

1. Number Representation (15 points)

The decimal value 11,184,810 is represented as a 32-bit signed binary with the bit pattern below (0x00aaaaaa):

0000 0000 1010 1010 1010 1010 1010 1010

When it is cast as a float, it is represented by the 32-bit floating point format (8-bits exp, 23-bit fraction) as (0x4b2aaaaa):

0100 1011 0010 1010 1010 1010 1010 1010

Explain why so many of the low-order bits are the same and why do the others differ. There is no need to convert these to decimal values.

*The exponent part of the float value is 1001 0110 which translates to $E = 150 - \text{bias} = 150 - 127 = 23$. Given that the value of the float is $1.\text{frac} * 2^{23}$, and the fractional part is 23 bits, the binary point moves 23 bits to the right. Therefore, we expect to see the same 23 low-order bits in the integer value with the next high-order bit being 1 (the implied 1. of the float representation). The remaining 8 high-order bits of the integer value are 0.*

2. Assembly Code (20 points)

A function 'flip' has the following overall structure:

```
int flip (*unsigned x) {
    int num=*x;
    int val=0;
    int i;
    for ( initialize ; test ; update ) {
        body
    }
    return val;
}
```

The GCC C compiler generates the following assembly code:

```
x at %ebp+8
1      movl  8(%ebp), %ebx      get x, a pointer to an unsigned int
2      movl  (%ebx), %esi      dereference x to get the unsigned int into num
3      movl  $0, %eax          initialize val to 0, stored in %eax
4      movl  $0, %ecx          initialize i to 0, stored in %ecx
5      .L13:
6      leal  (%eax, %eax), %edx double val, like shifting 1 left, put in %edx
7      movl  %esi, %eax        copy num to %eax
8      andl  $1, %eax          mask to get low-order bit of num
9      orl   %edx, %eax        OR the low-order bit with doubled val
10     shrl  %esi               shift num to right by 1
11     add   $1, %ecx           increment i
12     cmpl  $32, %ecx         test if reached 32
13     jne   .L13              jump to L13 (top of loop) if i < 32
14     ret                    return with val stored in %eax
```

Reverse engineer the operation of this code and then do the following:

A (15 pts). Use the assembly-code version to fill in the missing parts of the C code below. Also specify which lines above represent each of initialize, test, update, and body.

Initialize: 4

Test: 12, 13

Update: 11

Body: 6, 7, 8, 9, 10

```
int flip (*unsigned x) {
    int num=*x;
    int val=0;
    int i;
    for ( i=0 ; i<32 ; i++ ) {
        val = (val << 1) | (num & 0x1);
        num = num >> 1;
    }
    return val;
}
```

B (5 pts). Describe what this function computes in one English sentence (or at most two).

The function returns an int that has the same bits as stored at x but in reverse order.

3. Procedures (40 points)

The following assembly routine takes a positive integer as input and returns a positive integer:

```
0000000000400525 <mystery>:
 400525: 55                push   %rbp
 400526: 48 89 e5         mov    %rsp,%rbp
 400529: 53                push   %rbx
 40052a: 48 83 ec 18      sub    $0x18,%rsp

 40052e: 89 7d ec         mov    %edi,-0x14(%rbp)
 400531: 83 7d ec 00      cmpl  $0x0,-0x14(%rbp)
 400535: 75 07            jne   40053e <mystery+0x19>
 400537: b8 00 00 00 00  mov    $0x0,%eax
 40053c: eb 2b            jmp   400569 <mystery+0x44>
 40053e: 83 7d ec 01      cmpl  $0x1,-0x14(%rbp)
 400542: 75 07            jne   40054b <mystery+0x26>
 400544: b8 01 00 00 00  mov    $0x1,%eax
 400549: eb 1e            jmp   400569 <mystery+0x44>

 40054b: 8b 45 ec         mov    -0x14(%rbp),%eax
 40054e: 83 e8 01         sub    $0x1,%eax
 400551: 89 c7            mov    %eax,%edi
 400553: e8 cd ff ff ff  callq 400525 <mystery>
 400558: 89 c3            mov    %eax,%ebx
 40055a: 8b 45 ec         mov    -0x14(%rbp),%eax
 40055d: 83 e8 02         sub    $0x2,%eax
 400560: 89 c7            mov    %eax,%edi
 400562: e8 be ff ff ff  callq 400525 <mystery>
 400567: 01 d8            add    %ebx,%eax

 400569: 48 83 c4 18      add    $0x18,%rsp
 40056d: 5b                pop    %rbx
 40056e: 5d                pop    %rbp
 40056f: c3                retq
```

A (5 pts). Does this assembly code appear to follow the 32-bit or 64-bit parameter-passing guidelines? How can you tell?

The function uses mostly 64-bit registers. Also, input arguments are passed using %edi which indicates parameter passing through registers another sign of a 64-bit architecture. Don't be confused by the presence of the base pointer register, %rbp. A frame base pointer can still be used in the 64-bit architecture.

B (5 pts). Why is `%rbx` pushed onto the stack initially and then popped at the end?

%rbx is a callee-saved register, and the code uses %rbx (or %ebx) so it must save it before it overwrites it and then restore it before it returns.

C (5 pts). There are two `if()` statements in the code that produced this assembly. At which instruction addresses do they begin?

0x400531 and 0x40053e, where both of the comparisons occur.

D (5 pts). What does the byte `'ec'` most likely correspond to in the instruction at `0x40055a`?

'ec' is the twos-complement version of -0x14, the offset being used in the move instruction at that address.

E (15 pts). Write out C code that would assemble into the routine above.

```
unsigned int mystery(unsigned int n) {  
    if (n == 0) return 0;  
    if (n == 1) return 1;  
    return ( mystery(n-1) + mystery(n-2) );  
  
}
```

F (5 pts). What does this function do?

It returns the nth Fibonacci number (0,1,1,2,3,5,8,...).

4. Stack Discipline (25 points)

Consider a stack from an IA32 machine with the following contents:

Line ref number	Address in memory	Value in memory	Check if ret addr	Check if arg or local var	Check if saved ebp
22	0xffffffffc	0x00000001		✓	
21	0xffffffff8	0x00000005		✓	
20	0xffffffff4	0xffffffffc		✓	
19	0xffffffff0	0x004080a0	✓		
18	0xfffffffec	0xffffffffc			✓
17	0xffffffe8	0x00000005		✓	
16	0xffffffe4	0x0040801e	✓		
15	0xffffffe0	0xfffffffec			✓
14	0xffffffd4	0x00000004		✓	
13	0xfffffd8	0x0040801e	✓		
12	0xfffffd4	0xffffffe0			✓
11	0xfffffd0	0x00000003		✓	
10	0xfffffcc	0x0040801e	✓		
9	0xfffffc8	0xfffffd4			✓
8	0xfffffc4	0x00000002		✓	
7	0xfffffc0	0x0040801e	✓		
6	0xfffffbc	0xfffffc8			✓
5	0xfffffb8	0x00800000		✓	
4	0xfffffb4	0x008000d0		✓	
3	0xfffffb0	0x00000001		✓	
2	0xfffffac	0x00000001		✓	
1	0xfffffa8	0x00408053	✓		
	0xfffffa4				
	0xfffffa0				

Furthermore, you know that your code is in memory in locations from 0x00400000 to 0x005fffff and that your dynamic data heap is in locations 0x00800000 to 0x009fffff.

A (5 pts). Assume that machine execution has just been stopped just before the first instruction of a procedure. What address will we return to after that procedure completes?

The return address last placed on the stack in line 1, or 0x00408053.

B (5 pts). How much space did the calling procedure making this last call allocate on the stack for local variables and arguments? List the reference numbers of stack elements.

2, 3, 4, 5

C (10 pts). Annotate the stack on the previous page with the type of data stored at that location on the stack by placing a check mark in the appropriate column.

D (5 pts). Is there a recursive procedure on the stack? If so, how many calls deep is the recursion at the point represented by the stack above?

Yes, the four return addresses at lines 7, 10, 13, and 16 are the same indicating that we are four deep into a recursion.

REFERENCES

Powers of 2:

$2^0 = 1$	
$2^1 = 2$	$2^{-1} = .5$
$2^2 = 4$	$2^{-2} = .25$
$2^3 = 8$	$2^{-3} = .125$
$2^4 = 16$	$2^{-4} = .0625$
$2^5 = 32$	$2^{-5} = .03125$
$2^6 = 64$	$2^{-6} = .015625$
$2^7 = 128$	$2^{-7} = .0078125$
$2^8 = 256$	$2^{-8} = .00390625$
$2^9 = 512$	$2^{-9} = .001953125$
$2^{10} = 1024$	$2^{-10} = .0009765625$

Assembly Code Instructions:

push	push a value onto the stack and decrement the stack pointer
pop	pop a value from the stack and increment the stack pointer
call	jump to a procedure after first pushing a return address onto the stack
ret	pop return address from stack and jump there
mov	move a value between registers and memory
lea	compute effective address and store in a register
add	add 1 st operand to 2 nd with result stored in 2 nd
sub	subtract 1 st operand from 2 nd with result stored in 2 nd
and	bit-wise AND of two operands with result stored in 2 nd
or	bit-wise OR of two operands with result stored in 2 nd
shr	shift data by 1 bit to the right
jmp	jump to address
cmp	subtract 1 st operand from 2 nd and set flags
jne	conditional jump to address if zero flag is not set