

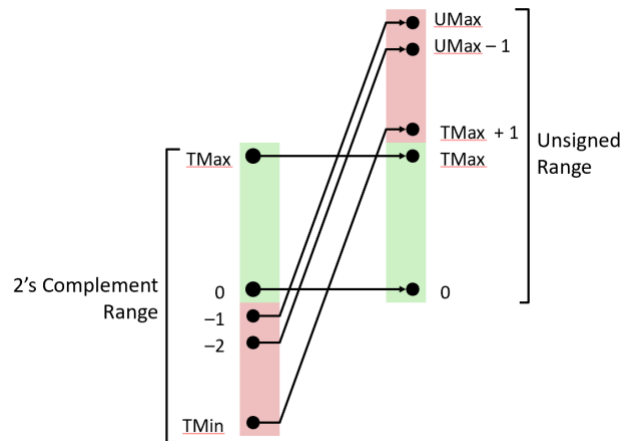
CSE 351 Section 3 – Integers and Floating Point

Welcome back to section, we're happy that you're here ☺

Integers and Arithmetic Overflow

Arithmetic overflow occurs when the result of a calculation can't be represented in the current encoding scheme (*i.e.*, it lies outside of the representable range of values), resulting in an incorrect value.

- **Unsigned overflow:** the result lies outside of [UMin, UMax]; an indicator of this is when you add two numbers and the result is smaller than either number.
- **Signed overflow:** the result lies outside of [TMin, TMax]; an indicator of this is when you add two numbers with the same sign and the result has the opposite sign.



Exercises:

- 1) Assuming these are all signed two's complement 6-bit integers, compute the result of each of the following additions. For each, indicate if it resulted in overflow. [Spring 2016 Midterm 1C]

| | | | |
|----------|----------|----------|----------|
| 001001 | 110001 | 011001 | 101111 |
| + 110110 | + 111011 | + 001100 | + 011111 |

- 2) Find the largest 8-bit unsigned numeral (answer in hex) such that $c + 0x80$ causes NEITHER signed nor unsigned overflow in 8 bits. [Autumn 2019 Midterm 1C]
- 3) Find the smallest 8-bit numeral (answer in hex) such that $c + 0x71$ causes signed overflow, but NOT unsigned overflow in 8 bits. [Autumn 2018 Midterm 1C]

4) What are the decimal values of the following `float`s?

`0x80000000`

`0xFF94BEEF`

`0x41180000`

Floating Point Mathematical Properties

- Not associative: $(2 + 2^{50}) - 2^{50} \neq 2 + (2^{50} - 2^{50})$
- Not distributive: $100 \times (0.1 + 0.2) \neq 100 \times 0.1 + 100 \times 0.2$
- Not cumulative: $2^{25} + 1 + 1 + 1 + 1 \neq 2^{25} + 4$

5) Based on floating point representation, explain why each of the three statements above occurs.

6) If `x` and `y` are variable type `float`, give two *different* reasons why `(x+2*y) - y == x+y` might evaluate to false.