Data III & Integers I

CSE 351 Spring 2022

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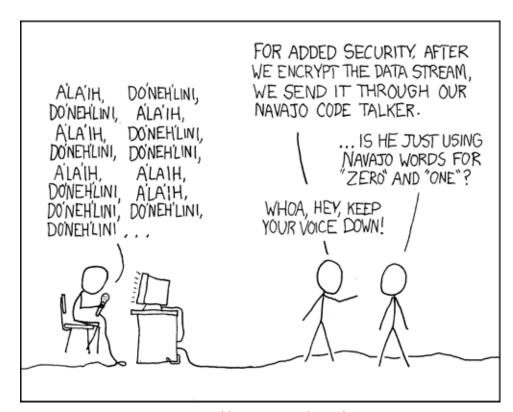
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http://xkcd.com/257/

Relevant Course Information

- Lab 0 and hw2 due tonight (4/04) @ 11:59 pm
- hw3 due Wednesday (4/06) @ 11:59 pm
- hw4 due Friday (4/08) @ 11:59 pm
- From here on out, at 11am on day of lecture:
 - Reading for that lecture is DUE at 11am
 - Lecture activities from the previous lecture are DUE at 11am

Lab 1a released!

- Labs can be found linked on our course home page:
 - https://courses.cs.washington.edu/courses/cse351/21sp/labs/lab1a.php
- Workflow:
 - 1) Edit pointer.c
 - 2) Run the Makefile (make clean followed by make) and check for compiler errors & warnings
 - 3) Run ptest (./ptest) and check for correct behavior
 - 4) Run rule/syntax checker (python3 dlc.py) and check output
- Due Monday 4/11, will overlap a bit with Lab 1b
 - Submit in Gradescope we grade just your last submission
 - Don't wait until the last minute to submit! Check autograder output!

Lab Synthesis Questions

- All subsequent labs (after Lab 0) have a "synthesis question" portion
 - Can be found on the lab specs and are intended to be done after you finish the lab
 - You will type up your responses in a .txt file for submission on Gradescope
 - These will be graded "by hand" (read by TAs)
- Intended to check your understanding of what you should have learned from the lab
 - Also great practice for short answer questions on the exams

Memory, Data, and Addressing

- Representing information as bits and bytes
 - Binary, hexadecimal, fixed-widths
- Organizing and addressing data in memory
 - Memory is a byte-addressable array
 - Machine "word" size = address size = register size
 - Endianness ordering bytes in memory
- Manipulating data in memory using C
 - Assignment
 - Pointers, pointer arithmetic, and arrays
- Boolean algebra and bit-level manipulations

Reading Review

- Terminology:
 - Bitwise operators (&, |, ^, ~)
 - Logical operators (&&, | |, !)
 - Short-circuit evaluation
 - Unsigned integers
 - Signed integers (Two's Complement)

Review Questions

- Compute the result of the following expressions for char c = 0x81;
 - **■** C ∧ C
 - ~c & 0xA9
 - c || 0x80
 - !!c
- Compute the value of signed char sc = 0xF0;
 (Two's Complement)

Bitmasks

- ❖ Typically binary bitwise operators (&, |, ∧) are used with one operand being the "input" and other operand being a specially-chosen bitmask (or mask) that performs a desired operation
- * Operations for a bit b (answer with 0, 1, b, or \overline{b}):

$$b \& 0 =$$

$$b \& 1 =$$

$$b \mid 0 =$$

$$b \mid 1 =$$

$$b \land 0 = _{__}$$

Bitmasks

- ❖ Typically binary bitwise operators (&, |, ∧) are used with one operand being the "input" and other operand being a specially-chosen bitmask (or mask) that performs a desired operation
- * Example: b|0 = b, b|1 = 1

$$\begin{array}{c} 01010101 \leftarrow \mathsf{input} \\ 11110000 \leftarrow \mathsf{bitmask} \\ 11110101 \end{array}$$

Short-Circuit Evaluation

- If the result of a binary logical operator (&&, | |) can be determined by its first operand, then the second operand is never evaluated
 - Also known as early termination
- Example: (p && *p) for a pointer p to "protect" the dereference
 - Dereferencing NULL (0) results in a segfault

Roadmap

C:

```
car *c = malloc(sizeof(car));
c->miles = 100;
c->gals = 17;
float mpg = get_mpg(c);
free(c);
```

Java:

Integers & floats x86 assembly Procedures & stacks Executables Arrays & structs Memory & caches Processes Virtual memory

Memory allocation

Assembly language:

```
get_mpg:
    pushq %rbp
    movq %rsp, %rbp
    ...
    popq %rbp
    ret
```

OS:

```
Windows 10 OS X Yosemite
```

Machine code:

Computer system:



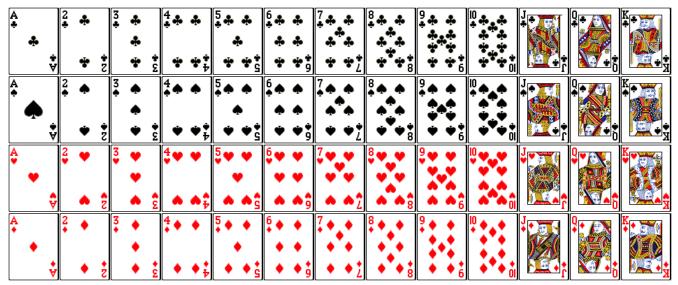




Java vs. C

Numerical Encoding Design Example

- Encode a standard deck of playing cards
- 52 cards in 4 suits
 - How do we encode suits, face cards?
- What operations do we want to make easy to implement?
 - Which is the higher value card?
 - Are they the same suit?

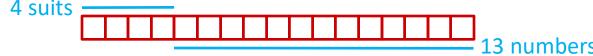


Two possible representations

1) 1 bit per card (52): bit corresponding to card set to 1

52 cards

- "One-hot" encoding (similar to set notation)
- Drawbacks:
 - Hard to compare values and suits
 - Large number of bits required
- 2) 1 bit per suit (4), 1 bit per number (13): 2 bits set



- Pair of one-hot encoded values (two fields)
- Easier to compare suits and values, but still lots of bits used

Two better representations

3) Binary encoding of all 52 cards – only 6 bits needed

$$2^6 = 64 \ge 52$$



low-order 6 bits of a byte

- Fits in one byte (smaller than one-hot encodings)
- How can we make value and suit comparisons easier?
- 4) Separate binary encodings of suit (2 bits) and value (4 bits)

bits) suit value

Also fits in one byte, and easy to do comparisons

K	Q	J	 3	2	Α
1101	1100	1011	 0011	0010	0001

•	00
•	01
	10
•	11

Compare Card Suits

mask: a bit vector designed to achieve a desired behavior when used with a bitwise operator on another bit vector v.

Here we turn all but the bits of interest in v to 0.

```
char hand[5];  // represents a 5-card hand
 char card1, card2; // two cards to compare
 card1 = hand[0];
 card2 = hand[1];
 if ( sameSuitP(card1, /card2) ) { ... }
#define SUIT MASK
                   0x30
int sameSuitP(char card1, char card2) {
  return (!((card1 & SUIT MASK) ^ (card2 & SUIT MASK)));
    return (card1 & SUIT MASK) == (card2 & SUIT MASK);
                                                equivalent
 returns int
            SUIT_MASK = 0x30 = |0|
                                        value
                                  suit
                                                          15
```

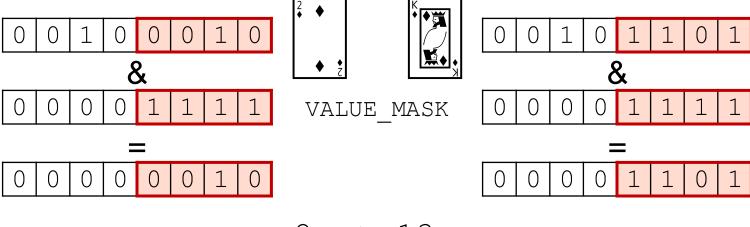
Compare Card Suits

```
#define SUIT MASK 0x30
int sameSuitP(char card1, char card2) {
  return (!((card1 & SUIT MASK) ^ (card2 & SUIT MASK)));
  //return (card1 & SUIT MASK) == (card2 & SUIT MASK);
                         SUIT MASK
! (x^y) equivalent to x==y
```

Compare Card Values

Compare Card Values

```
#define VALUE_MASK 0x0F
int greaterValue(char card1, char card2) {
   return ((unsigned int)(card1 & VALUE_MASK) >
        (unsigned int)(card2 & VALUE_MASK));
}
```



$$2_{10} > 13_{10}$$
0 (false)

Roadmap

C:

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car *c = malloc(sizeof(car));
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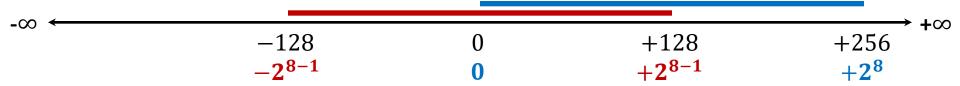
Java vs. C

Integers

- Binary representation of integers
 - Unsigned and signed
- Shifting and arithmetic operations
- In C: Signed, Unsigned and Casting
- Consequences of finite width representations
 - Overflow, sign extension

Encoding Integers

- The hardware (and C) supports two flavors of integers
 - unsigned only the non-negatives
 - signed both negatives and non-negatives
- Cannot represent all integers with w bits
 - Only 2^w distinct bit patterns
 - Unsigned values: $0 \dots 2^w 1$
 - Signed values: $-2^{w-1} \dots 2^{w-1} 1$
- Example: 8-bit integers (e.g. char)



Unsigned Integers (Review)

- Unsigned values follow the standard base 2 system
 - $b_7b_6b_5b_4b_3b_2b_1b_0 = b_72^7 + b_62^6 + \dots + b_12^1 + b_02^0$
- * Useful formula: $2^{N-1} + 2^{N-2} + ... + 2 + 1 = 2^N 1$
 - *i.e.*, N ones in a row = $2^N 1$
 - *e.g.*, 0b111111 = 63

Not used in practice for integers!

- Designate the high-order bit (MSB) as the "sign bit"
 - sign=0: positive numbers; sign=1: negative numbers

Benefits:

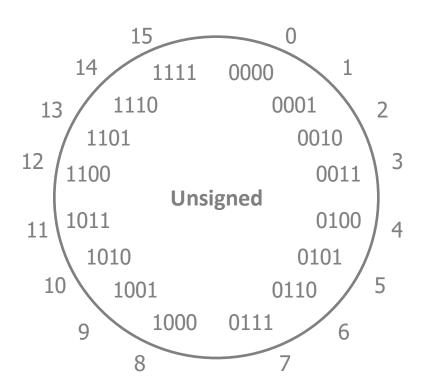
- Using MSB as sign bit matches positive numbers with unsigned
- All zeros encoding is still = 0

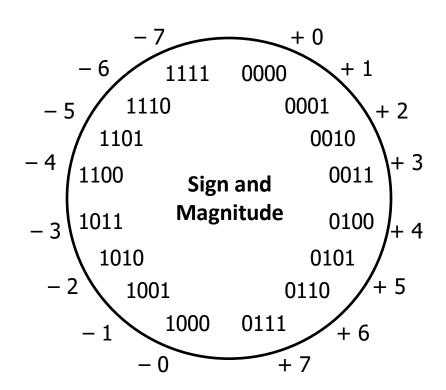
Examples (8 bits):

- $0x00 = 00000000_2$ is non-negative, because the sign bit is 0
- $0x7F = 011111111_2$ is non-negative (+127₁₀)
- $0x85 = 10000101_2$ is negative (-5₁₀)
- $0x80 = 10000000_2$ is negative... zero????

Not used in practice for integers!

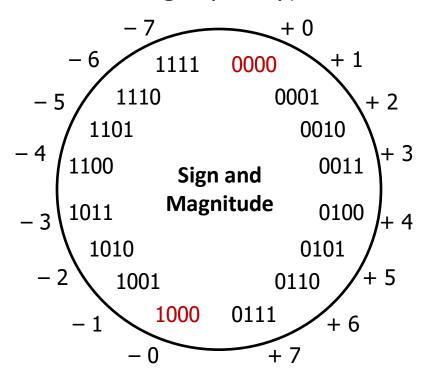
- MSB is the sign bit, rest of the bits are magnitude
- Drawbacks?





Not used in practice for integers!

- MSB is the sign bit, rest of the bits are magnitude
- Drawbacks:
 - Two representations of 0 (bad for checking equality)

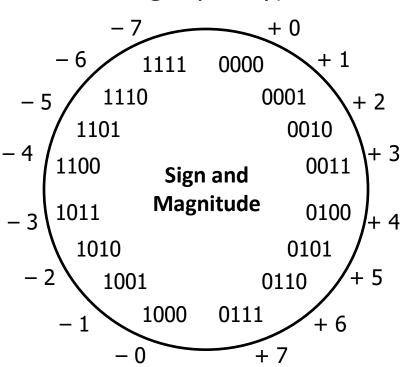


Not used in practice for integers!

- MSB is the sign bit, rest of the bits are magnitude
- Drawbacks:
 - Two representations of 0 (bad for checking equality)
 - Arithmetic is cumbersome
 - Example: 4-3 != 4+(-3)

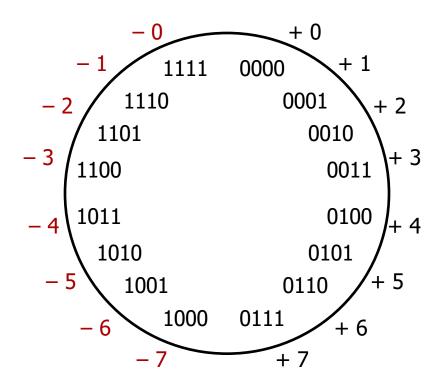
– /	1111
	1111
+ - 3	+ 1011
4	0100

Negatives "increment" in wrong direction!



Two's Complement

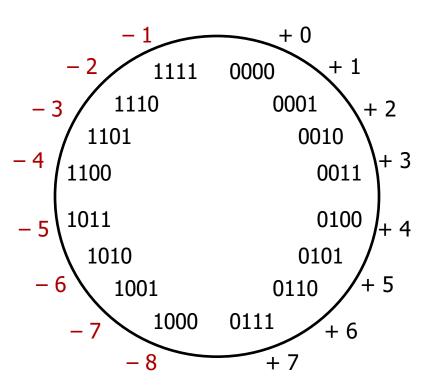
- Let's fix these problems:
 - 1) "Flip" negative encodings so incrementing works



Two's Complement

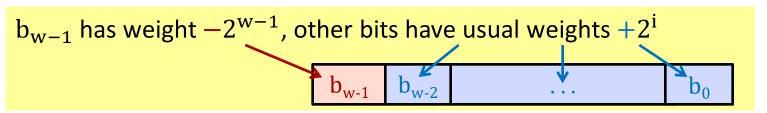
- Let's fix these problems:
 - 1) "Flip" negative encodings so incrementing works
 - 2) "Shift" negative numbers to eliminate -0

- MSB still indicates sign!
 - This is why we represent one more negative than positive number $(-2^{N-1} \text{ to } 2^{N-1} 1)$



Two's Complement Negatives (Review)

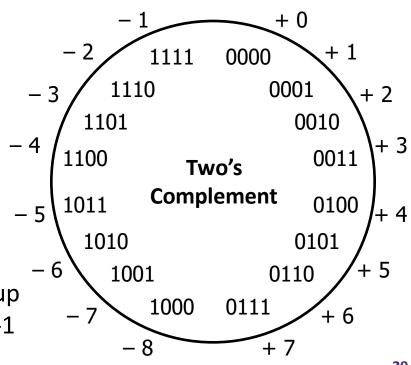
Accomplished with one neat mathematical trick!



- 4-bit Examples:
 - 1010_2 unsigned: $1*2^3+0*2^2+1*2^1+0*2^0=10$
 - 1010_2 two's complement: $-1*2^3+0*2^2+1*2^1+0*2^0 = -6$
- -1 represented as:

$$1111_2 = -2^3 + (2^3 - 1)$$

 MSB makes it super negative, add up all the other bits to get back up to -1



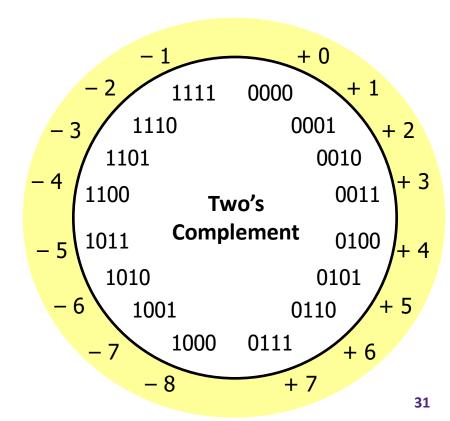
Polling Question

- * Take the 4-bit number encoding x = 0b1011
- Which of the following numbers is NOT a valid interpretation of x using any of the number representation schemes discussed today?
 - Unsigned, Sign and Magnitude, Two's Complement
 - Vote in Ed Lessons
 - A. -4
 - B. -5
 - C. 11
 - D. -3
 - E. We're lost...

Two's Complement is Great (Review)

- Roughly same number of (+) and (-) numbers
- Positive number encodings match unsigned
- Single zero
- All zeros encoding = 0

- Simple negation procedure:
 - Get negative representation of any integer by taking bitwise complement and then adding one!
 (~x + 1 == -x)



Summary

- Bit-level operators allow for fine-grained manipulations of data
 - Bitwise AND (&), OR (|), and NOT (\sim) different than logical AND (&&), OR (||), and NOT (!)
 - Especially useful with bit masks
- Choice of encoding scheme is important
 - Tradeoffs based on size requirements and desired operations
- Integers represented using unsigned and two's complement representations
 - Limited by fixed bit width
 - We'll examine arithmetic operations next lecture