Practice Cache Exam Problem (11 pts)
We have a 64 KiB address space. The cache is a 1 KiB, direct-mapped cache using 256-byte blocks with write-back and write-allocate policies.

a) Calculate the TIO address breakdown for:

<table>
<thead>
<tr>
<th>Tag</th>
<th>Index</th>
<th>Offset</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>2</td>
<td>8</td>
</tr>
</tbody>
</table>

\[
2^{16} = 64 \text{ KiB, so we have 16 bit addresses.}
\]

\[
16 - 2 - 8 = 6
\]

\[
\frac{2^{10}}{2^8} = 2^2 \rightarrow 2
\]

\[
2^8 = 256 \rightarrow 8
\]

b) During some part of a running program, the cache's management bits are as shown below. Four options for the next two memory accesses are given (R = read, W = write). Circle the option that results in data from the cache being written to memory.

<table>
<thead>
<tr>
<th>Line</th>
<th>Valid</th>
<th>Dirty</th>
<th>Tag</th>
</tr>
</thead>
<tbody>
<tr>
<td>00</td>
<td>0</td>
<td>0</td>
<td>1000 01</td>
</tr>
<tr>
<td>01</td>
<td>1</td>
<td>1</td>
<td>0101 01</td>
</tr>
<tr>
<td>10</td>
<td>1</td>
<td>0</td>
<td>1110 00</td>
</tr>
<tr>
<td>11</td>
<td>0</td>
<td>0</td>
<td>0000 11</td>
</tr>
</tbody>
</table>

Note that, since the last 8 bits form the offset, we can ignore the last two hex digits for this problem.

(1) R 0x4C00, W 0x5C00

R 0b0100 1100..., W 0b0101 1100...
The read evicts line 0, but the dirty bit was not set so nothing is written (also, line 0 was initially invalid).
The write overwrites line 0 again but since the cache is write-back nothing is written to memory.

(2) W 0x5500, W 0x7A0

W 0b01010101..., W 0b0111 1010...
The first write doesn't evict anything because the tags match. The second write evicts the old data but the dirty bit was not set so the old data doesn't need to be written back to memory.

(3) W 0x2300, R 0x0F08

W 0b0010 0011..., R 0000 1111...
The write evicts line 3 which was invalid and also not dirty, so nothing is written. The read, however, also maps to line 3 so it must write the value changed in the write back to memory before it can update the cache.

(4) R 0x3000, R 0x3000

R 0b0011 0000..., R 0011 0000...
Line 0 is initially not dirty (and invalid) so nothing is written back to memory from either of these reads (which both read from the same line).

c) The code snippet below loops through a character array. Give the value of LEAP that results in a Hit Rate of 15/16.

```c
#define ARRAY_SIZE 8192
char string[ARRAY_SIZE]; // &string = 0x8000
for(i = 0; i < ARRAY_SIZE; i += LEAP) {
    string[i] |= 0x20; // to lower
}
```

Note that |= is a read and a write (i.e., two accesses). To obtain a 15/16 hit rate, we want to perform \( \frac{256}{16} = 16 \) accesses per block (the first access will be a miss, subsequent accesses will be hits). However, since each loop iteration performs two accesses, we want to loop 8 times per block. Therefore \( \text{LEAP} = \frac{256}{8} = 32 \).
d) For the loop shown in part (c), let LEAP = 64. Circle ONE of the following changes that increases the hit rate:

- Larger block size mean that we can fit more bytes in a block, so more information will be pulled in on each miss. Therefore, hit rate will increase.
- Increasing cache size will not change hit rate since we are accessing data contiguously.
- Adding a L2 cache will not change the hit rate (it will just decrease the miss penalty).
- Increasing LEAP will increase the miss rate since data accessed will be further apart in memory.

e) What are the three kinds of cache misses? Circle the kind of miss that happens in part (c)

- Compulsory
- Conflict
- Capacity

Benedict Cumbercache:

Given the following sequence of access results (addresses are given in decimal) on a cold/empty cache of size 16 bytes, what can we deduce about its properties? Assume an LRU replacement policy.

(1) (2) (3) (4) (5)
(0, Miss), (8, Miss), (0, Hit), (16, Miss), (8, Miss)

1) What can we say about the block size?

After access (1), values from address 0 to address [block size - 1] will be put in the cache. This is because caches load a full block from memory at a time and 0 will always be aligned to the beginning of a block. Thus, if access (2) to address 8 is a miss, it means that the block size must be ≤ 8.

2) Assuming that the block size is 8 bytes, can this cache be...

a. Direct-mapped?

<table>
<thead>
<tr>
<th>Index</th>
<th>Address (not tag)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0x0 0x10</td>
</tr>
<tr>
<td>1</td>
<td>0x8</td>
</tr>
</tbody>
</table>

Does this cache work for the access results?
Yes, Yes, Yes, Yes (evict 0), No (8 would still be in cache)

b. 2-way set associative?

<table>
<thead>
<tr>
<th>Index</th>
<th>Address (not tag)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0x0</td>
</tr>
<tr>
<td>0</td>
<td>0x8 0x10</td>
</tr>
</tbody>
</table>

Does this cache work for the access results?
Yes, Yes, Yes, Yes (evict 8 b/c it’s the least recently used), Yes (8 is no longer in cache)

c. 4-way set associative?

No, because the block size is 8, multiplied by 4 lines per set, and that’s 32B, which is already bigger than the entire cache.
Fork and Concurrency:

Consider this code using Linux's `fork`:

```c
int x = 7;
if( fork() ) {
    x++;
    printf(" %d ", x);
    fork();
    x++;
    printf(" %d ", x);
} else {
    printf(" %d ", x);
}
```

What are all the different possible outputs (i.e. order of things printed) for this code?
(Hint: there are four of them.)

**Note:** `fork()` returns 0 to the child, and the child’s process ID (PID) to the parent.

From our first fork, we know child 1 will print “7”, but since this print statement is not dependent on any other code (besides the initial `fork()`), it could be printed at any time.

We also know the parent will have to print “8” before the second call to `fork()`, meaning that the “8” is printed before the “9”s. Since the parent and child 2 both print out “9”, even if the ordering of their prints changes, the output will not.

Possible orderings:
- 7 8 9 9
- 8 7 9 9
- 8 9 7 9
- 8 9 9 7