CSE351 Autumn 2010 Final Exam (December 13, 2010)

Please read through the entire examination first! We designed this exam so that it can be completed in 100 minutes and, hopefully, this estimate will prove to be reasonable.

There are 7 problems worth a total of 100 points. The point value of each problem is indicated in the table below. Write your answer neatly in the spaces provided. If you need more space (you shouldn't), you can write on the back of the sheet where the question is posed, but please make sure that you indicate clearly the problem to which the comments apply. Do NOT use any other paper to hand in your answers. If you have difficulty with part of a problem, move on to the next one. They are mostly independent of each other.

The exam is CLOSED book and CLOSED notes. Please do not ask or provide anything to anyone else in the class during the exam. Make sure to ask clarification questions early so that both you and the others may benefit as much as possible from the answers.

Name:

| Problem | Max Score | Score |
|---------|-----------|-------|
| 1 | 12 | |
| 2 | 10 | |
| 3 | 10 | |
| 4 | 12 | |
| 5 | 24 | |
| 6 | 20 | |
| 7 | 12 | |
| TOTAL | 100 | |

1. Caches (12 points)

When images are printed on paper four different inks are used to generate colors: cyan, magenta, yellow, and black (CMYK). Software that deals with color printing needs to be able to represent images as arrays of these colors. For this problem we would like to determine the efficiency of the following code on a machine with a 2048-byte direct-mapped data cache with 32-byte blocks. We are given the following data definitions:

```
struct point_color {
  int c;
  int m;
  int y;
  int k;
};
struct point_color grid[16][16];
int i, j;
```

Assume the following:

- sizeof(int) == 4
- grid begins at memory address 0
- The cache is initially empty
- The only memory accesses are to the entries of array grid. Variables i and j are stored in registers

What is the cache hit ratio when the following code is executed?

```
for (i = 0; i < 16; i++) {
  for (j = 0; j < 16; j++) {
    grid[i][j].c = 0;
    grid[i][j].m = 0;
    grid[i][j].y = 0;
    grid[i][j].k = 0;
}</pre>
```

Include enough details so we can follow your calculations. Please try to simplify your answers, but it's ok if you need to save time by leaving some of them as fractions.

```
Write
Your
Answer
On the
Next
Page ...
```

1. Caches (cont.)

Write your answer here.

2. Caches and Programming (10 points)

Three programmers are debating how best to write the code to transpose a matrix in a C software package that will run on a variety of different machines. The exact details of the different computers aren't known. What is known is that all of them have caches and virtual memory. The matrix is much too large to fit entirely in the caches, but it is small enough to fit in main memory, so virtual memory paging is not an issue. The array is a normal C array of doubles stored in row-major order.

Alice says that this code will do the best overall job:

```
for (i = 0; i < N; i++) {
  for (j = 0; j < N; j++) {
    temp = A[i][j];
    A[i][j] = A[j][i];
    A[j][i] = temp;
}</pre>
```

Bob says that this is all wrong and that the performance will be much better if it's written this way:

```
for (j = 0; j < N; j++) {
  for (i = 0; i < N; i++) {
    temp = A[i][j];
    A[i][j] = A[j][i];
    A[j][i] = temp;
}</pre>
```

Chris says it doesn't matter. The code will perform about the same either way.

Who's right and why? Give a brief technical justification for your answer.

3. Disk Performance (10 points)

The Round Number Disk Manufacturing Company specializes in manufacturing disks designed to produce simple calculations on CSE exams. Their CSE351 Special has the following performance characteristics:

Rotational speed: 6000 rpm (100 revolutions per second)

Average seek time: 5 ms.

Number of sectors (data blocks) per track: 1000

Sector size: 500 bytes

The disk has only two surfaces on a single platter. Tracks on both surfaces can be accessed without moving the head once it is in position after a seek.

Recall that the time needed to read data from a disk is the time needed to position the head over the first block (average rotational latency and seek time) plus the time for the data to move under the head once it is positioned.

a) What is the best expected time in milliseconds (ms) needed to read 1,000,000 bytes from the disk, assuming that the data is organized sequentially on the disk with the best possible mapping of logical blocks to disk sectors.

b) What is the expected time in milliseconds (ms) needed to read the same 1,000,000 bytes from the disk if the data blocks are scattered randomly on the disk?

4. Linking and Relocation (12 points)

Here is the code and relocation information for a small function named f. Lines have been numbered for reference below

```
1)
      00000000 <f>:
2)
         0: 55
                                     push
                                            %ebp
3)
         1: 89 e5
                                    mov
                                            %esp, %ebp
4)
         3: 83 ec 10
                                    sub
                                            $0x10,%esp
5)
         6: a1 0c 00 00 00
                                    mov
                                            0xc, %eax
                              7: R 386 32 stuff
6)
7)
        b: a3 00 00 00 00
                                    mov
                                            %eax,0x0
                              c: R 386 32 data
8)
        10: c7 45 f8 fc ff ff
                                    movl $0xfffffffc, -0x8(%ebp)
9)
                              13: R_386_32 stuff
10)
        17: b8 11 00 00 00
                                     mov
                                            $0x11,%eax
11)
        1c: c9
12)
                                     leave
13)
        1d: c3
                                     ret
```

When this code is loaded, the linker assigned the following absolute addresses for the external symbols in the .code and .data sections of the program, and loads the bytes of function f starting at the address given here (0x08048394):

| f | 0x08048394 |
|-------|------------|
| stuff | 0x08049634 |
| data | 0x08049648 |

The above code contains three relocated references. For each relocated reference, give the line number in the above code of the instruction that is being relocated, the runtime memory address of the relocated data, and the relocated value stored at that address.

| Relocated Data Address | Relocated Data Value |
|------------------------|------------------------|
| | |
| | |
| | |
| | |
| | |
| | |
| | Relocated Data Address |

5. Virtual Memory (24 points)

Our system implements virtual memory with a translation look-aside buffer (TLB - 16 entries, 4-way set associative), page table (PT - 1024 page entries, only the first 16 shown below), and memory cache (16 entries, 4-byte lines, direct-mapped). The initial contents are shown in the tables below. The virtual address is 16 bits (4 hex digits) while the physical address is 12 bits (3 hex digits); the page size is 64 bytes.

(You can remove this page for reference while answering the rest of this question.)

TLB

| Set | Tag | PPN | Valid |
|-----|-----|-----|-------|-----|-----|-------|-----|-----|-------|-----|-----|-------|
| 0 | 03 | - | 0 | 09 | 0D | 1 | 00 | - | 0 | 07 | 02 | 1 |
| 1 | 03 | 2D | 1 | 02 | - | 0 | 04 | - | 0 | 0A | - | 0 |
| 2 | 02 | 33 | 1 | 08 | - | 0 | 06 | - | 0 | 03 | 11 | 1 |
| 3 | 07 | - | 0 | 03 | 0D | 1 | 0A | 34 | 1 | 02 | - | 0 |

Page Table

| VPN | PPN | Page Valid | | VPN | PPN | Valid |
|-----|-----|---------------|---|-----|-----|-------|
| 000 | 28 | 1 | l | 008 | 13 | 1 |
| 001 | - | 0 | l | 009 | 17 | 1 |
| 002 | 09 | 1 | | 00A | 33 | 1 |
| 003 | 02 | 1 | | 00B | - | 0 |
| 004 | - | 0 | l | 00C | - | 0 |
| 005 | 16 | 1 | l | 00D | 2D | 1 |
| 006 | - | 0 | | 00E | 11 | 1 |
| 007 | - | 0 | | 00F | 0D | 1 |

Cache

| Index | Tag | Valid | В0 | B1 | B2 | В3 |
|-------|-----|-------|----|----|----|----|
| 0 | 28 | 1 | 99 | 1F | 23 | 11 |
| 1 | 15 | 0 | - | - | - | - |
| 2 | 1B | 1 | 00 | 02 | 04 | 08 |
| 3 | 36 | 0 | - | - | - | - |
| 4 | 32 | 1 | 43 | 6D | 8F | 09 |
| 5 | 0D | 1 | 36 | 72 | F0 | 1D |
| 6 | 31 | 0 | - | - | _ | _ |
| 7 | 16 | 1 | 11 | C2 | DF | 03 |

| Tag | Valid | В0 | B1 | B2 | В3 | |
|-----|--|------------------------------------|--|--|--|--|
| 11 | 1 | 3A | 00 | 51 | 89 | |
| 2D | 0 | | | - | - | |
| 2D | 1 | 93 | 15 | DA | 3B | |
| 0B | 0 | - | - | - | - | |
| 12 | 0 | - | | | - | |
| 16 | 1 | 04 | 96 | 34 | 15 | |
| 13 | 1 | 83 | 77 | 1B | D3 | |
| 14 | 0 | - | - | - | - | |
| | 11 2D 2D 0B 12 16 13 | 11 1 2D 0 2D 1 0B 0 12 0 16 1 13 1 | 11 1 3A 2D 0 - 2D 1 93 0B 0 - 12 0 - 16 1 04 13 1 83 | 11 1 3A 00 2D 0 2D 1 93 15 0B 0 12 0 16 1 04 96 13 1 83 77 | 11 1 3A 00 51 2D 0 2D 1 93 15 DA 0B 0 12 0 16 1 04 96 34 13 1 83 77 1B | |

a) (2 points) Outline the bits corresponding to each of the components of the virtual address, namely, the virtual page number (VPN), the virtual page offset (VPO), the TLB set index (TLBI), and the TLB tag value (TLBT).

| 15 | | | | | | | | |
|----|--|--|--|--|--|--|--|--|
| | | | | | | | | |

b) (2 points) Outline the bits corresponding to each of the components of the physical address, namely, the physical page number (PPN), the physical page offset (PPO), the cache set index (CI), the cache tag value (CT), and the cache byte offset (CO).

| 11 | | | | | | |
|----|--|--|--|--|--|--|
| | | | | | | |

c) (12 points) Determine the returned values for the following sequence of accesses and specify whether a TLB miss, page fault, and/or cache miss occurred. In some cases, it may not be possible to determine what value is accessed or whether there is a cache miss or not. For these cases, simply write ND (for Not Determinable). If it matters, assume the accesses occur in this sequence and each access updates the tables as needed.

| Virtual Address | Physical Address | Value | TLB Miss? | Page Fault? | Cache Miss? |
|-----------------|-------------------------|-------|-----------|-------------|--------------------|
| 0x01B9 | | | | | |
| 0×0363 | | | | | |
| 0x0353 | | | | | |
| 0x072B | | | | | |

d) (5 points) One of our customers is running the following code snippet to initialize every entry in a byte array to 0x00:

```
char array[32][32];

for (int i = 0; i < 32; i++) {
    for (int j = 0; j < 32; j++) {
        array[j][i] = 0;
    }
}</pre>
```

How many TLB misses occur when this code runs on our system? (You should assume this code is executed on a cold system with an initially empty cache and empty TLB.)

e) (3 points) Bernie Bitkiller, the summer intern, suggested that it would be better if we used the virtual address bits differently to access the TLB. His idea is that the TLBI (TLB Index) bits should be the high-order bits of the virtual address starting at bit 15, then the TLBT (TLB Tag) bits next, and the VPO (virtual page offset) bits in the lower-order part of the address ending with bit 0. Basically he wants to interchange the positions of the TLBI and TLBT bits.

| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|---|
| | | | | | | | | | | | | | | | |

Suppose we execute code that has many sequential reads from memory. How will this design perform for those programs? What will the TLB hit/miss ratios be like and why?

6. Memory Management (20 points)

One of our customers has an unusual request for an addition to our memory manager code. They would like to have the following function added:

```
void * max alloc(size t * size found)
```

- max_alloc() locates the largest single block on the free list and allocates it to the caller. It is similar to malloc, except that the caller does not specify the size requested; instead the largest available free block is allocated.
- If the free list is empty when max_alloc() is called, it returns null as the function result and does not use the pointer parameter size_found.
- Otherwise, if there is at least one block on the free list, max_alloc finds the largest such block, removes it from the free list, and returns a pointer to the payload part of the block as the function result. It also stores the payload size in bytes in the variable referenced by the pointer size_found. (i.e., this function has two outputs a pointer to the allocated block and the size of the block. The pointer is the value returned by the function; the size is stored in the memory location referenced by the parameter.)
- If two or more blocks on the free list have the maximum size, the function removes only one of them from the free list and allocates it. (i.e., you may break ties any way you wish)

Write C-like pseudo-code for this function, using the explicit free list from lab 7. Be sure to adhere to the specification above. Your pseudo-code should be close to C (with comments as needed), but don't worry about syntax details if you don't remember them exactly.

Here is the relevant code from our explicit free list implementation for reference. You may call any of the functions below. You may also remove this page and the next one from the exam if you wish. Write your answer on the page after that.

```
/* Alignment of blocks returned by mm_malloc. */
#define ALIGNMENT 8

/* Size of a word on this architecture. */
#define WORD_SIZE sizeof(void*)

/* Pointer to the first BlockInfo in the free list, the list's head. You can treat this as a BlockInfo*. */
#define FREE_LIST_HEAD *((BlockInfo **)mem_heap_lo())

/* Minimum implementation-internal block size (to account for size header, next ptr, prev ptr, and boundary tag). This is NOT the minimum size of an object that may be returned to the caller of mm_malloc. */
#define MIN_BLOCK_SIZE 4*WORD_SIZE
```

```
/* Macros for pointer arithmetic to keep other code cleaner. Casting
   to a char* has the effect that pointer arithmetic happens at the
  byte granularity (i.e. POINTER ADD(0x1, 1) would be 0x2). (By
   default, incrementing a pointer in C has the effect of incrementing
   it by the size of the type to which it points (e.g. BlockInfo).) */
#define POINTER ADD(p,x) ((char*)(p) + (x))
#define POINTER SUB(p,x) ((char*)(p) - (x))
/* A BlockInfo contains information about a block, including the size
   and usage tags, as well as pointers to the next and previous blocks
   in the free list.
  Note that the next and prev pointers are only needed when the block
   is free. To achieve better utilization, mm malloc would use the
   space for next and prev as part of the space it returns.
   | sizeAndTags | <- BlockInfo pointers in free list point here
      next | <- Pointers returned by mm malloc point here
   +----+
      prev
   +----+
   | space |
      . . .
* /
struct BlockInfo {
/* Size of the block (log(ALIGNMENT) high bits) and tags for whether
   the block and its predecessor in memory are in use. */
int sizeAndTags;
   // Pointer to the next block in the free list.
struct BlockInfo* next;
  // Pointer to the previous block in the free list.
struct BlockInfo* prev;
typedef struct BlockInfo BlockInfo;
/* SIZE(x) selects just the higher bits of x to ensure that it is
  properly aligned. Additionally, the low bits of the sizeAndTags
  member are used to tag a block as free/used, etc. */
#define SIZE(x) ((x) & \sim (ALIGNMENT - 1))
/* TAG USED bit mask used in sizeAndTags to mark a block as used. */
#define TAG USED 1
/* TAG PRECEDING USED is the bit mask used in sizeAndTags to indicate
   that the block preceding it in memory is used. (used in turn for
   coalescing) */
#define TAG PRECEDING USED 2
void insertFreeBlock(BlockInfo* freeBlock);
void removeFreeBlock(BlockInfo* freeBlock);
void coalesceFreeBlock(BlockInfo* oldBlock);
void * mm malloc (size t size);
void mm free (void *ptr);
```

6. Memory Management (cont)

Implement max_alloc below

```
void * max_alloc(size_t * size_found) {
// PLACE YOUR CODE HERE
```

7. Processes and Concurrency (12 points)

Suppose we have the following program:

```
int main()
{
    printf("0");
    if (fork() != 0) {
        printf("1");
        fork();
        printf("2");
    } else {
        printf("3");
    }
    exit(0);
}
```

List all of the possible outputs that can occur when this program is run. If it helps, feel free to draw a graph showing the various processes that are created.