Intro to Digital Design
Finite State Machines

Instructor: Justin Hsia

Teaching Assistants:

Emilio Alcantara
Eujean Lee
Naoto Uemura
Pedro Amarante
Wen Li

Relevant Course Information

- Quiz 1 grades should be out on Gradescope tonight
  - Both the quiz and solutions will be added to the question bank on the course website

- Lab 5 – Verilog implementation of FSMs
  - Step up in difficulty from Labs 1-4 (worth 100 points)
  - Bonus points for minimal logic
    - Simplification through *design* (Verilog does the rest)

Review of Timing Terms

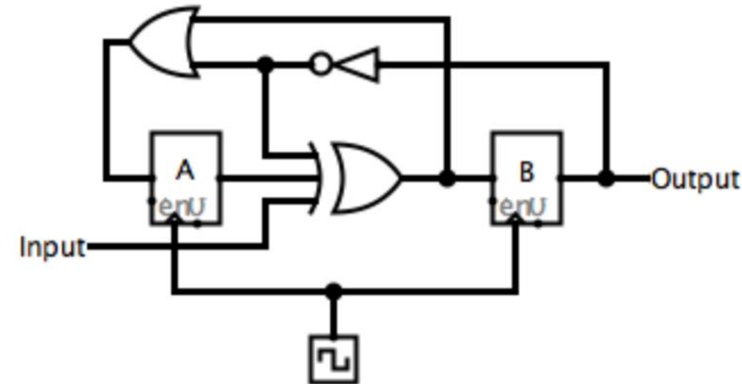
- Clock: steady square wave that synchronizes system

- Flip-flop: one bit of state that samples every rising edge of CLK (positive edge-triggered)
- Register: several bits of state that samples on rising edge of CLK (positive edge-triggered); often has a RESET

- Setup Time: when input must be stable *before* CLK trigger
- Hold Time: when input must be stable *after* CLK trigger
- CLK-to-Q Delay: how long it takes output to change from CLK trigger

SDS Timing Question (all times in ns)

- The circuit below has the following timing parameters
  - $t_{\text{period}} = 20, t_{\text{setup}} = 2$
  - $t_{\text{XOR}} = t_{\text{OR}} = 5, t_{\text{NOT}} = 4$
  - Input changes 1 ns after clock trigger



- What is the max t_{C2Q}?

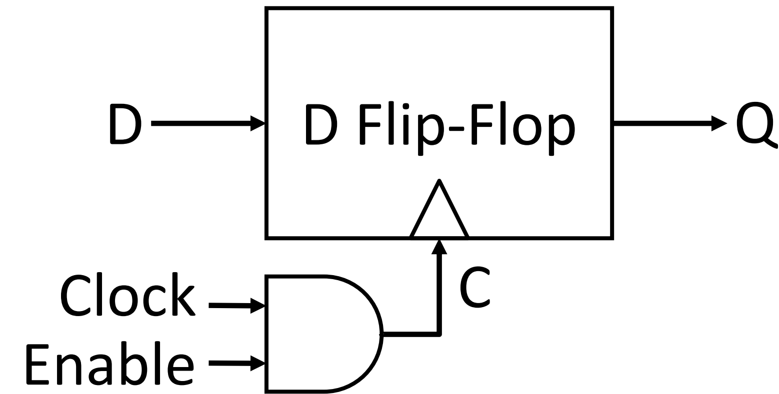
- If $t_{\text{C2Q}} = 3$, what is the max t_{hold}?

Outline

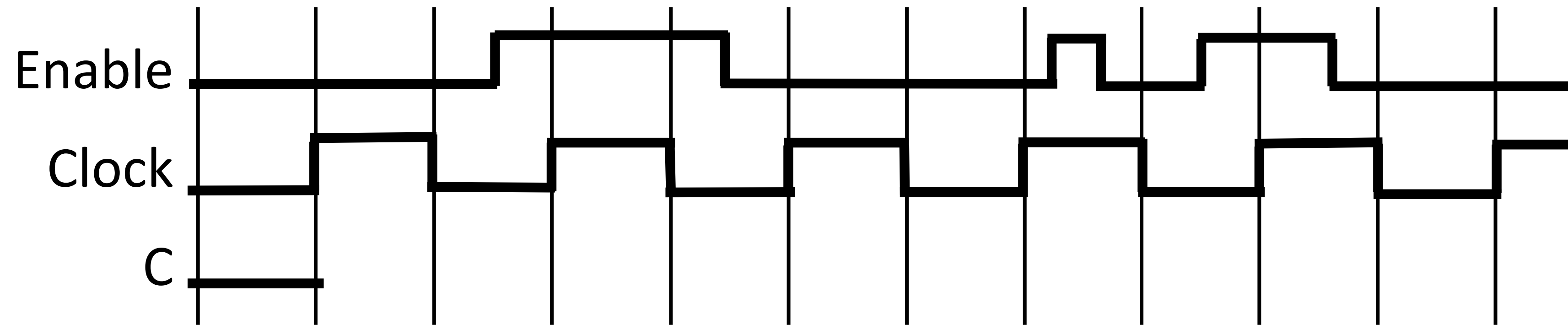
- **Flip-Flop Realities**
- Finite State Machines
- FSMs in Verilog

Flip-Flop Realities: Gating the Clock

- Delay can cause part of circuit to get out of sync with rest
  - More timing headaches!
  - Adds to *clock skew*



- Hard to track non-uniform triggers

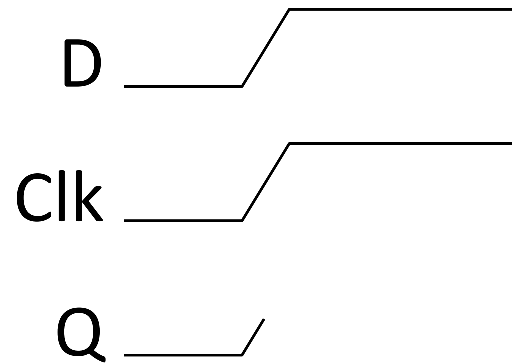


- **NEVER GATE THE CLOCK!!!**

Flip-Flop Realities: External Inputs

- External inputs aren’t synchronized to the clock
  - If not careful, can violate timing constraints

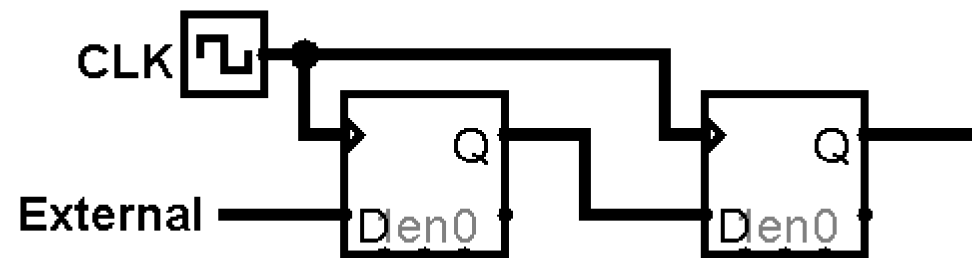
- What happens if input changes around clock trigger?



Flip-Flop Realities: Metastability

- **Metastability** is the ability of a digital system to persist for an unbounded time in an unstable equilibrium or metastable state
  - Circuit may be unable to settle into a stable '0' or '1' logic level within the time required for proper circuit operation
  - Unpredictable behavior or random value
  - https://en.wikipedia.org/wiki/Metastability_in_electronics

- State elements can help reject transients
  - Longer chains = more rejection, but longer signal delay

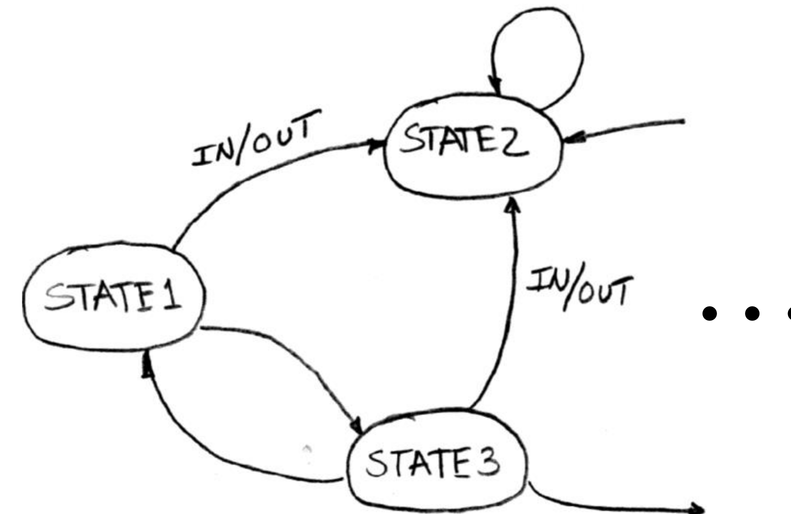


Outline

- Flip-Flop Realities
- **Finite State Machines**
- FSMs in Verilog

Finite State Machines (FSMs)

- A convenient way to conceptualize computation over time
  - Function can be represented with a *state transition diagram*
  - You've seen these before in CSE311
- **New for CSE369:** Implement FSMs in hardware as synchronous digital systems
  - Flip-flops/registers hold "state"
  - Controller (state update, I/O) implemented in combinational logic



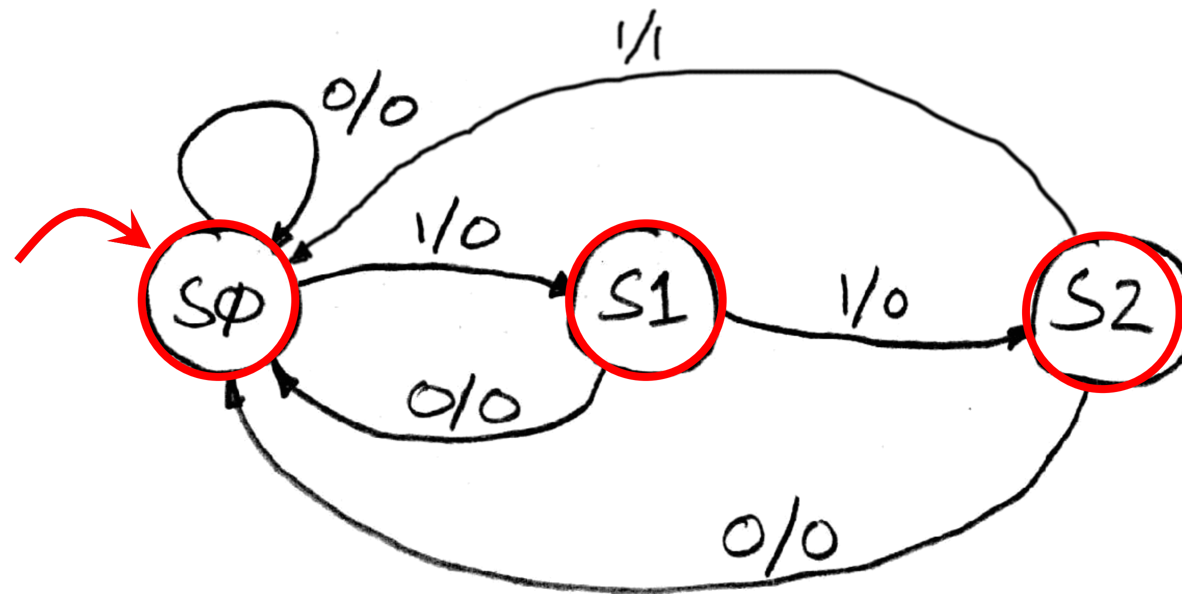
State Diagrams

- An state diagram (in this class) is defined by:
  - A set of *states* S (circles)
  - An *initial state* s_0 (only arrow not between states)
  - A *transition function* that maps from the current input and current state to the output and the next state (arrows between states)
    - **Note:** We cover Mealy machines here; Moore machines put outputs on states, not transitions

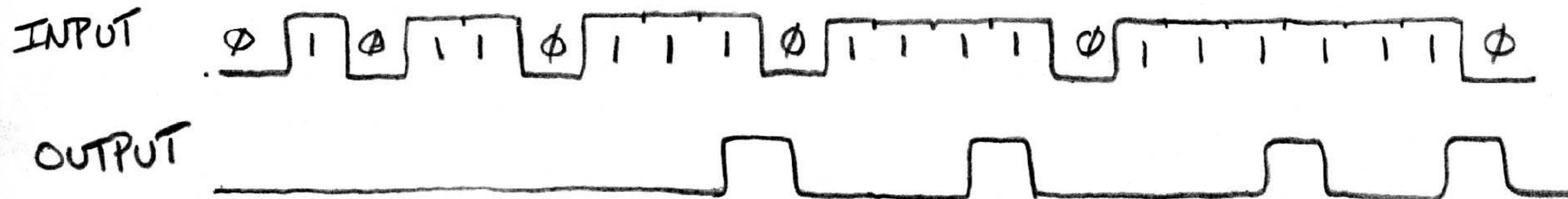
- State transitions are controlled by the clock:
  - On each clock cycle the machine checks the inputs and generates a new state (could be same) and new output

Example: Buggy 3 Ones FSM

- FSM to detect 3 consecutive 1's in the Input



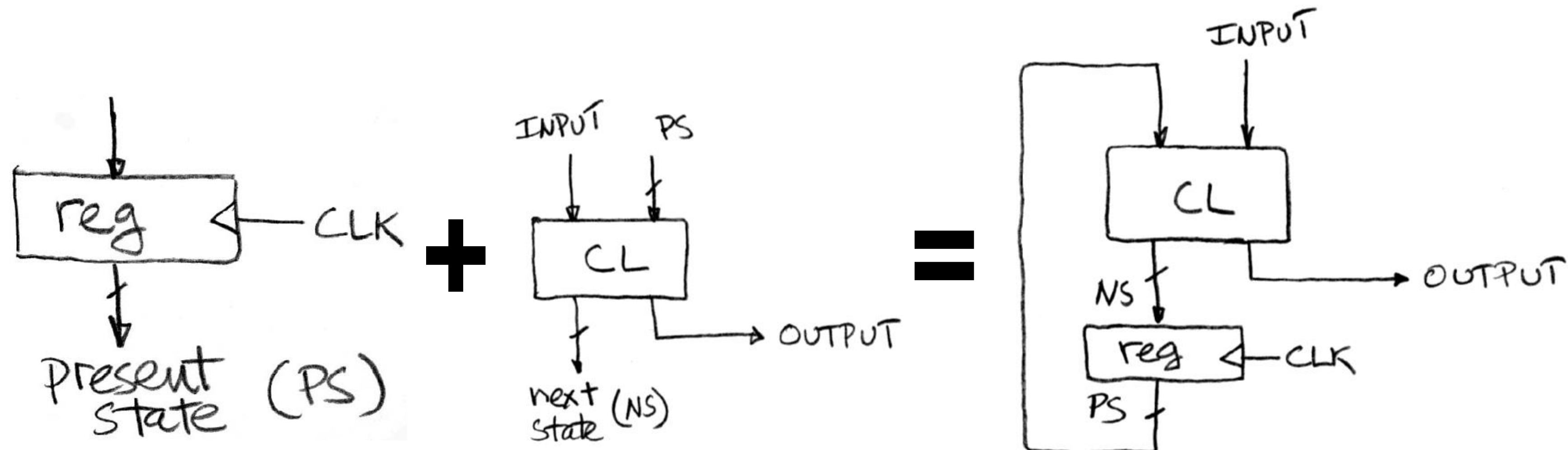
States: S0, S1, S2
Initial State: S0
Transitions of form:
input/output



Hardware Implementation of FSM

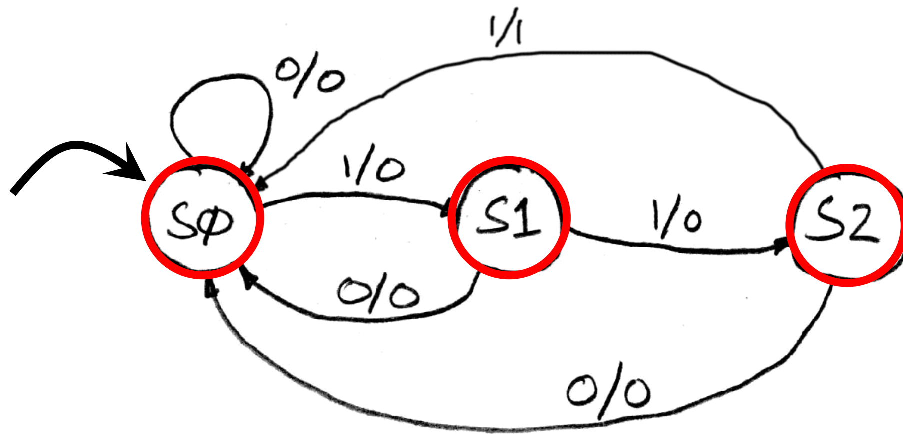
- Register holds a representation of the FSM's state
  - Must assign a *unique* bit pattern for each state
  - Output is *present/current state* (PS/CS)
  - Input is *next state* (NS)

- Combinational Logic implements transition function (state transitions + output)



FSM: Combinational Logic

- Read off transitions into Truth Table!
  - **Inputs:** Present State (PS) and Input (In)
  - **Outputs:** Next State (NS) and Output (Out)

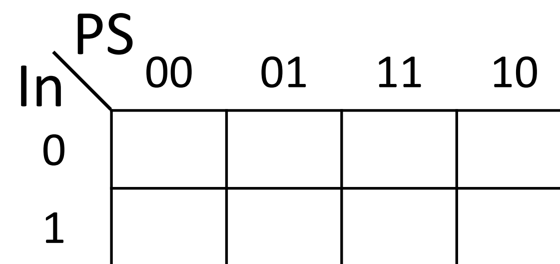


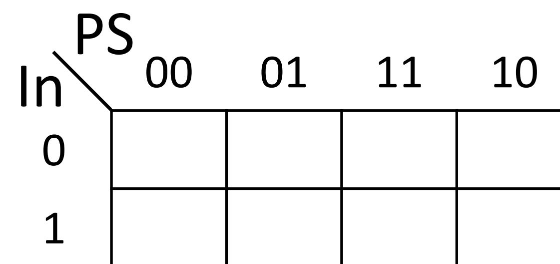
PS	In	NS	Out
00	0	00	0
00	1	01	0
01	0	00	0
01	1	10	0
10	0	00	0
10	1	00	1

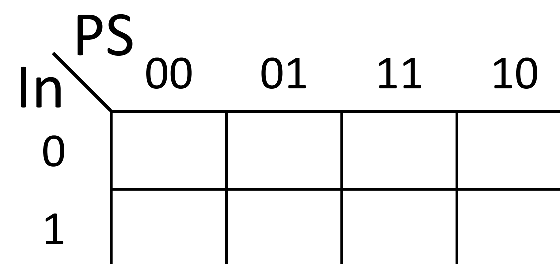
- Implement logic for *EACH* output (2 for NS, 1 for Out)

FSM: Logic Simplification

PS	In	NS	Out
00	0	00	0
00	1	01	0
01	0	00	0
01	1	10	0
10	0	00	0
10	1	00	1
11	0	XX	X
11	1	XX	X







FSM: Implementation

- $NS_1 = PS_0 \cdot In$
- $NS_0 = \overline{PS_1} \cdot \overline{PS_0} \cdot In$
- $Out = PS_1 \cdot In$

- How do we test the FSM?
  - “Take” every *transition* that we care about!

State Diagram Properties

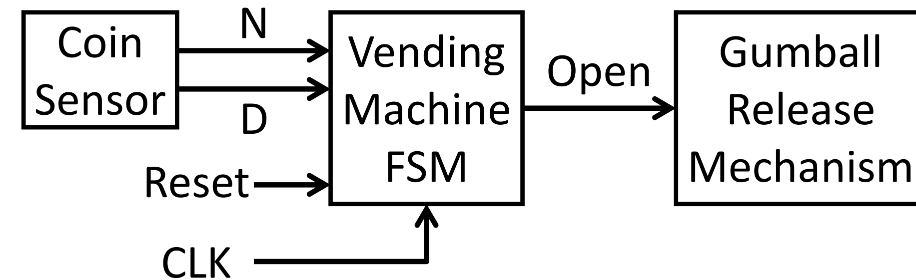
- For S states, how many state bits do I use?

- For I inputs, what is the *maximum* number of transition arrows on the state diagram?

  - Can sometimes combine transition arrows
  - Can sometimes omit transitions (don't cares)
- For s state bits and I inputs, how big is the truth table?

Vending Machine Example

- Vending machine description/behavior:
  - Single coin slot for dimes and nickels
  - Releases gumball after ≥ 10 cents deposited
  - Gives no change



- **State Diagram:**

Vending Machine State Table

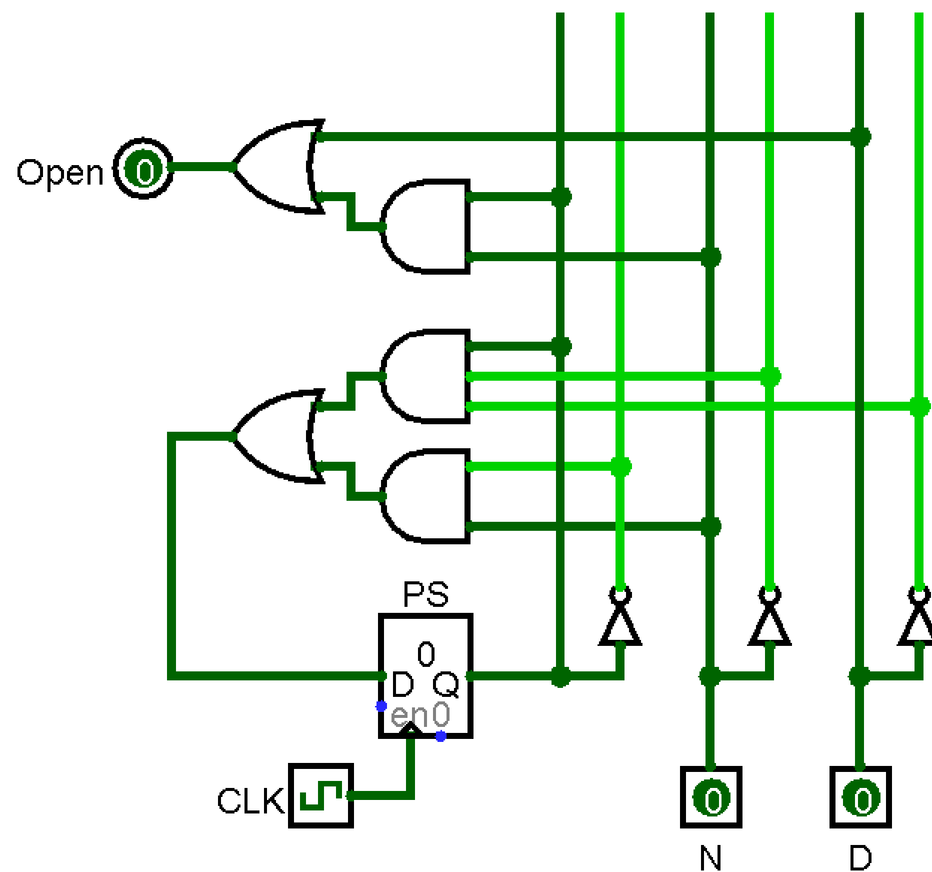
PS	N	D	NS	Open
0	0	0		
0	0	1		
0	1	0		
0	1	1		
1	0	0		
1	0	1		
1	1	0		
1	1	1		

D \ PS,N	00	01	11	10
0				
1				

D \ PS,N	00	01	11	10
0				
1				

Vending Machine Implementation

- $\text{Open} = \text{D} + \text{PS} \cdot \text{N}$
- $\text{NS} = \overline{\text{PS}} \cdot \text{N} + \text{PS} \cdot \overline{\text{N}} \cdot \overline{\text{D}}$

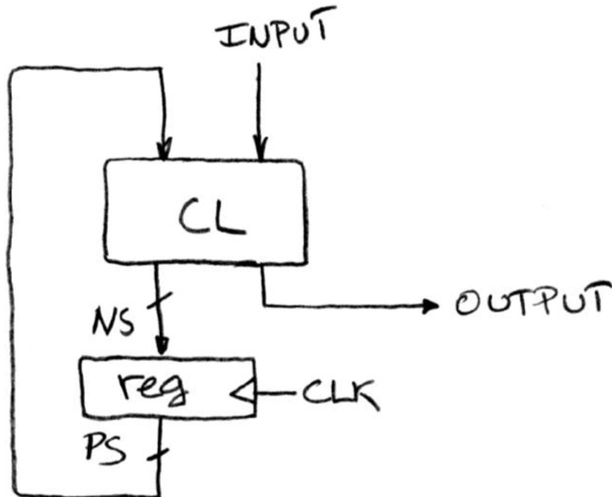


Outline

- Flip-Flop Realities
- Finite State Machines
- **FSMs in Verilog**

FSMs in Verilog: Overview

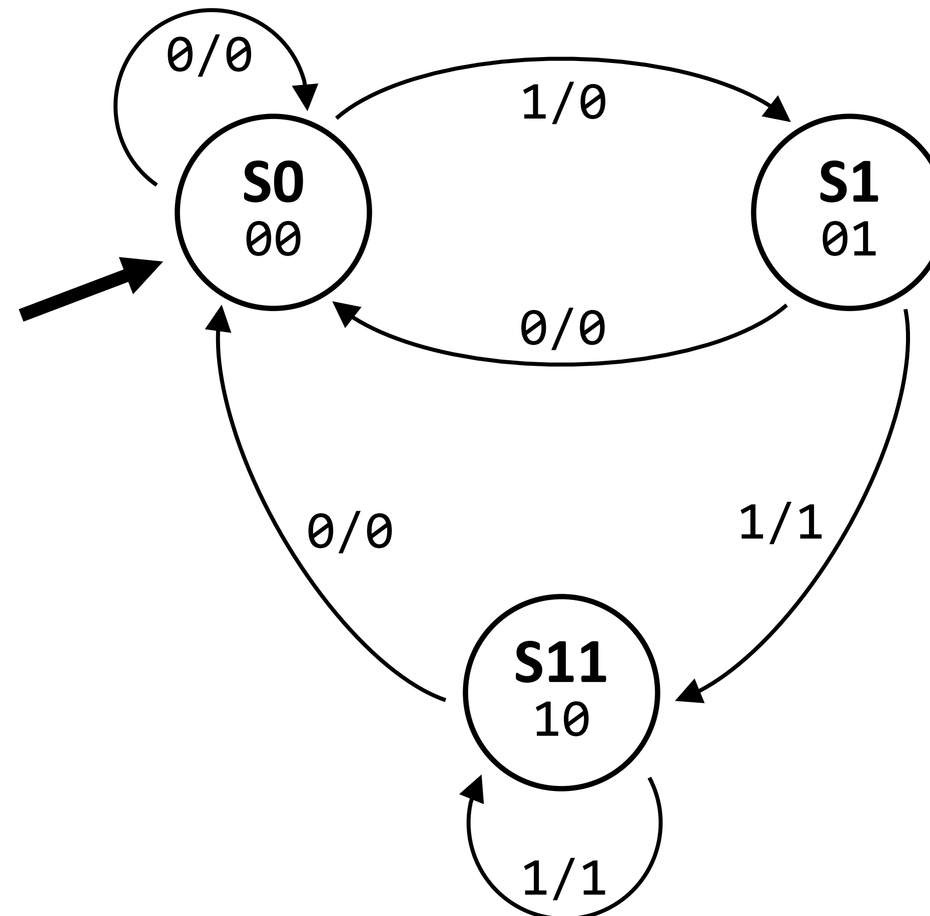
- FSMs follow a very particular organizational structure:



- They can be implemented using the following design pattern:
  1) Define states and state variables
  2) Next state logic (ns)
  3) Output logic
  4) State update logic (ps)

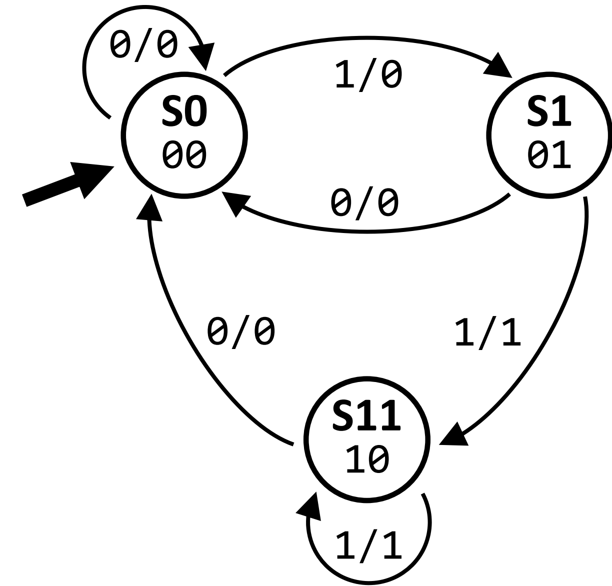
FSMs in Verilog: Example

- Arbitrary 3-state FSM that outputs 1 when two consecutive 1's are seen on the input
  - 2-bit state `ps`
  - `clk` and `reset` inputs
  - 1-bit input `w`
  - 1-bit output `out`



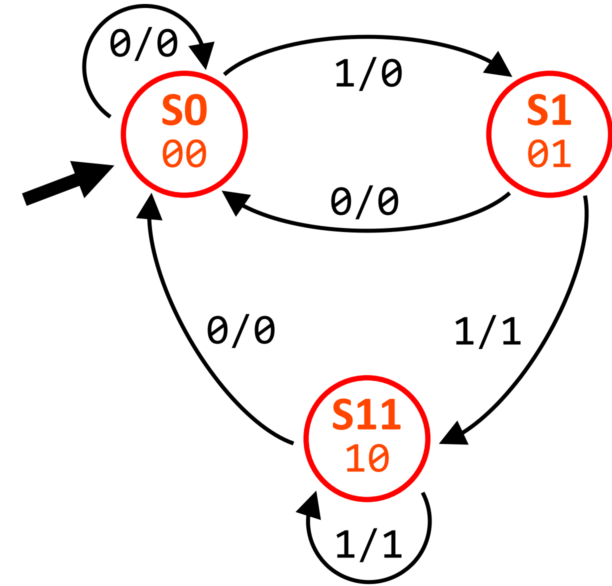
FSMs in Verilog: (0) Module Outline

```
module simpleFSM (clk, reset, w, out);
  input  logic clk, reset, w;
  output logic out;









endmodule  // simpleFSM
```



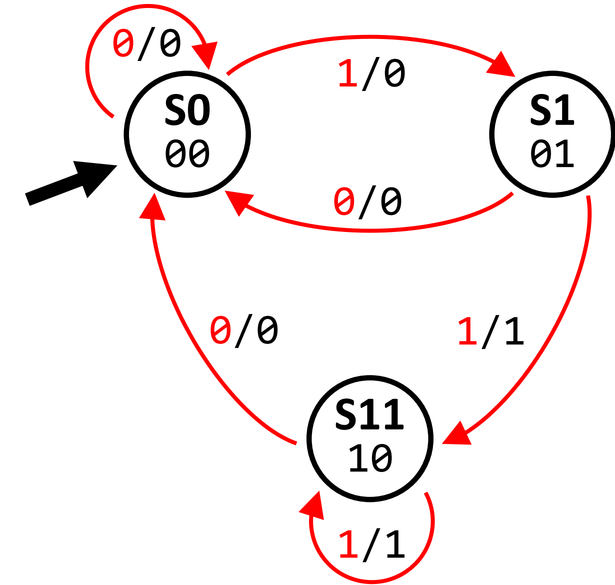
FSMs in Verilog: (1) State Declarations

```
module simpleFSM (clk, reset, w, out);
  input  logic clk, reset, w;
  output logic out;

  // State Encodings and variables
  // (ps = Present State, ns = Next State)
  enum logic [1:0] {S0=2'b00, S1=2'b01, S11=2'b10} ps, ns;









endmodule  // simpleFSM
```



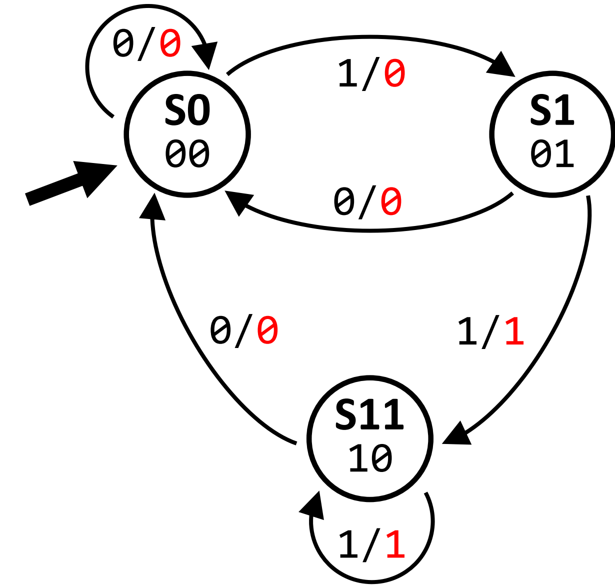
FSMs in Verilog: (2) Next State Logic

```
module simpleFSM (clk, reset, w, out);
  ...  // (0) port declarations
  ...  // (1) state encodings and variables

  // Next State Logic (ns)
  always_comb
    case (ps)
      S0:  if (w)  ns = S1;
           else    ns = S0;
      S1:  if (w)  ns = S11;
           else    ns = S0;
      S11: if (w)  ns = S11;
           else    ns = S0;
    endcase

endmodule  // simpleFSM
```



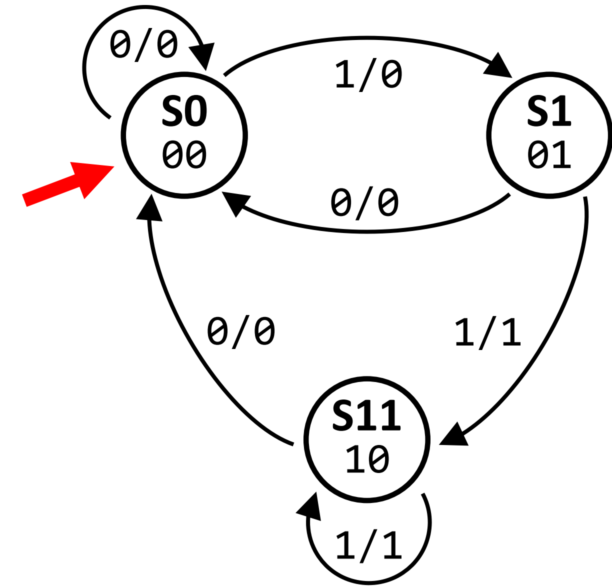
FSMs in Verilog: (2) Output Logic

```
module simpleFSM (clk, reset, w, out);
  ...  // (0) port declarations
  ...  // (1) state encodings and variables
  ...  // (2) Next State Logic (ns)

  // Output Logic - could have been in "always" block
  // or part of Next State Logic.
  assign out = (ns == S11);

endmodule  // simpleFSM
```



FSMs in Verilog: (2) Output Logic

```
module simpleFSM (clk, reset, w, out);
  ...  // (0) port declarations
  ...  // (1) state encodings and variables
  ...  // (2) Next State Logic (ns)
  ...  // (3) Output Logic

  // State Update Logic (ps)
  always_ff @(posedge clk)
    if (reset)
      ps <= S0;
    else
      ps <= ns;



endmodule  // simpleFSM
```



Reminder: Blocking vs. Non-blocking

- NEVER mix in one `always` block!
- Each variable written in only one `always` block

Blocking (=) in CL:

```
// Output Logic
assign out = (ns == S11);

// Next State Logic (ns)
always_comb
  case (ps)
    S0:  if (w) ns = S1;
         else   ns = S0;
    S1:  if (w) ns = S11;
         else   ns = S0;
    S11: if (w) ns = S11;
         else   ns = S0;
  endcase
```

Non-blocking (<=) in SL:

```
// State Update Logic (ps)
always_ff @(posedge clk)
  if (reset)
    ps <= S0;
  else
    ps <= ns;
```

One or Two Blocks?

- We showed the state update in two separate blocks:
  - `always_comb` block that calculates the next state (`ns`)
  - `always_ff` block that defines the register (`ps` updates to last `ns` on clock trigger)

- Can this be done with a single block?
  - If so, which one: `always_comb` or `always_ff`

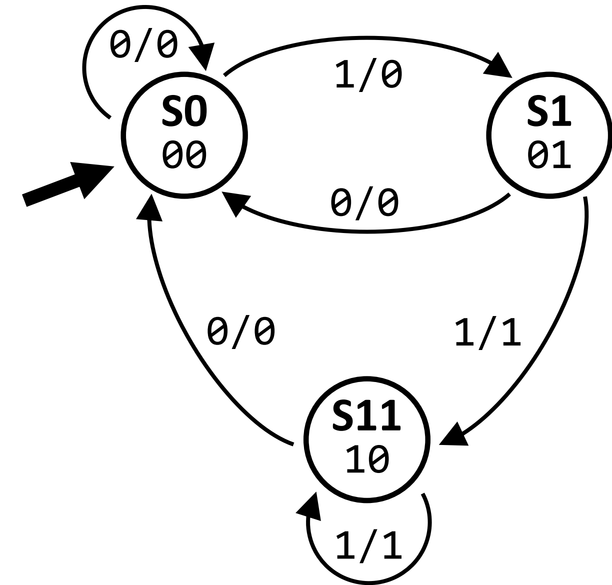
One or Two Blocks?

```
always_comb
  case (ps)
    S0:  if (w) ns = S1;
         else   ns = S0;
    S1:  if (w) ns = S11;
         else   ns = S0;
    S11: if (w) ns = S11;
         else   ns = S0;
  endcase

always_ff @(posedge clk)
  if (reset)
    ps <= S0;
  else
    ps <= ns;
```

```
always_ff @(posedge clk)
  if (reset)
    ps <= S0;
  else
    case (ps)
      S0:  if (w) ps <= S1;
           else   ps <= S0;
      S1:  if (w) ps <= S11;
           else   ps <= S0;
      S11: if (w) ps <= S11;
           else   ps <= S0;
    endcase
```

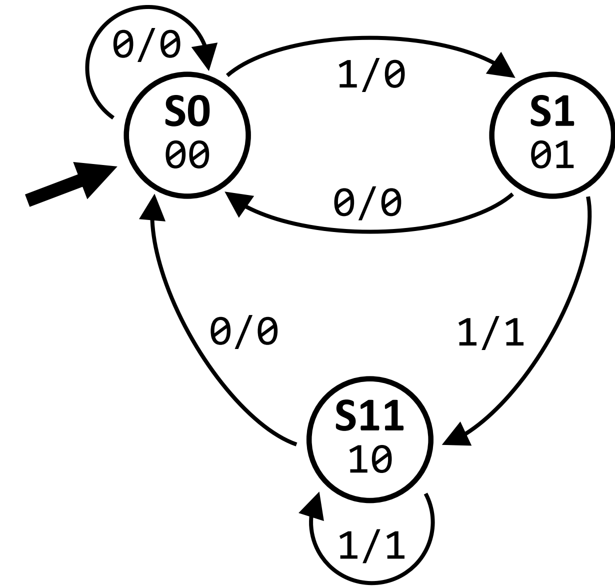
FSMs Test Bench (1/2)

```
module simpleFSM_tb ();
  logic clk, reset, w, out;

  // instantiate device under test
  simpleFSM dut (.clk, .reset, .w, .out);

  // generate simulated clock
  parameter CLOCK_PERIOD=100;
  initial begin
    clk <= 0;
    forever #(CLOCK_PERIOD/2) clk <= ~clk;
  end

  ... // generate test vectors

endmodule  // simpleFSM_tb
```

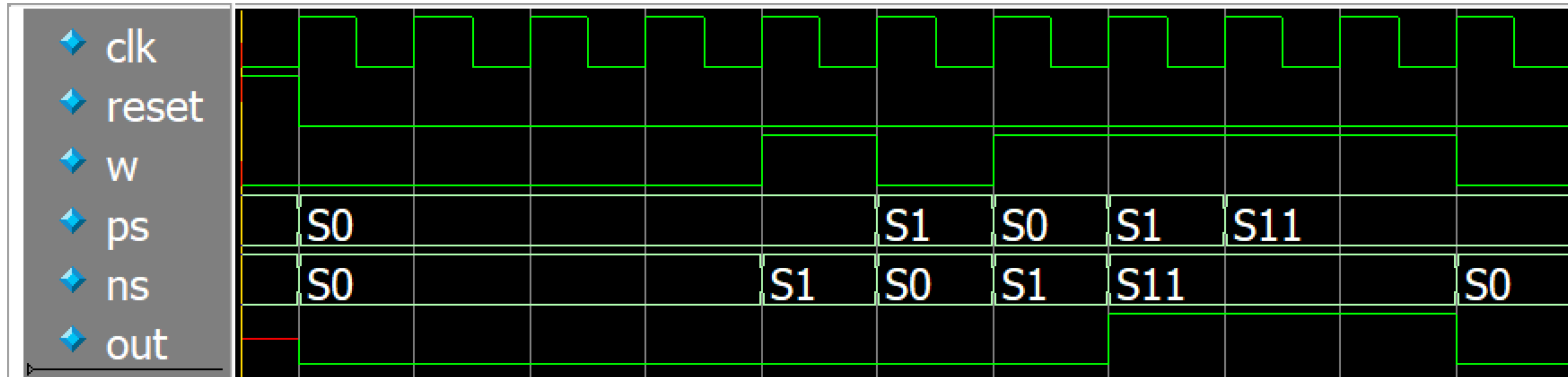


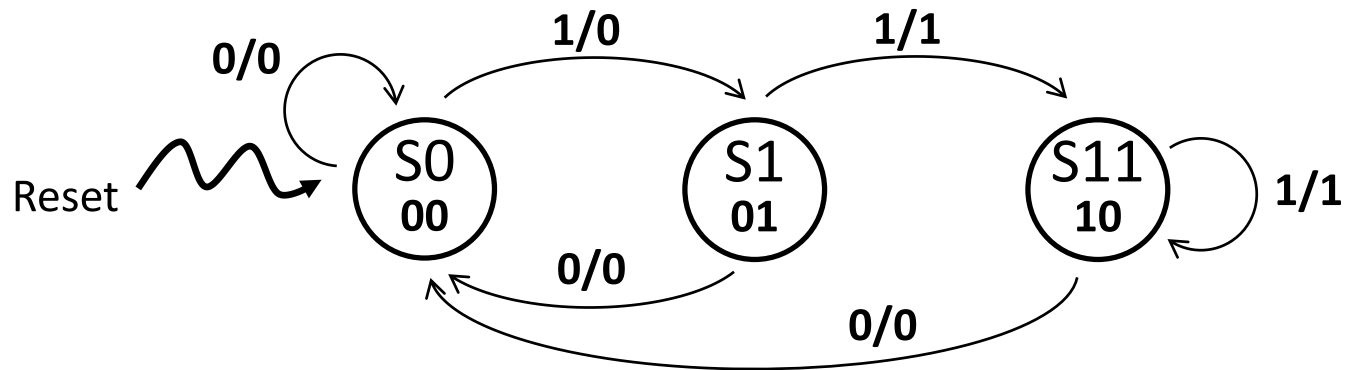
FSMs Test Bench (2/2)

```
  // generate test vectors
  initial begin
    reset <= 1; w <= 0; @(posedge clk);  // reset
    reset <= 0;         @(posedge clk);  // 4 cycles of 0 input
                        @(posedge clk);
                        @(posedge clk);
                        @(posedge clk);
                w <= 1; @(posedge clk);
                w <= 0; @(posedge clk);
                w <= 1; @(posedge clk);  // 4 cycles of 1 input
                        @(posedge clk);
                        @(posedge clk);
                        @(posedge clk);
                w <= 0; @(posedge clk);
                        @(posedge clk);  // extra cycle
    $stop;  // pause the simulation
  end
endmodule  // simpleFSM_tb
```



Testbench Waveforms





Summary

- Gating the clock and external inputs can cause timing issues and metastability
- FSMs visualize state-based computations
  - Implementations use registers for the state (PS) and combinational logic to compute the next state and output(s)
  - Mealy machines have outputs based on *state transitions*
- FSMs in Verilog usually have separate blocks for state updates and CL
  - Blocking assignments in CL, non-blocking assignments in SL
  - Testbenches need to be carefully designed to test all state transitions