

CSE 370 Spring 2000
Solutions for Assignment 3
04/06/2000

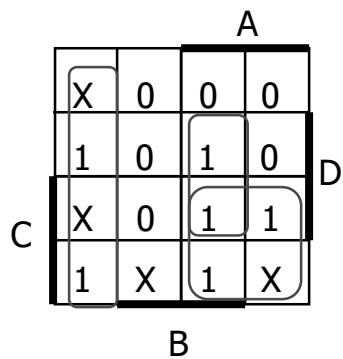
1.

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

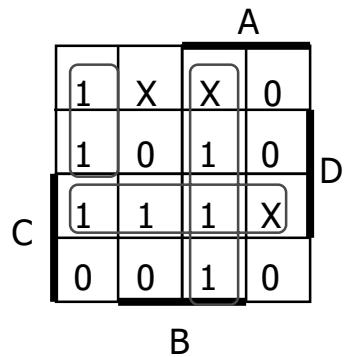
- a) $f = \Pi M(0, 1, 2, 5, 7, 10, 11, 14, 15)$
- b) $f = \Sigma m(3, 4, 6, 8, 9, 12, 13)$
- c) $f' = \Pi M(3, 4, 6, 8, 9, 12, 13)$
- d) $f' = \Sigma m(0, 1, 2, 5, 7, 10, 11, 14, 15)$

2.

a) $A'B' + AC + ABD$

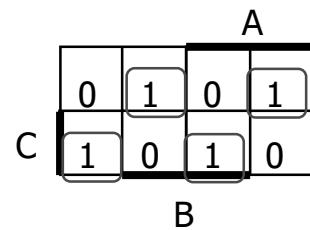


b) $AB + CD + A'B'C'$



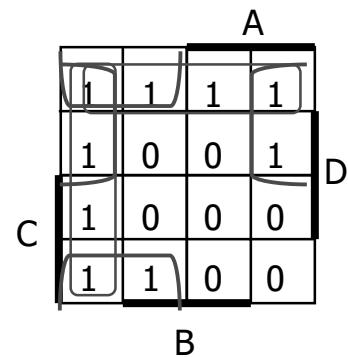
c) $AB'C' + ABC + A'BC' + A'B'C$

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1



3.

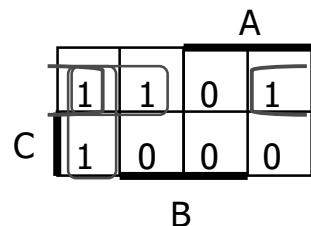
A	B	C	D	Adj
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0



$$\text{Adj} = \sum m_{(0, 1, 2, 3, 4, 6, 8, 9, 12)} \\ = C'D' + A'B' + B'C' + A'D'$$

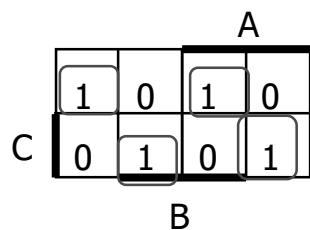
4.

A	B	C	Y1	Y0
0	0	0	1	1
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	0	0

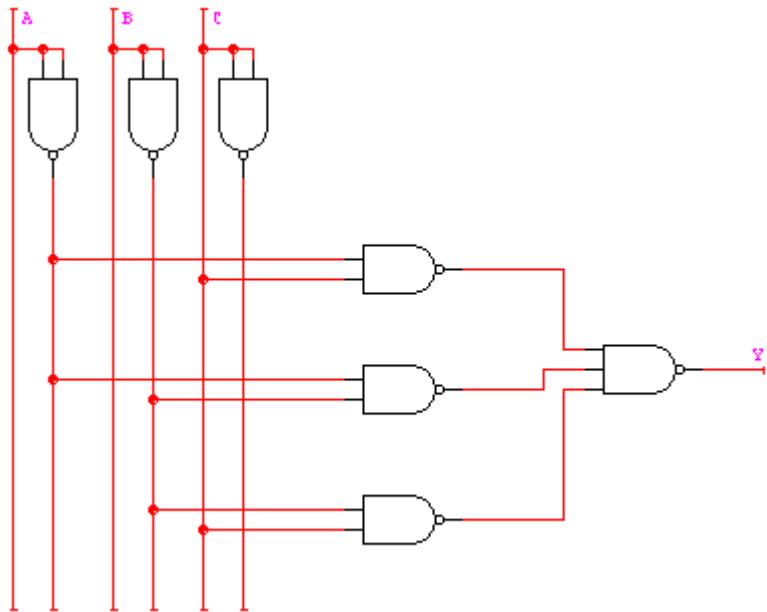


$$Y1 = A'C' + A'B' + B'C'$$

$$Y_0 = A'B'C' + A'BC + ABC' + AB'C$$

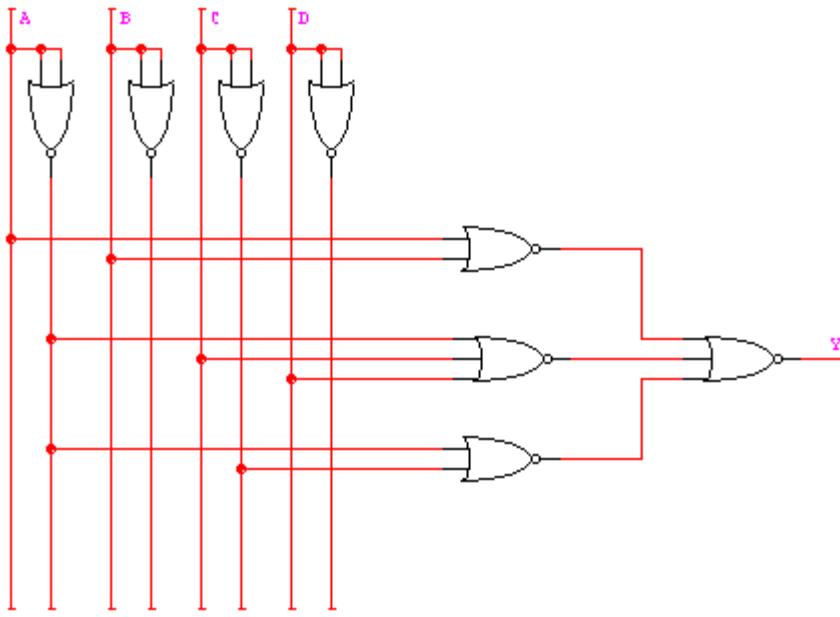


$$5. \quad Y = (AB)'(A'C')' = (A' + B')(A + C) = A'C + AB' + B'C$$



6.

$$Y = (A + B)(A' + C + d)(A' + C')$$



7.

a. $(B \oplus C)(A \oplus B)' + (A \oplus B)(B \oplus C)'$

b.

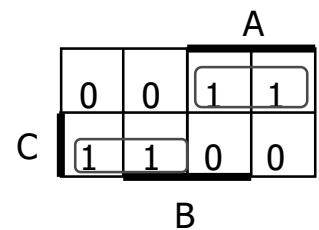
A	B	C	$A \oplus B$	$B \oplus C$	Y
0	0	0	0	0	0
0	0	1	0	1	1
0	1	0	1	1	0
0	1	1	1	0	1
1	0	0	1	0	1
1	0	1	1	1	0
1	1	0	0	1	1
1	1	1	0	0	0

c. $Y = \sum m_{(1, 3, 4, 6)}$

d.

$$\begin{aligned}
 & (B \oplus C)(A \oplus B)' + (A \oplus B)(B \oplus C)' \\
 &= (BC' + B'C)(AB' + A'B)' + (AB' + A'B)(BC' + B'C)' && \text{By definition of xor} \\
 &= (BC' + B'C)(A' + B)(A + B') + (AB' + A'B)(B' + C)(B + C') && \text{De Morgans law} \\
 &= (BC' + B'C)(A'B' + AB) + (AB' + A'B)(B'C' + BC) && \text{Distributive law and Theorem of complementarity} \\
 &= ABC' + A'B'C + AB'C' + A'BC && \text{Distributive law and Theorem of complementarity} \\
 &= AC'(B + B') + A'C(B + B') && \text{Distributive law} \\
 &= AC' + A'C && \text{Theorem of complementarity}
 \end{aligned}$$

e. $Y = AC' + A'C$



f. $Y' = A'C' + AC$

