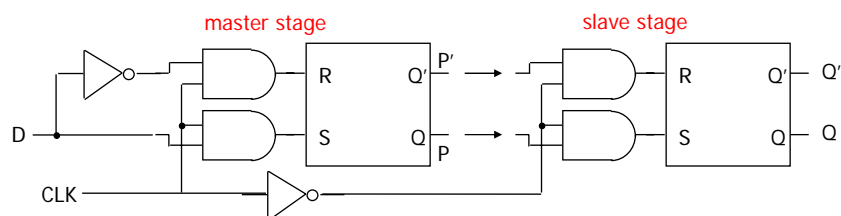
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19

## D flip-flop

- Make S and R complements of each other
  - eliminates 1s catching problem
  - can't just hold previous value (must have new value ready every clock period)
  - value of D just before clock goes low is what is stored in flip-flop
  - can make R-S flip-flop by adding logic to make  $D = S + R' Q$



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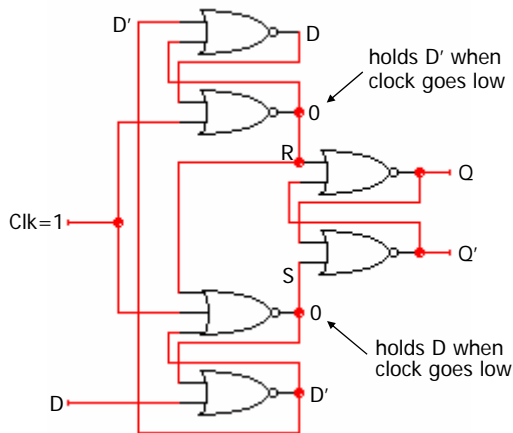
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10 gates

20

## Edge-triggered flip-flops using gates

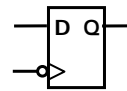
- Only 6 gates
  - sensitive to inputs only near edge of clock signal (not while high)



negative edge-triggered D flip-flop (D-FF)

4-5 gate delays

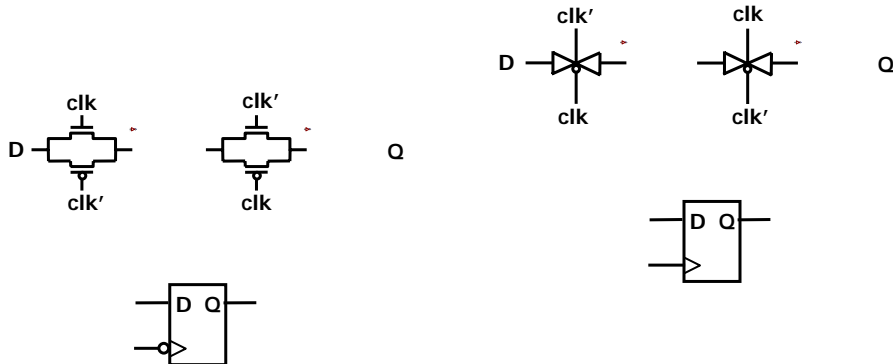
must respect setup and hold time constraints to successfully capture input



characteristic equation  
 $Q(t+1) = D$

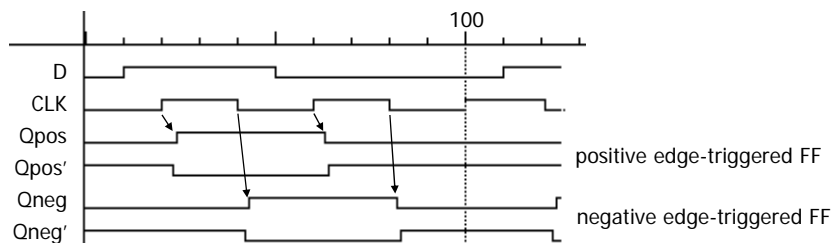
## Edge-triggered flip-flops using transistors

- Only 8 transistors



## Edge-triggered flip-flops (cont'd)

- Positive edge-triggered
  - inputs sampled on rising edge; outputs change after rising edge
- Negative edge-triggered flip-flops
  - inputs sampled on falling edge; outputs change after falling edge



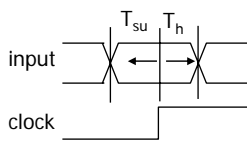
## Timing methodologies

- Rules for interconnecting components and clocks
  - guarantee proper operation of system when strictly followed
- Approach depends on building blocks used for memory elements
  - we'll focus on systems with edge-triggered flip-flops
    - found in programmable logic devices
  - many custom integrated circuits focus on level-sensitive latches
- Basic rules for correct timing:
  - (1) correct inputs, with respect to time, are provided to the flip-flops
  - (2) no flip-flop changes state more than once per clocking event

## Timing methodologies (cont'd)

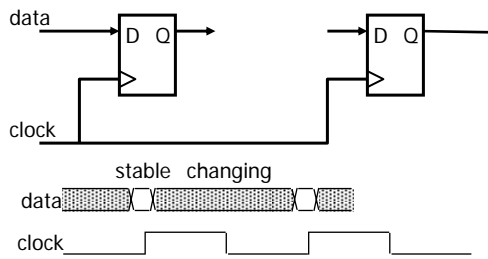
### ■ Definition of terms

- clock: periodic event, causes state of memory element to change  
can be rising edge or falling edge or high level or low level
- setup time: minimum time before the clocking event by which the input must be stable ( $T_{su}$ )
- hold time: minimum time after the clocking event until which the input must remain stable ( $T_h$ )



there is a timing "window" around the clocking event during which the input must remain stable and unchanged in order to be recognized

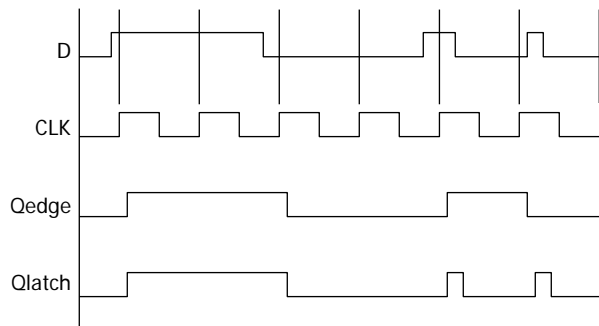
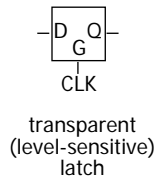
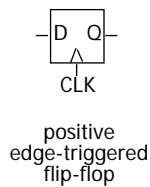
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25

## Comparison of latches and flip-flops



behavior is the same unless input changes while the clock is high

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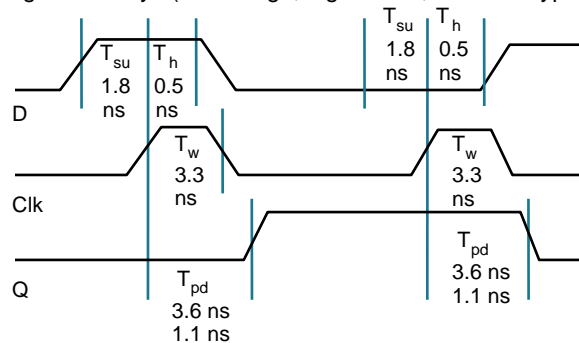
26

## Comparison of latches and flip-flops (cont'd)

Type	When inputs are sampled	When output is valid
unclocked latch	always	propagation delay from input change
level-sensitive latch	clock high ( $T_{su}/T_h$ around falling edge of clock)	propagation delay from input change or clock edge (whichever is later)
master-slave flip-flop	clock hi-to-lo transition ( $T_{su}/T_h$ around falling edge of clock)	propagation delay from falling edge of clock
negative edge-triggered flip-flop	clock hi-to-lo transition ( $T_{su}/T_h$ around falling edge of clock)	propagation delay from falling edge of clock

## Typical timing specifications

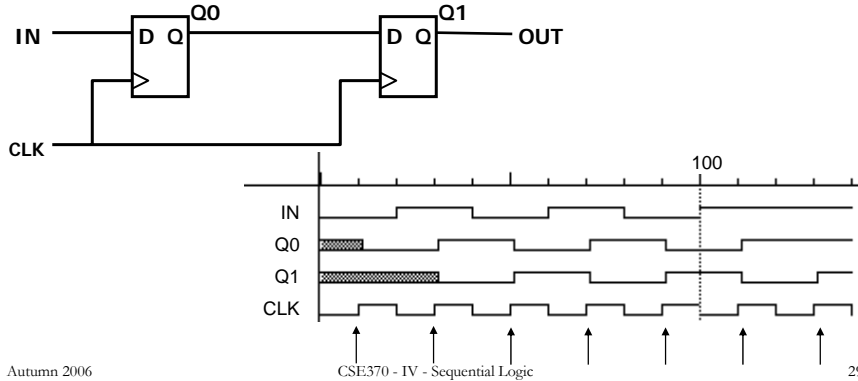
- Positive edge-triggered D flip-flop
  - setup and hold times
  - minimum clock width
  - propagation delays (low to high, high to low, max and typical)



all measurements are made from the clocking event (the rising edge of the clock)

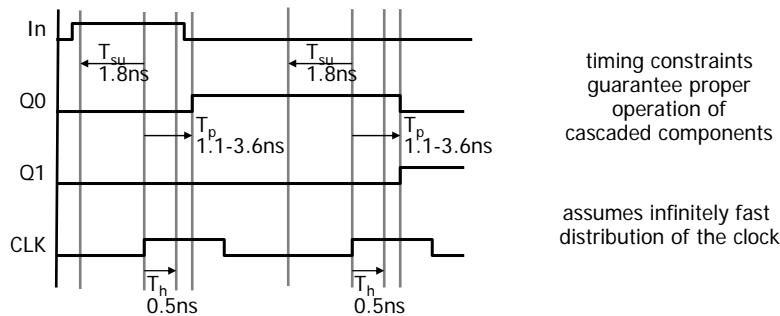
## Cascading edge-triggered flip-flops

- Shift register
  - new value goes into first stage
  - while previous value of first stage goes into second stage
  - consider setup/hold/propagation delays (prop must be > hold)



## Cascading edge-triggered flip-flops (cont'd)

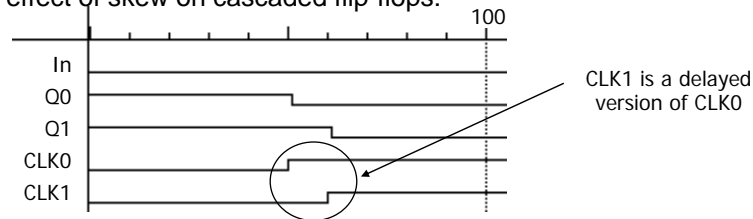
- Why this works
  - propagation delays exceed hold times
  - clock width constraint exceeds setup time
  - this guarantees following stage will latch current value before it changes to new value



## Clock skew

### ■ The problem

- correct behavior assumes next state of all storage elements determined by all storage elements at the same time
- this is difficult in high-performance systems because time for clock to arrive at flip-flop is comparable to delays through logic
- effect of skew on cascaded flip-flops:



## Summary of latches and flip-flops

### ■ Development of D-FF

- level-sensitive used in custom integrated circuits
  - can be made with 8 switches
- edge-triggered used in modern programmable logic devices
- good choice for data storage register

### ■ Historically J-K FF was popular but now never used

- similar to R-S but with 1-1 being used to toggle output (complement state)
- good in days of TTL/SSI (more complex input function:  $D = J Q' + K' Q$ )
- can always be implemented using D-FF

### ■ Preset and clear inputs are highly desirable on flip-flops

- used at start-up or to reset system to a known state

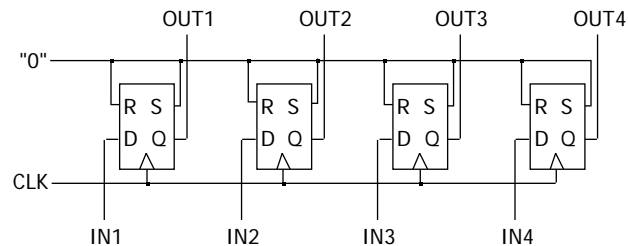


## Flip-flop features

- Reset (set state to 0) – R
  - synchronous:  $D_{new} = R' \cdot D_{old}$  (when next clock edge arrives)
  - asynchronous: doesn't wait for clock, quick but dangerous
- Preset or set (set state to 1) – S (or sometimes P)
  - synchronous:  $D_{new} = D_{old} + S$  (when next clock edge arrives)
  - asynchronous: doesn't wait for clock, quick but dangerous
- Both reset and preset
  - $D_{new} = R' \cdot D_{old} + S$  (set-dominant)
  - $D_{new} = R' \cdot D_{old} + R'S$  (reset-dominant)
- Selective input capability (input enable or load) – LD or EN
  - multiplexor at input:  $D_{new} = LD' \cdot Q + LD \cdot D_{old}$
  - load may or may not override reset/set (usually R/S have priority)
- Complementary outputs – Q and Q'

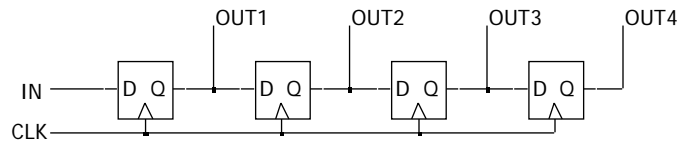
## Registers

- Collections of flip-flops with similar controls and logic
  - stored values somehow related (for example, form binary value)
  - share clock, reset, and set lines
  - similar logic at each stage
- Examples
  - shift registers
  - counters



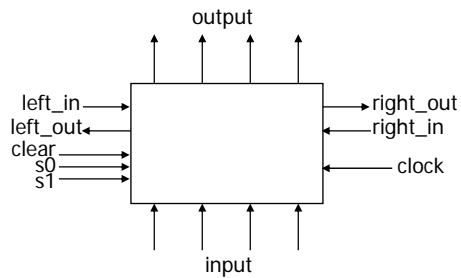
## Shift register

- Holds samples of input
  - store last 4 input values in sequence
  - 4-bit shift register:



## Universal shift register

- Holds 4 values
  - serial or parallel inputs
  - serial or parallel outputs
  - permits shift left or right
  - shift in new values from left or right



clear sets the register contents and output to 0

s1 and s0 determine the shift function

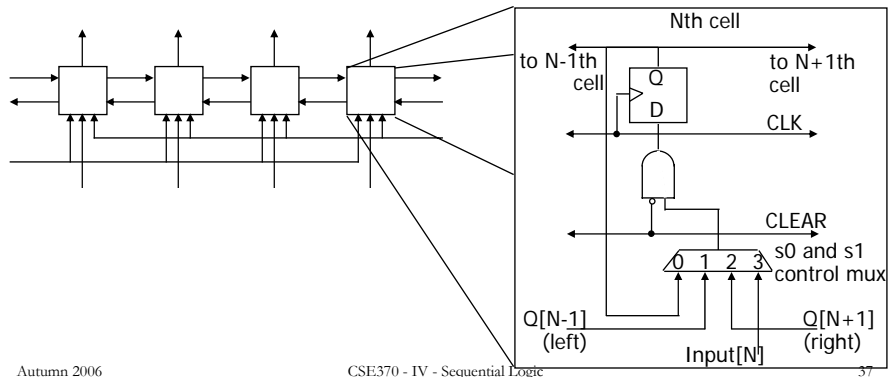
s0	s1	function
0	0	hold state
0	1	shift right
1	0	shift left
1	1	load new input

## Design of universal shift register

- Consider one of the four flip-flops

- new value at next clock cycle:

clear	s0	s1	new value
1	-	-	0
0	0	0	output
0	0	1	output value of FF to left (shift right)
0	1	0	output value of FF to right (shift left)
0	1	1	input



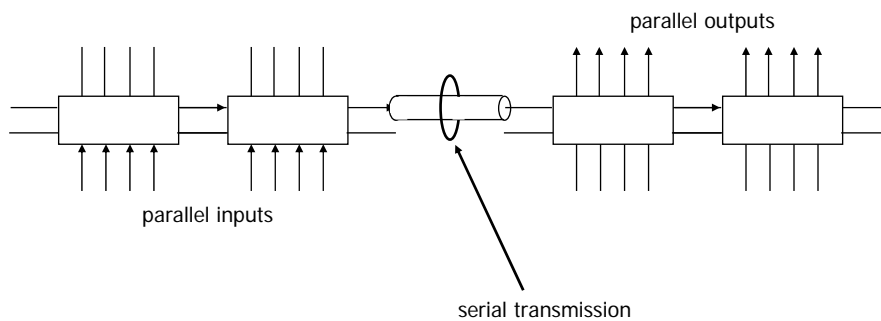
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37

## Shift register application

- Parallel-to-serial conversion for serial transmission



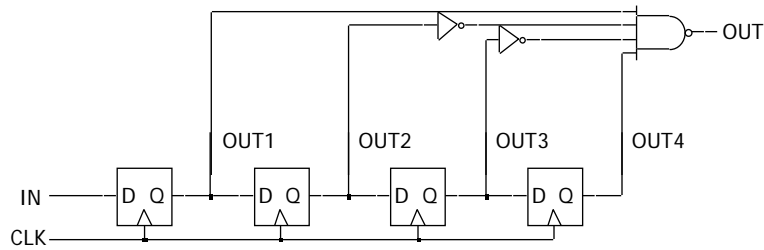
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38

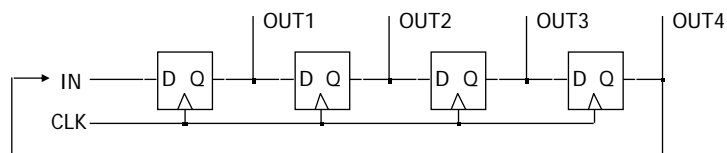
## Pattern recognizer

- Combinational function of input samples
  - in this case, recognizing the pattern 1001 on the single input signal



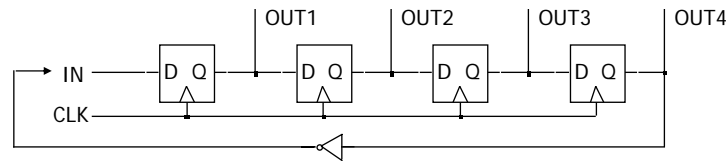
## Counters

- Sequences through a fixed set of patterns
  - in this case, 1000, 0100, 0010, 0001
  - if one of the patterns is its initial state (by loading or set/reset)



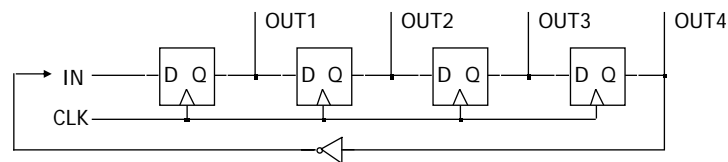
## Activity

- How does this counter work?



## Activity

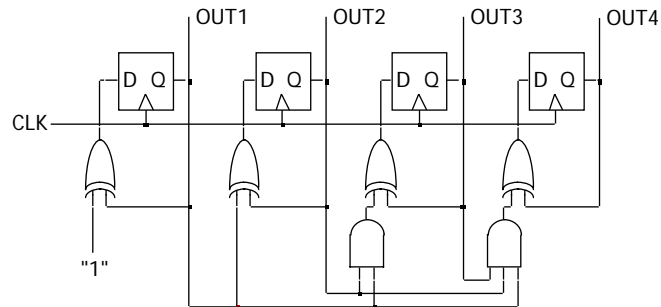
- How does this counter work?



- Counts through the sequence: 1000, 1100, 1110, 1111, 0111, 0011, 0001, 0000
- Known as Mobius (or Johnson) counter

## Binary counter

- Logic between registers (not just multiplexer)
  - XOR decides when bit should be toggled
  - always for low-order bit, only when first bit is true for second bit, and so on



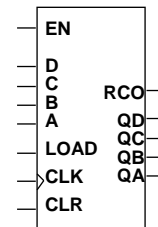
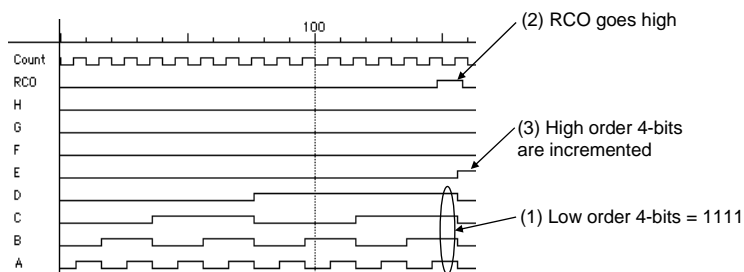
Autumn 2006

CSE370 - IV - Sequential Logic

43

## Four-bit binary synchronous up-counter

- Standard component with many applications
  - positive edge-triggered FFs w/ synchronous load and clear inputs
  - parallel load data from D, C, B, A
  - enable inputs: must be asserted to enable counting
  - RCO: ripple-carry out used for cascading counters
    - high when counter is in its highest state 1111
    - implemented using an AND gate



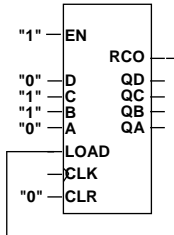
Sequential Logic

44

## Offset counters

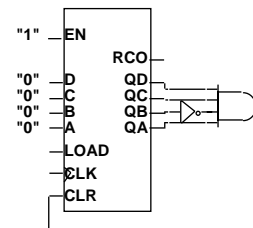
- Starting offset counters – use of synchronous load

- e.g., 0110, 0111, 1000, 1001, 1010, 1011, 1100, 1101, 1111, 0110, . . .



- Ending offset counter – comparator for ending value

- e.g., 0000, 0001, 0010, ..., 1100, 1101, 0000



- Combinations of the above (start and stop value)

## Hardware Description Languages and Sequential Logic

- Flip-flops
  - representation of clocks - timing of state changes
  - asynchronous vs. synchronous
- Shift registers
- Simple counters

## Flip-flop in Verilog

- Use always block's sensitivity list to wait for clock edge

```
module dff (clk, d, q);  
  
    input  clk, d;  
    output q;  
    reg   q;  
  
    always @(posedge clk)  
        q = d;  
  
endmodule
```

## More Flip-flops

- Synchronous/asynchronous reset/set
  - single thread that waits for the clock
  - three parallel threads – only one of which waits for the clock

### Synchronous

```
module dff (clk, s, r, d, q);  
    input clk, s, r, d;  
    output q;  
    reg   q;  
  
    always @(posedge clk)  
        if (r)    q = 1'b0;  
        else if (s) q = 1'b1;  
        else      q = d;  
  
endmodule
```

### Asynchronous

```
module dff (clk, s, r, d, q);  
    input clk, s, r, d;  
    output q;  
    reg   q;  
  
    always @(posedge r)  
        q = 1'b0;  
    always @(posedge s)  
        q = 1'b1;  
    always @(posedge clk)  
        q = d;  
  
endmodule
```



## Incorrect Flip-flop in Verilog

- Use always block's sensitivity list to wait for clock to change

```
module dff (clk, d, q);  
    input  clk, d;  
    output q;  
    reg    q;  
  
    always @(clk)  
        q = d;  
  
endmodule
```

Not correct! Q will change whenever the clock changes, not just on an edge.

## Blocking and Non-Blocking Assignments

- Blocking assignments ( $X=A$ )
  - completes the assignment before continuing on to next statement
- Non-blocking assignments ( $X<=A$ )
  - completes in zero time and doesn't change the value of the target until a blocking point (delay/wait) is encountered
- Example: swap

```
always @(posedge CLK)  
begin  
    temp = B;  
    B = A;  
    A = temp;  
end
```

```
always @(posedge CLK)  
begin  
    A <= B;  
    B <= A;  
end
```

## Register-transfer-level (RTL) Assignment

- Non-blocking assignment is also known as an RTL assignment
  - if used in an always block triggered by a clock edge
  - all flip-flops change together

```
// B,C,D all get the value of A
always @(posedge clk)
begin
    B = A;
    C = B;
    D = C;
end
```

```
// implements a shift register
always @(posedge clk)
begin
    B <= A;
    C <= B;
    D <= C;
end
```

## Shift register in Verilog

```
module shift_register (clk, in, out);

    input  clk;
    input  in;
    output [0:3] out;

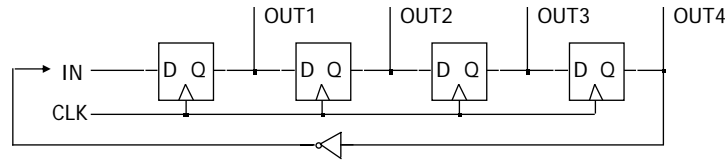
    reg [0:3] out;

    initial begin
        out = 0; // out[0:3] = {0, 0, 0, 0};
    end

    always @(posedge clk) begin
        out = {in, out [0:2]};
    end

endmodule
```

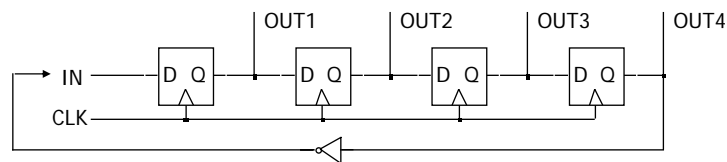
## Activity: express in Verilog



```
always @(posedge clk)
begin
```

```
end
```

## Mobius Counter in Verilog



```
initial
begin
  A = 1'b0;
  B = 1'b0;
  C = 1'b0;
  D = 1'b0;
end
```

```
always @(posedge clk)
begin
  A <= ~D;
  B <= A;
  C <= B;
  D <= C;
end
```

```
{A, B, C, D} <= {~D, A, B, C};
```

## Binary Counter in Verilog

```
module binary_counter (clk, c8, c4, c2, c1);  
  
    input  clk;  
    output c8, c4, c2, c1;  
  
    reg [3:0] count;  
  
    initial begin  
        count = 0;  
    end  
  
    always @(posedge clk) begin  
        count = count + 4'b0001;  
    end  
  
    assign c8 = count[3];  
    assign c4 = count[2];  
    assign c2 = count[1];  
    assign c1 = count[0];  
  
endmodule
```

```
module binary_counter (clk, c8, c4, c2, c1, rco);  
  
    input  clk;  
    output c8, c4, c2, c1, rco;  
  
    reg [3:0] count;  
    reg rco;  
  
    initial begin . . . end  
  
    always @(posedge clk) begin . . . end  
  
    assign c8 = count[3];  
    assign c4 = count[2];  
    assign c2 = count[1];  
    assign c1 = count[0];  
    assign rco = (count == 4b'1111);  
  
endmodule
```

## Sequential logic summary

- Fundamental building block of circuits with state
  - latch and flip-flop
  - R-S latch, R-S master/slave, D master/slave, edge-triggered D flip-flop
- Timing methodologies
  - use of clocks
  - cascaded FFs work because propagation delays exceed hold times
  - beware of clock skew
- Basic registers
  - shift registers
  - counters
- Hardware description languages and sequential logic