

# CSE351 Spring 2014 – Midterm Exam (5 May 2014)

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Please read through the entire examination first! We designed this exam so that it can be completed in 50 minutes and, hopefully, this estimate will prove to be reasonable.

There are 5 problems for a total of 90 points. The point value of each problem is indicated in the table below. Write your answer neatly in the spaces provided. If you need more space (you shouldn't), you can write on the back of the sheet where the question is posed, but please make sure that you indicate clearly the problem to which the comments apply. Do NOT use any other paper to hand in your answers. If you have difficulty with part of a problem, move on to the next one. They are independent of each other.

The exam is CLOSED book and CLOSED notes (no summary sheets, no calculators, no mobile phones, no laptops). Please do not ask or provide anything to anyone else in the class during the exam. Make sure to ask clarification questions early so that both you and the others may benefit as much as possible from the answers.

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Name: \_\_\_\_\_

ID#: \_\_\_\_\_

Problem	Max Score	Score
1	15	
2	10	
3	20	
4	30	
5	15	
<b>TOTAL</b>	<b>90</b>	

## 1. Warm-up (15 points)

- A. If we have six (6) bits in which to represent integers, what is largest unsigned number and what is largest 2s complement number we can represent (in decimal)?

Largest unsigned number: \_\_\_\_\_

Largest 2s complement number: \_\_\_\_\_

- B. If `%eax` stores  $x$  and `%ebx` stores  $y$ , what do the following lines of assembly compute? Note that the result is in `%eax`.

```
mov    %ebx, %ecx
add    %eax, %ebx
je     .L1
sub    %eax, %ecx
je     .L1
xor    %eax, %eax
jmp    .L2
L1:
mov    $1, %eax
L2:
...
```

## 2. Floating Point Representation (10 points)

Suppose we have 16-bit floating point numbers where 6 bits are assigned to the exponent and 9 bits to the fraction and 1 to the sign bit.

A. What is the bias for this float?

B. Given the decimal number 3.625, calculate the fraction (frac) and exponent (exp) that would appear in the floating point representation. (Note: you may leave your answer in decimal for the exponent.)

### 3. C and Assembly Code (20 points)

Given the C code for the function foo, determine which IA32 and x86-64 code snippet corresponds to a correct implementation of foo.

```
int foo (int x, int y) {  
    int c = x << (y + 3);  
    if (x != 0) {  
        return c;  
    } else {  
        return 1;  
    }  
}
```

A. Which of the following IA-32 implementations is correct for foo()? Circle the correct one and give at least one reason why the other two are not correct.

```
i)  push    %ebp
     mov     %esp, %ebp
     mov     0xc(%ebp), %ecx
     add     $0x3, %ecx
     mov     0x8(%ebp), %eax
     shl     %eax, %ecx
     mov     %ecx, %eax
     cmp     $0x8($ebp), $0
     jne     $0x808472 // two lines down to leave
     mov     $0x1, %eax
     leave
     ret
```

```
ii) push    %ebp
     mov     %esp, %ebp
     mov     0xc(%ebp), %ecx
     add     $0x3, %ecx
     mov     0x8(%ebp), %eax
     shl     %ecx, %eax
     cmp     $0x8(%ebp), $0
     jne     $0x808472 // two lines down to leave
     mov     $0x1, %eax
     leave
     ret
```

```
iii) push    $ebp
     mov     %esi, %ecx
     add     $0x3, %ecx
     mov     %edi, %eax
     shl     %ecx, %eax
     test    %edi, $0
     jne     $0x808472 // two lines down to leave
     mov     $0x1, %eax
     leave
     ret
```

B. Which of the following x86-64 implementations is correct for foo()? Circle the correct one and give at least one reason why the other two are not correct.

```
i)  add    $0x3, %rsi
     mov    %rdi, %rax
     shl   %rsi, %rax
     test  %rdi, %rdi
     jne   $0x808472 // two lines down to leave
     mov   $0x1, %rax
     leave
     ret
```

```
ii) push  $rbx
     mov   %rsi, %rbx
     add   $0x3, %rbx
     mov   %rdi, %rax
     shl   %rbx, %rax
     test  %rdi, %rdi
     jne   $0x808472 // two lines down to leave
     mov   $0x1, %rax
     leaveq
     ret
```

```
iii) mov   %rdi, %rdx
      add   $0x3, %rdx
      mov   %rsi, %rax
      shl   %rdx, %rax
      test  $0, %rdi
      jne   $0x808472 // two lines down to leave
      mov   $0x1, %rax
      ret
```

#### 4. Stack Discipline (30 points)

The following function recursively computes the greatest common divisor of the integers a, b:

```
int gcd(int a, int b) {
    if (b == 0) {
        return a;
    } else {
        return gcd(b, a % b);
    }
}
```

Here is the x86\_64 assembly for the same function:

```
4006c6 <gcd>:
4006c6:  sub     $0x18, %rsp
4006ca:  mov     %edi, 0x10(%rsp)
4006ce:  mov     %esi, 0x08(%rsp)
4006d2:  cmpl   $0x0, %esi
4006d7:  jne    4006df <gcd+0x19>
4006d9:  mov     0x10(%rsp), %eax
4006dd:  jmp    4006f5 <gcd+0x2f>
4006df:  mov     0x10(%rsp), %eax
4006e3:  cltd
4006e4:  idivl  0x08(%rsp)
4006e8:  mov     0x08(%rsp), %eax
4006ec:  mov     %edx, %esi
4006ee:  mov     %eax, %edi
4006f0:  callq  4006c6 <gcd>
4006f5:  add     $0x18, %rsp
4006f9:  retq
```

Note: **cltd** is an instruction that sign extends *%eax* into *%edx* to form the 64-bit signed value represented by the concatenation of [ *%edx* | *%eax* ].

Note: **idivl <mem>** is an instruction divides the 64-bit value [ *%edx* | *%eax* ] by the long stored at <mem>, storing the quotient in *%eax* and the remainder in *%edx*.

- A. Suppose we call `gcd(144, 64)` from another function (i.e. `main()`), and set a breakpoint just before the statement “return a”. When the program hits that breakpoint, what will the stack look like, starting at the top of the stack and going all the way down to the saved instruction address in `main()`? Label all return addresses as “ret addr”, label local variables, and leave all unused space blank.

Memory address on stack	Value (8 bytes per line)
0x7fffffffad0	Return address back to main
0x7fffffffac8	
0x7fffffffac0	
0x7fffffffab8	
0x7fffffffab0	
0x7fffffffaa8	
0x7fffffffaa0	
0x7fffffff998	
0x7fffffff990	
0x7fffffff888	
0x7fffffff800	
0x7fffffff780	
0x7fffffff700	

<-%rsp points here at start of procedure



B. How many total bytes of local stack space are created in each frame (in decimal)?

\_\_\_\_\_

C. When the function begins, where are the arguments (a, b) stored?

D. From a memory-usage perspective, why are iterative algorithms generally preferred over recursive algorithms?

**5. Structs (15 points)**

- A. Draw a picture of the following struct, specifying the byte offset of each of the struct's fields and the size of any areas of fragmentation. Assume a 64-bit architecture.

```
typedef struct blah {  
    char b;  
    int l;  
    char *a;  
    char h;  
} blahblahblah;
```

- B. How many bytes of internal fragmentation does the struct contain? External fragmentation?

Internal fragmentation: \_\_\_\_\_

External fragmentation: \_\_\_\_\_

C. Reorder the fields of the struct to minimize fragmentation:

```
typedef struct blah {  
    _____  
    _____  
    _____  
    _____  
} blahblahblah;
```

D. What is the size of the reordered struct?

\_\_\_\_\_

E. How many bytes of internal fragmentation does the struct contain? External?

Internal fragmentation: \_\_\_\_\_

External fragmentation: \_\_\_\_\_

## REFERENCES

### **Powers of 2:**

$2^0 = 1$	
$2^1 = 2$	$2^{-1} = .5$
$2^2 = 4$	$2^{-2} = .25$
$2^3 = 8$	$2^{-3} = .125$
$2^4 = 16$	$2^{-4} = .0625$
$2^5 = 32$	$2^{-5} = .03125$
$2^6 = 64$	$2^{-6} = .015625$
$2^7 = 128$	$2^{-7} = .0078125$
$2^8 = 256$	$2^{-8} = .00390625$
$2^9 = 512$	$2^{-9} = .001953125$
$2^{10} = 1024$	$2^{-10} = .0009765625$

### **Assembly Code Instructions:**

push	push a value onto the stack and decrement the stack pointer
pop	pop a value from the stack and increment the stack pointer
call	jump to a procedure after first pushing a return address onto the stack
ret	pop return address from stack and jump there
mov	move a value between registers and memory
lea	compute effective address and store in a register
add	add src (1 <sup>st</sup> operand) to dst (2 <sup>nd</sup> ) with result stored in dst (2 <sup>nd</sup> )
sub	subtract src (1 <sup>st</sup> operand) from dst (2 <sup>nd</sup> ) with result stored in dst (2 <sup>nd</sup> )
and	bit-wise AND of src and dst with result stored in dst
or	bit-wise OR of src and dst with result stored in dst
sar	shift data in the dst to the right (arithmetic shift) by the number of bits specified in 1 <sup>st</sup> operand
jmp	jump to address
jne	conditional jump to address if zero flag is not set
cmp	subtract src (1 <sup>st</sup> operand) from dst (2 <sup>nd</sup> ) and set flags
test	bit-wise AND src and dst and set flags

### Register map for x86-64:

Note: all registers are caller-saved except those explicitly marked as callee-saved, namely, `rbx`, `rbp`, `r12`, `r13`, `r14`, and `r15`. `rsp` is a special register.

<code>%rax</code>	Return value	<code>%r8</code>	Argument #5
<code>%rbx</code>	Callee saved	<code>%r9</code>	Argument #6
<code>%rcx</code>	Argument #4	<code>%r10</code>	Caller saved
<code>%rdx</code>	Argument #3	<code>%r11</code>	Caller Saved
<code>%rsi</code>	Argument #2	<code>%r12</code>	Callee saved
<code>%rdi</code>	Argument #1	<code>%r13</code>	Callee saved
<code>%rsp</code>	Stack pointer	<code>%r14</code>	Callee saved
<code>%rbp</code>	Callee saved	<code>%r15</code>	Callee saved