



## 1. Number Representation (30 points)

(15 pts) Part A: Integers

We are converting from an old 16-bit machine to a new 64-bit architecture. Here is a C function that given 64 bits representing four 16-bit signed integers (`old4ints`), extracts the integer requested (specified by `int_number` ranging from 0 for most significant – leftmost, to 3 for least significant - rightmost) and converts it to a 64-bit signed integer (the return value). **Remember**: shifts are logical for unsigned integers and arithmetic for signed integers.

```
int64_t extract (uint64_t old4ints, int64_t int_number) {
    int64_t newint;
    newint = old4ints >> ( int_number << 4 );
    return newint & 0xFFFF;
}
```

(5 pts) There is something terribly wrong with this function. Describe the error(s) in a couple of sentences.

*The amount of the shift is wrong. For 0<sup>th</sup> 16-bit int we should be shifting by 48, not 0.*

*Masking newint before the return clears its sign bit so that negative values are not properly translated.*

(10 pts) Write a correct version of the function.

*Rather than shifting by  $(3 - \text{int\_number}) \ll 4$ , we change the direction of the shift so that the 16-bits wanted end up in the high-order 16-bits rather than the low-order. We then do a constant arithmetic shift of 48 that also does sign extension properly.*

```
int64_t extract (uint64_t old4ints, int64_t int_number) {
    int64_t newint;
    newint = old4ints << ( int_number << 4 );
    return newint >> 48;
}
```

(15 pts) Part B: Floating point numbers

A new pizzeria has opened on the Ave. It is mysteriously called “Pizza 0x40490FDB”. Given that you have just completed CSE351, you have a hunch what the mystery might be. Consider the string of hex digits as a 32-bit IEEE floating point number (8-bit exponent and 23-bit fraction). Fill in the hexadecimal digits in the bytes below and then translate them to individual bits.

8 hex digits in 4 bytes: 4 0 4 9 0 F D B

32 bits: 0 1 0 0 0 0 0 0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 1 1 1 0 1 1 0 1 1

(2 pts) Is this number positive or negative (circle one)?  Positive  Negative

(4 pts) What is the exponent?  $(1000\ 0000)$   $128\text{-Bias} = 128 - 127 = 1$   
(*exponents are biased in this representation so make sure to make this adjustment*)

(4 pts) What is the significand?  $1.1001001 = 1 + .5 + .0625 + .0078125 = 1.5703125$   
(*only use the first 7 bits of the fraction, ignore the lower-order 16 bits*)

(4 pts) What is the decimal number represented?  $1.5703125 * 2^1 = 3.1406250$   
(*only show two decimal digits after the decimal point*)

(1 pt) What is the pizzeria’s mystery name? \_\_\_\_\_ Pizza Pi

## 2. Writing Assembly Code (35 points)

Below is a short C function that, given a pointer to a 4-character array consisting of only ASCII numbers (0 through 9 are represented in ASCII as 0x30 through 0x39), converts them to an integer representing a year A.D. (between 0 and 9999). It assumes the year is coded in big-endian order.

```
int charCodedYear2Integer (char *codedyr) {  
    int intyr = 0;  
  
    // get the first char and mask everything but the digit  
    // then multiply by 10 and add the second digit (after masking)  
    // then multiply by 10 and add the third digit (after masking)  
    // then multiply by 10 and add the fourth digit (after masking)  
  
    intyr =          (int) *codedyr          & 0x0F;  
    intyr = 10*intyr + ( (int) *(codedyr + 1) & 0x0F );  
    intyr = 10*intyr + ( (int) *(codedyr + 2) & 0x0F );  
    intyr = 10*intyr + ( (int) *(codedyr + 3) & 0x0F );  
  
    return intyr;  
}
```

Complete the IA32 assembly code corresponding to this C function using only:  
add, and, lea, and mov instructions or any of their variants.

Recall that %eax, %ecx, and %edx are caller-save registers.

The variable intyr corresponds to %eax as it is also the return value.

Use the following page to write your code.

Make sure to comment each line.

```
<charCodedYear2Integer>:  
    pushl    %ebp                Save old %ebp  
    movl    %esp,%ebp           Initialize new %ebp  
    movl    8(%ebp),%ecx         Get addr of first char  
    xorl    %eax,%eax           Clear %eax to use for intyr
```

<your assembly code (on next page) goes here>

```
    leave   Restore old %ebp  
    ret    Return
```

Write your assembly code here (should be no more than 25 lines or so):

*Hints: Start by moving the first character into a register. Multiply using additions (leal and/or add instructions) instead of multiply instructions.*

movzbl	0(%ecx), %edx	<i>Get first char</i>
andl	0x0F, %edx	<i>Mask</i>
addl	%edx, %eax	<i>Add to intyr</i>
leal	(%eax, %eax, 4), %eax	<i>intyr=5*intyr</i>
addl	%eax, %eax	<i>intyr=2*intyr</i>
movzbl	1(%ecx), %edx	<i>Get second char</i>
andl	0x0F, %edx	<i>Mask</i>
addl	%edx, %eax	<i>Add to intyr</i>
leal	(%eax, %eax, 4), %eax	<i>intyr=5*intyr</i>
addl	%eax, %eax	<i>intyr=2*intyr</i>
movzbl	2(%ecx), %edx	<i>Get third char</i>
andl	0x0F, %edx	<i>Mask</i>
addl	%edx, %eax	<i>Add to intyr</i>
leal	(%eax, %eax, 4), %eax	<i>intyr=5*intyr</i>
addl	%eax, %eax	<i>intyr=2*intyr</i>
movzbl	3(%ecx), %edx	<i>Get fourth char</i>
andl	0x0F, %edx	<i>Mask</i>
addl	%edx, %eax	<i>Add to intyr</i>

### 3. Stack and Procedures (35 points)

(18 pts) Part A: Return values

Consider a return value from a procedure that needs to be a struct rather than a simple value. A struct can't be placed in a register (such as `%rax` that is used to transfer return values). For each of the situations described below, provide at most a couple of sentences to explain your approach.

- (a) Consider the case when the struct is allocated statically in memory at compile time. The callee wants to return the struct which contains an arbitrary number of fields and doesn't fit in `%rax`. How could it return the struct?

*We can return a pointer to the struct in `%rax`. The caller procedure can then find the struct in memory at that address. It should make sure to use what it needs before calling the callee procedure again.*

- (b) Consider the case when the struct is allocated on the stack by the **caller** and a pointer to it is passed as an argument. Are there any different issues in that case?

*If the caller allocated memory for the struct on the stack, then the callee will have a pointer to it as an argument and can modify it as necessary. The caller will find the modified struct on the stack where it initially put it and use it as needed.*

- (c) Consider the case when the struct is created and allocated on the stack by the **callee**. Are there any different issues in that case?

*If the callee allocated memory for the struct on the stack, then we have to be very careful on returning it to the caller (as a pointer in `%rax` pointing to an address on the stack now beyond the caller's stack frame). The compiler needs to insert code to copy the struct to another more permanent location or use the needed values in the struct right away – before those same locations on the stack are used by another procedure.*

(17 pts) Part B: Stack frames

We have a three procedure program with functions `main`, `proc_a`, and `proc_b` compiled for x86-64. `main` calls `proc_a` or `proc_b` based on the values of some inputs and the two procedures can call each other. `proc_a` has 7 arguments, while `proc_b` has only 2 arguments. `proc_a` also has a register it must save on the stack (a callee-save register) before it calls any other procedures and restore before it itself returns and it also allocates one 64-bit int on the stack. Thus four types of values can end up on the stack: return address (RET ADDR), argument (ARG), allocated value (ALLOCATED), and callee-saved register (CALLEE).

Here are some tiny assembly code snippets:

```
0000000000405060 <main>:
```

```
...
405068:  call <proc_a>
40506d:  ...
...
```

```
0000000000405132 <proc_a>:
```

```
...
405155:  call <proc_b>
40515a:  ...
...
```

```
0000000000406354 <proc_b>:
```

```
...
40637c:  call <proc_a>
406381:  ...
...
```

(cont'd on next page)

Given the following stack contents, complete the Type column below by entering one of the four types of values the entry represents (RET ADDR, ARG, ALLOCATED, or CALLEE). Also complete the third column specifying which procedure placed the ALLOCATED value or CALLEE-saved register on the stack, or if an ARG, which procedure placed it on the stack for which other procedure, or if a RET ADDR, the name of the procedure that covers that address.

VALUES IN STACK MEMORY	TYPE	PROCEDURE USING VALUE OR CONTAINING ADDRESS
...		...
0000000000000001	ARG	<i>main for proc_a</i>
000000000040506d	RET ADDR	<i>main</i>
0000000000000002	CALLEE	<i>saved by proc_a</i>
0000000000000003	ALLOCATED	<i>allocated by proc_a</i>
000000000040515a	RET ADDR	<i>proc_a</i>
0000000000000004	ARG	<i>proc_b for proc_a</i>
0000000000406381	RET ADDR	<i>proc_b</i>
0000000000406380	CALLEE	<i>saved by proc_a</i>
0000000000000006	ALLOCATED	<i>allocated by proc_a</i> ← %rsp

## REFERENCES

### **Powers of 2:**

$2^0 = 1$	
$2^1 = 2$	$2^{-1} = .5$
$2^2 = 4$	$2^{-2} = .25$
$2^3 = 8$	$2^{-3} = .125$
$2^4 = 16$	$2^{-4} = .0625$
$2^5 = 32$	$2^{-5} = .03125$
$2^6 = 64$	$2^{-6} = .015625$
$2^7 = 128$	$2^{-7} = .0078125$
$2^8 = 256$	$2^{-8} = .00390625$
$2^9 = 512$	$2^{-9} = .001953125$
$2^{10} = 1024$	$2^{-10} = .0009765625$

### **Assembly Code Instructions:**

pushl	push a 32-bit value onto the stack
leave	restore ebp from the stack
ret	pop return address from stack and jump there
movl	move 4 bytes between immediate values, registers and memory
movzbl	move 1 byte into the low-order byte of a long word, filling the other 3 bytes with 0s.
movsbl	move 1 byte into the low-order byte of a long word, filling the other 3 bytes by sign-extending the low-order byte that was moved
addl	add 1 <sup>st</sup> operand to 2 <sup>nd</sup> with result stored in 2 <sup>nd</sup>
subl	subtract 1 <sup>st</sup> operand from 2 <sup>nd</sup> with result stored in 2 <sup>nd</sup>
andl	logical bitwise AND of 1 <sup>st</sup> operand with 2 <sup>nd</sup> with result stored in 2 <sup>nd</sup>
xorl	logical bitwise XOR of 1 <sup>st</sup> operand with 2 <sup>nd</sup> with result stored in 2 <sup>nd</sup>
jmp	jump to address
je	conditional jump to address if zero flag set
jne	conditional jump to address if zero flag is not set
cmpl	subtract 1 <sup>st</sup> operand from 2 <sup>nd</sup> and set flags
testl	logical bitwise AND of 1 <sup>st</sup> and 2 <sup>nd</sup> operands to set flags