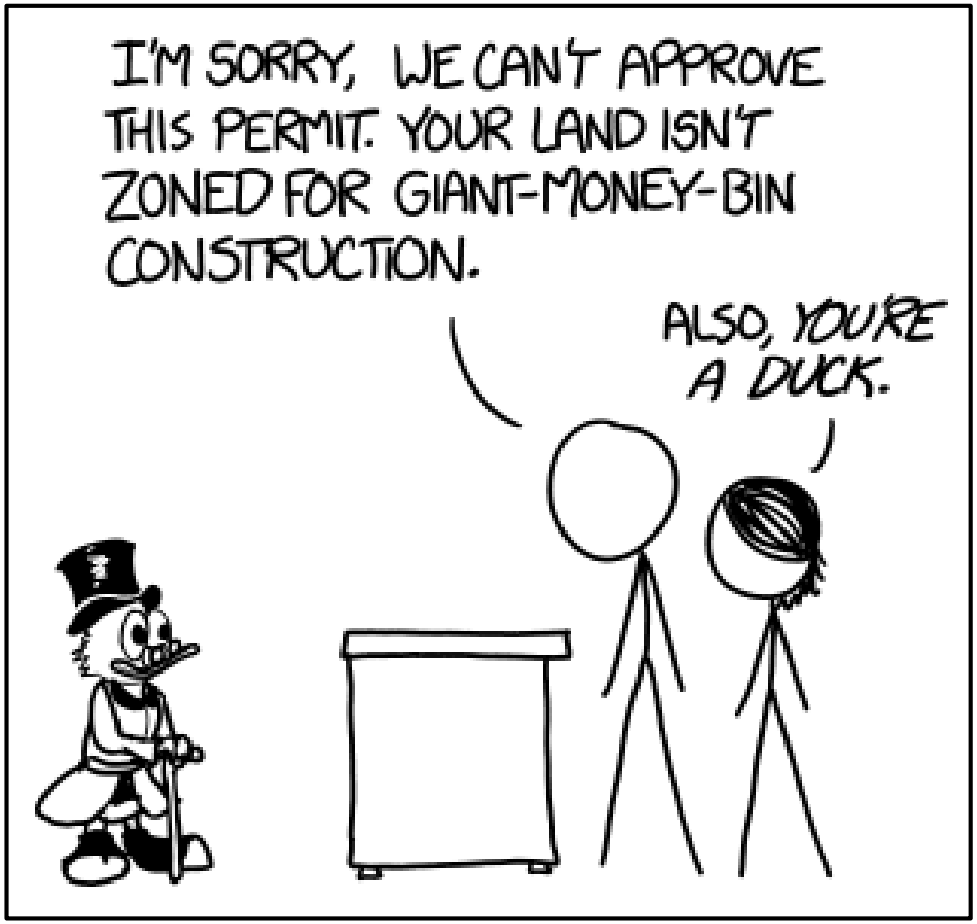
Caches III

CSE 351 Spring 2020

Instructor:
Ruth Anderson

Teaching Assistants:
Alex Olshanskyy
Rehaan Bhimani
Callum Walker
Chin Yeoh
Diya Joy
Eric Fan
Edan Sneh
Jonathan Chen
Jeffery Tian
Millicent Li
Melissa Birchfield
Porter Jones
Joseph Schafer
Connie Wang
Eddy (Tianyi) Zhou



https://what-if.xkcd.com/111/

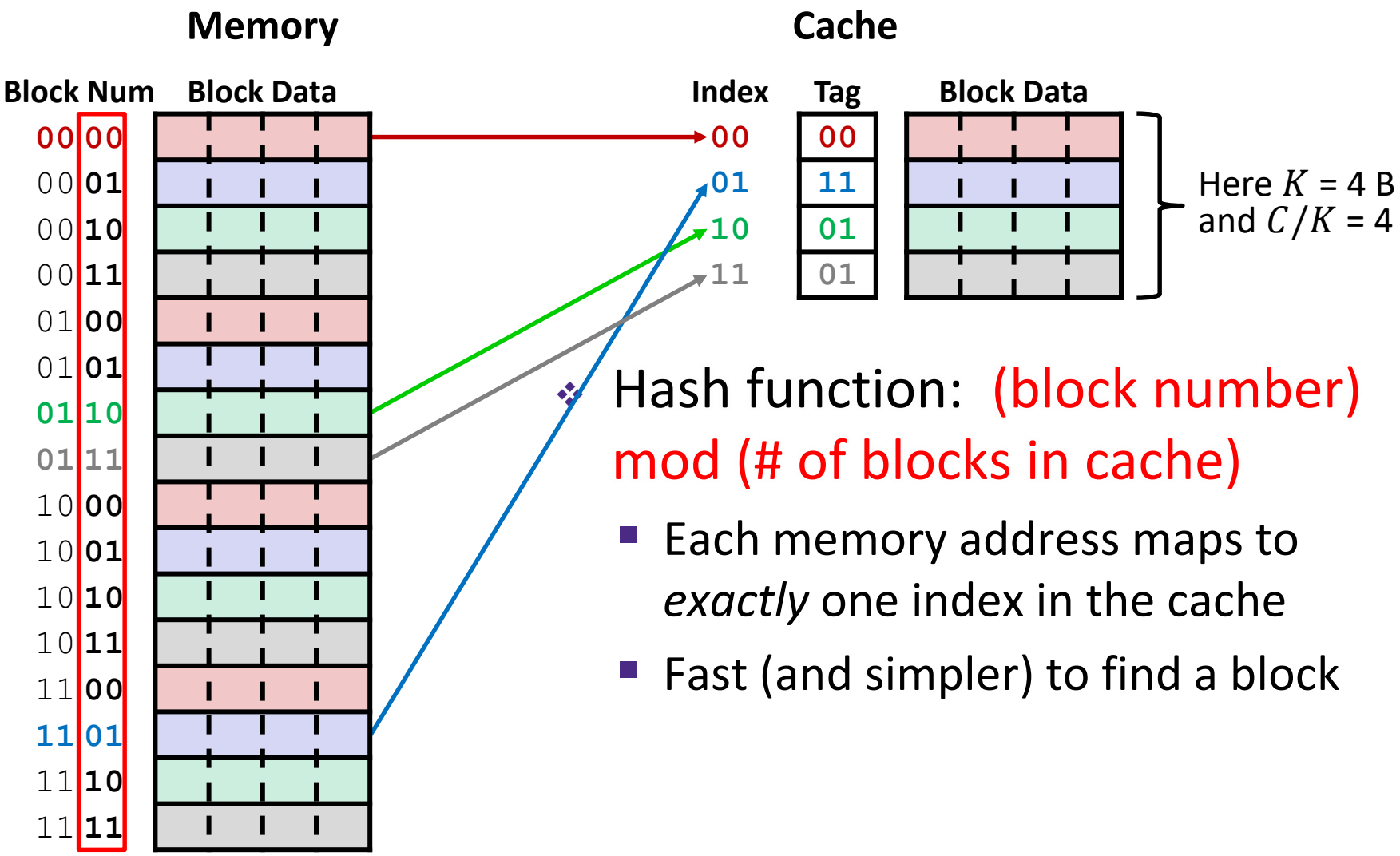
Administrivia

- Unit Summary #2 due TONIGHT, Friday (5/08)
  - Submit to Canvas – TWO SEPARATE SUBMISIONS
- Lab 3 due Wednesday (5/13)
- **You must log on with your @uw google account to access!!**
  - **Google doc** for 11:30 Lecture: https://tinyurl.com/351-05-08A
  - **Google doc** for 2:30 Lecture: https://tinyurl.com/351-05-08B

Making memory accesses fast!

- Cache basics
- Principle of locality
- Memory hierarchies
- Cache organization
  - Direct-mapped (*sets*; index + tag)
  - **Associativity (*ways*)**
  - **Replacement policy**
  - Handling writes
- Program optimizations that consider caches

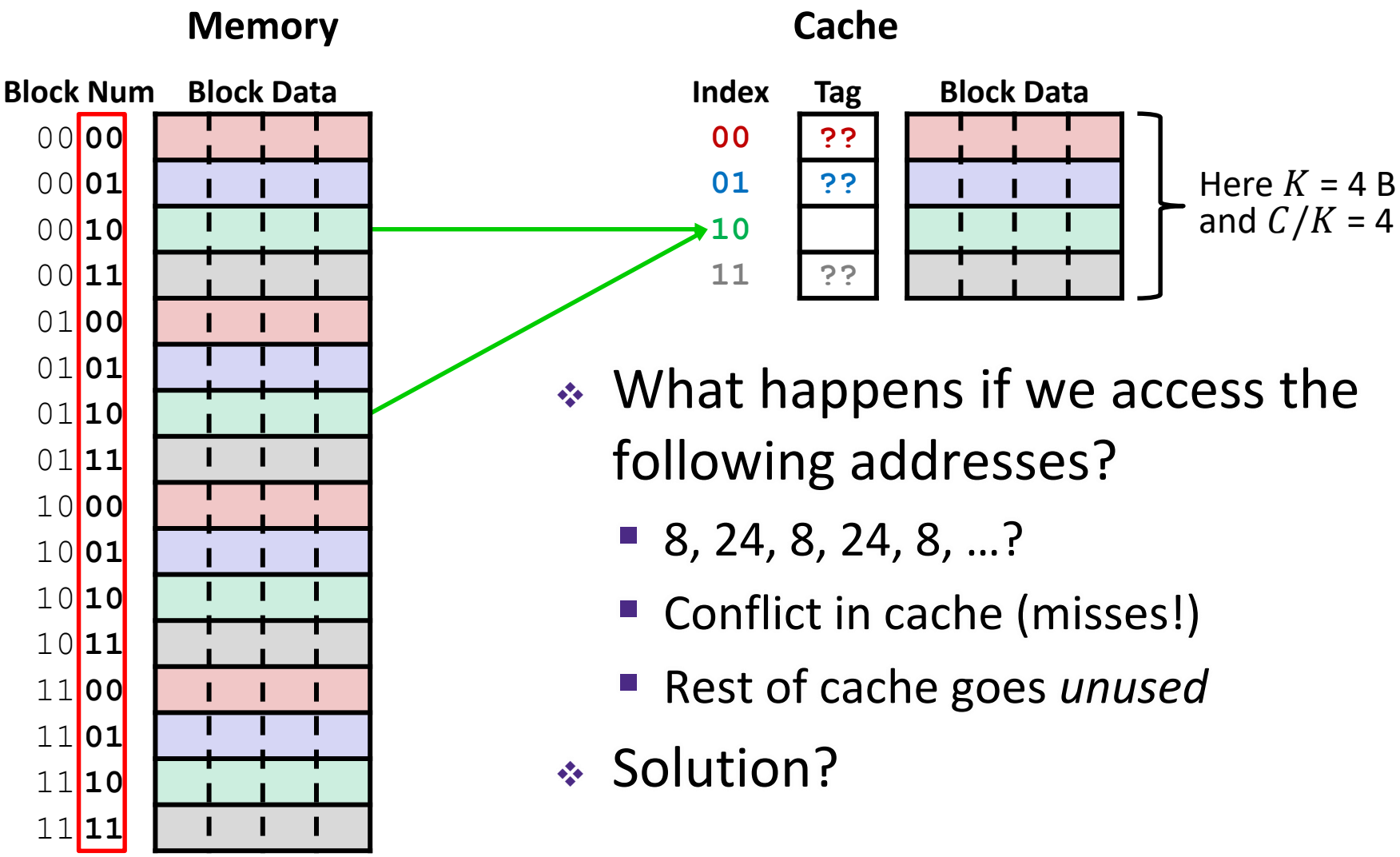
Review: Direct-Mapped Cache



Hash function: (block number) mod (# of blocks in cache)

- Each memory address maps to *exactly* one index in the cache
- Fast (and simpler) to find a block

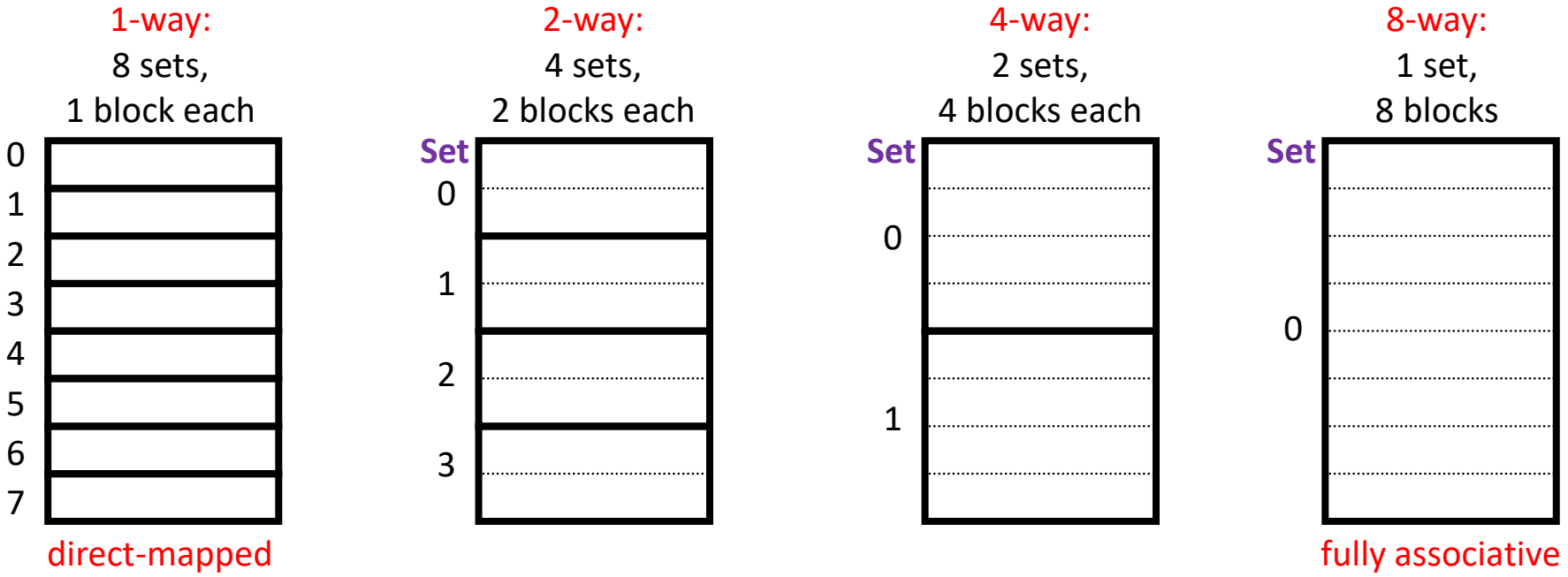
Direct-Mapped Cache Problem



- What happens if we access the following addresses?
  - 8, 24, 8, 24, 8, …?
  - Conflict in cache (misses!)
  - Rest of cache goes *unused*
- Solution?

Associativity

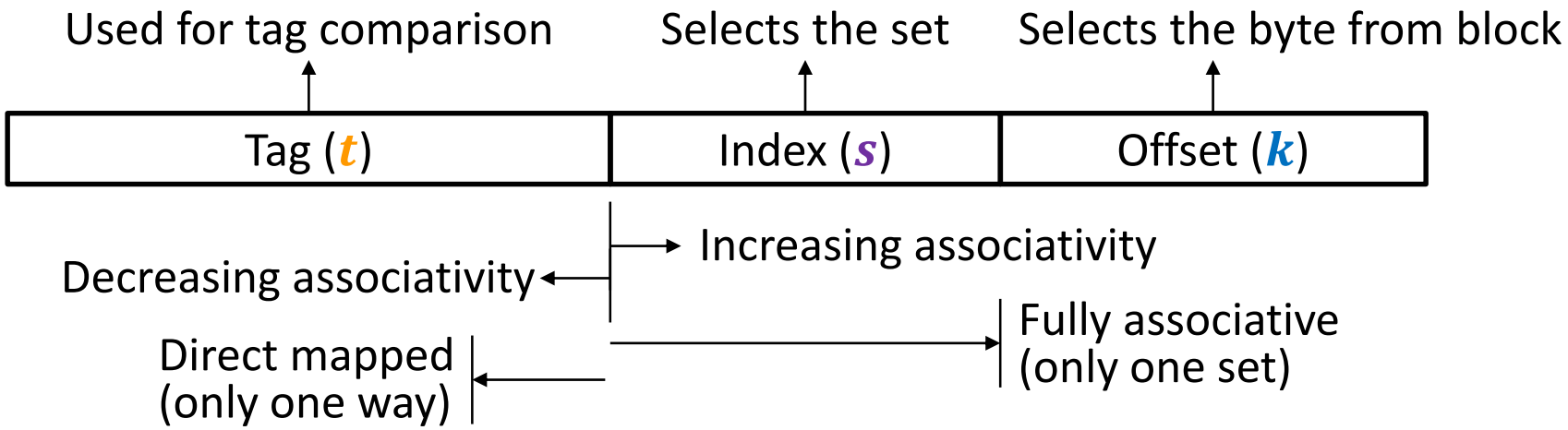
- What if we could store data in any place in the cache?
  - More complicated hardware = more power consumed, slower
- So we *combine* the two ideas:
  - Each address maps to exactly one **set**
  - Each set can store block in more than one **way**



Cache Organization (3)

Note: The textbook uses "b" for offset bits

- Associativity (E): # of ways for each set
  - Such a cache is called an "*E-way set associative cache*"
  - We now index into cache *sets*, of which there are $S = C/K/E$
  - Use lowest $\log_2(C/K/E)$ = $\boldsymbol{s}$ bits of block address
    - Direct-mapped: E = 1, so $\boldsymbol{s}$ = $\log_2(C/K)$ as we saw previously
    - Fully associative: $E = C/K$, so $\boldsymbol{s}$ = 0 bits



Example Placement

block size:	16 B
capacity:	8 blocks
address:	16 bits

- Where would data from address `0x1833` be placed?
  - Binary: `0b 0001 1000 0011 0011`

$t = m-s-k$ $s = \log_2(C/K/E)$ $k = \log_2(K)$

m-bit address:

Tag (t)	Index (s)	Offset (k)

s = ?
Direct-mapped

Set	Tag	Data
0		
1		
2		
3		
4		
5		
6		
7		

s = ?
2-way set associative

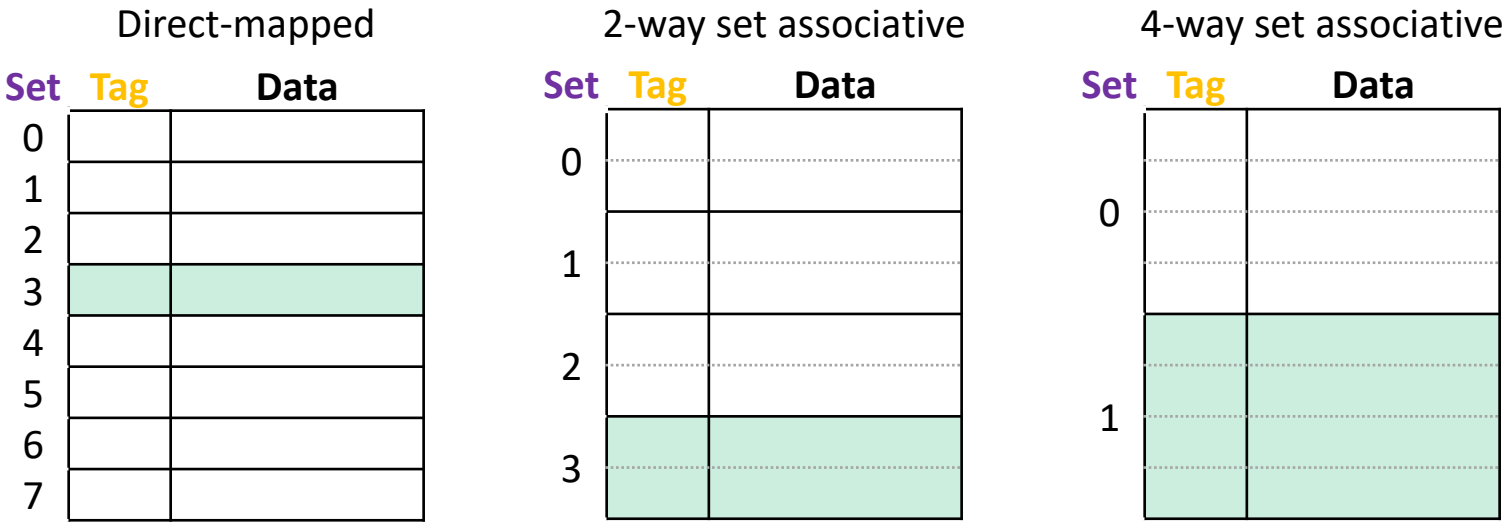
Set	Tag	Data
0		
1		
2		
3		

s = ?
4-way set associative

Set	Tag	Data
0		
1		

Block Replacement

- *Any* empty block in the correct set may be used to store block
- If there are no empty blocks, which one should we replace?
  - No choice for direct-mapped caches
  - Caches typically use something close to ***least recently used (LRU)*** (hardware usually implements "*not most recently used*")



Polling Question [Cache III]

- We have a cache of size 2 KiB with block size of 128 B. If our cache has 2 sets, what is its associativity?
  - Vote at http://pollev.com/rea

A. 2

B. 4

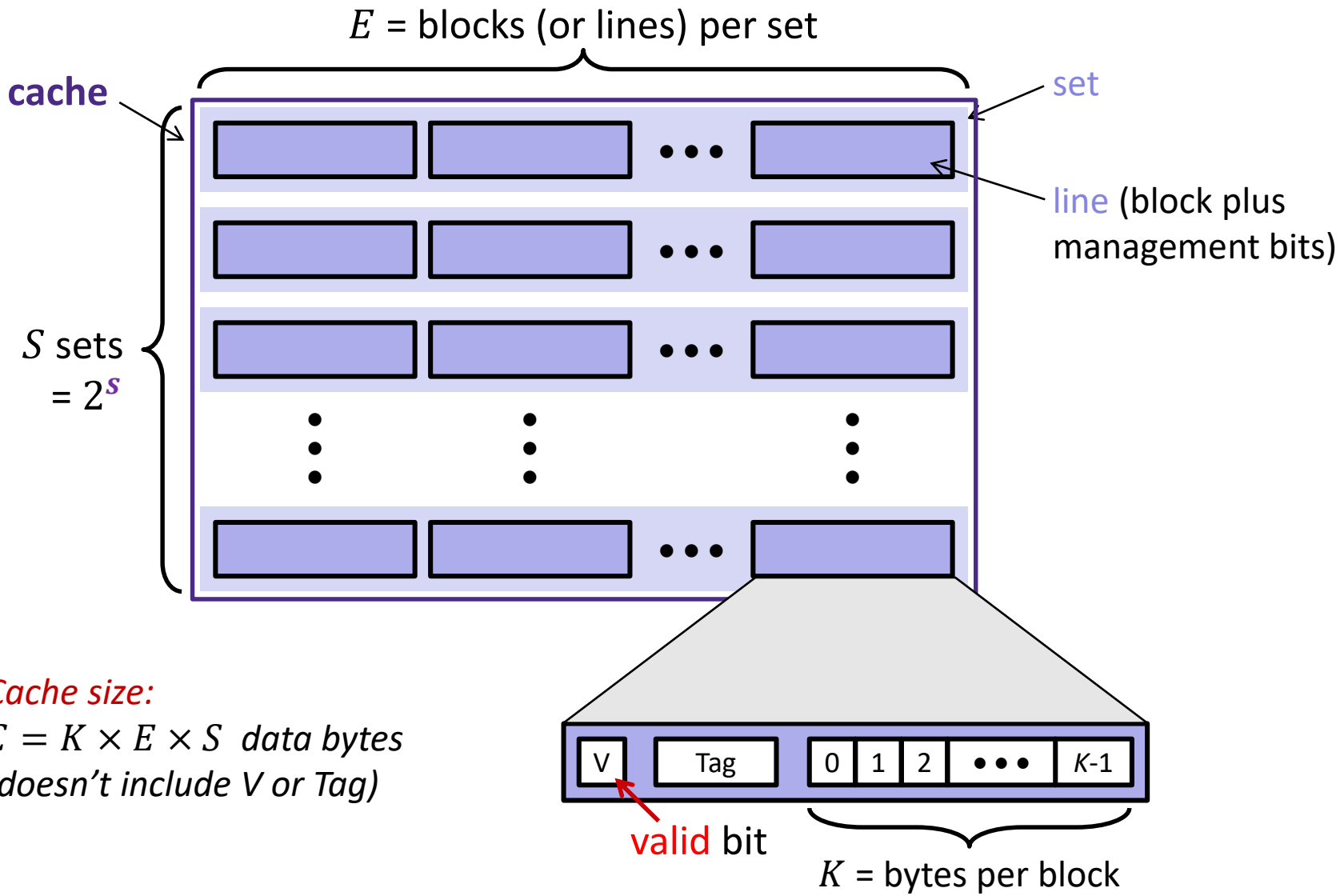
C. 8

D. 16

E. We're lost…

- If addresses are 16 bits wide, how wide is the Tag field?

General Cache Organization (S, E, K)



Cache size:
$C = K \times E \times S$ *data bytes*
(doesn't include V or Tag)

Notation Review

- We just introduced a lot of new variable names!
  - Please be mindful of block size notation when you look at past exam questions or are watching videos

Parameter	Variable	Formulas
Block size	K (B in book)	$M = 2^{\boldsymbol{m}} \leftrightarrow \boldsymbol{m} = \log_2 M$ $S = 2^{\boldsymbol{s}} \leftrightarrow \boldsymbol{s} = \log_2 S$ $K = 2^{\boldsymbol{k}} \leftrightarrow \boldsymbol{k} = \log_2 K$ $C = K \times E \times S$ $\boldsymbol{s} = \log_2(C/K/E)$ $\boldsymbol{m} = \boldsymbol{t} + \boldsymbol{s} + \boldsymbol{k}$
Cache size	C	
Associativity	E	
Number of Sets	S	
Address space	M	
Address width	$\boldsymbol{m}$	
Tag field width	$\boldsymbol{t}$	
Index field width	$\boldsymbol{s}$	
Offset field width	$\boldsymbol{k}$ ($\boldsymbol{b}$ in book)	

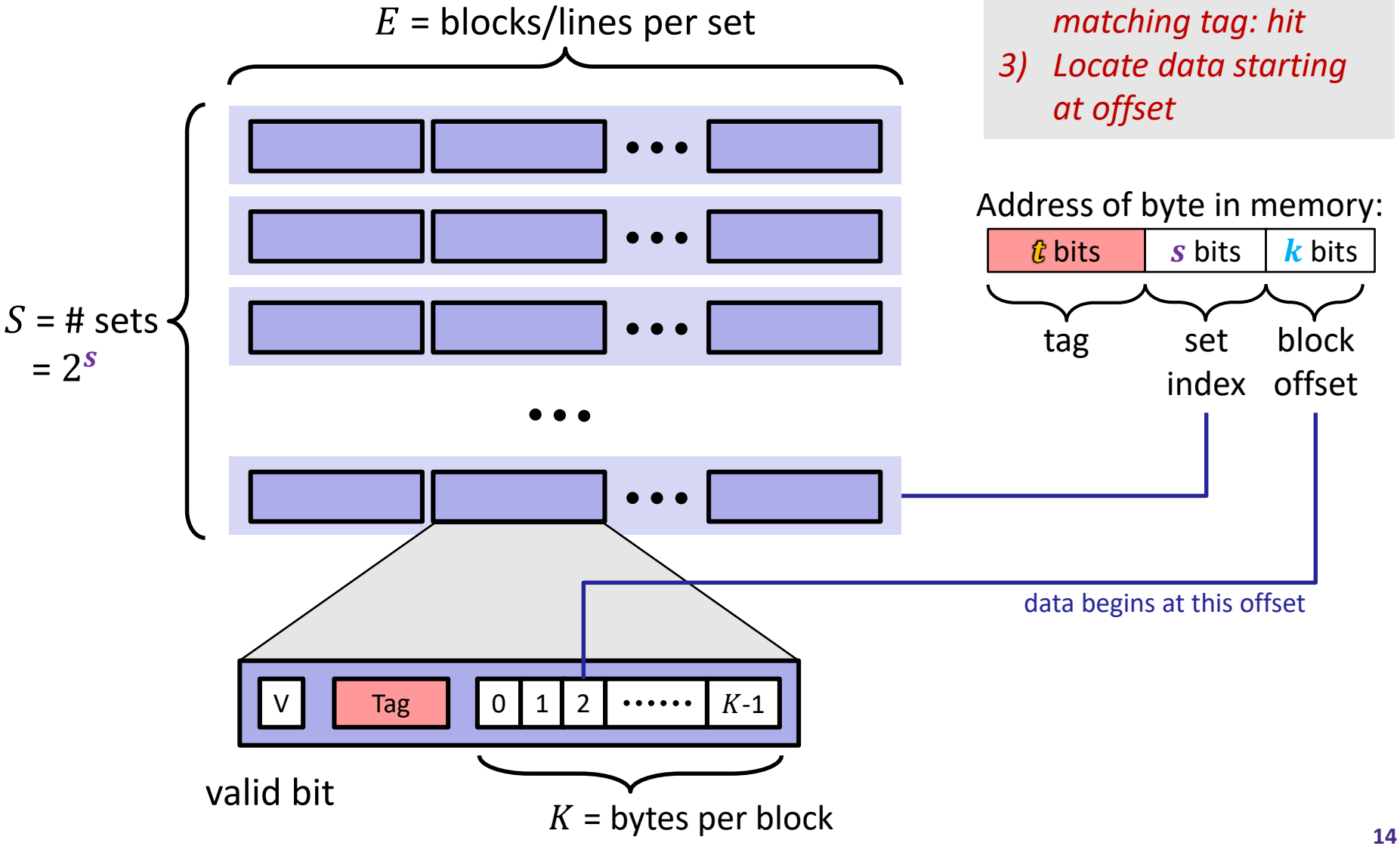
Example Cache Parameters Problem

- 4 KiB address space, 125 cycles to go to memory. Fill in the following table:

Cache Size	256 B
Block Size	32 B
Associativity	2-way
Hit Time	3 cycles
Miss Rate	20%
Tag Bits	
Index Bits	
Offset Bits	
AMAT	

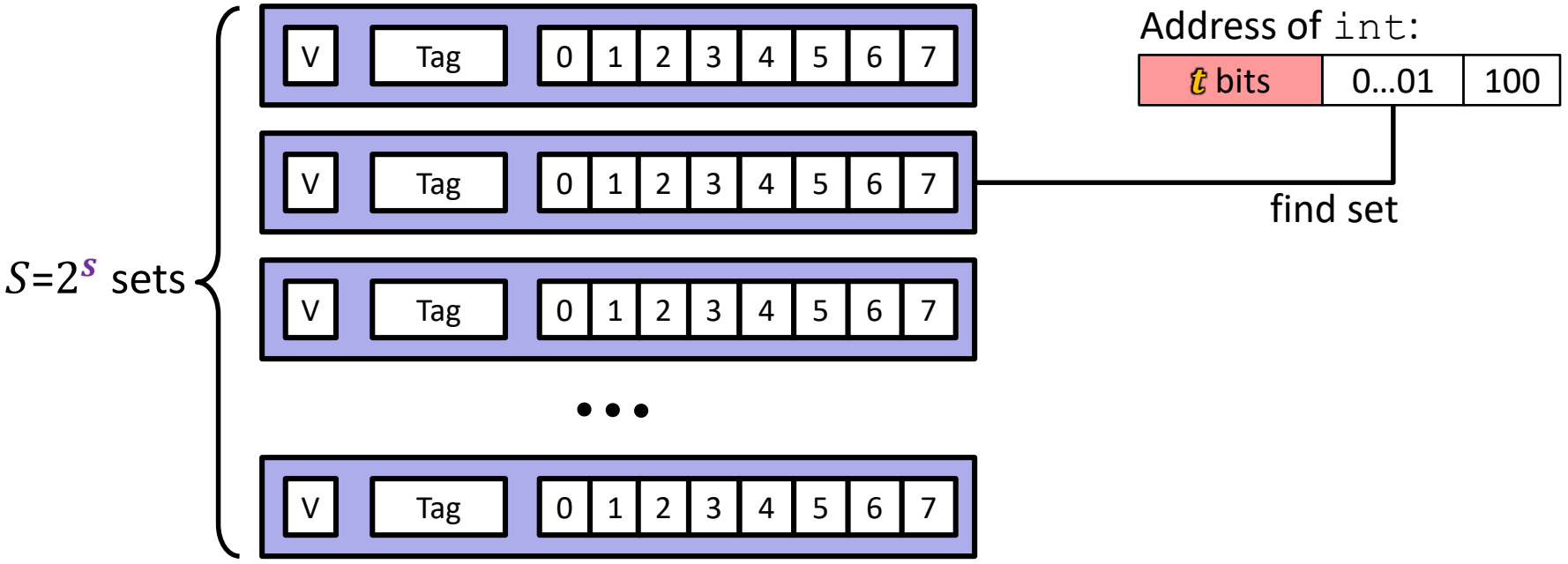
Cache Read

1) *Locate set*
2) *Check if any line in set is valid and has matching tag: hit*
3) *Locate data starting at offset*



Example: Direct-Mapped Cache (E = 1)

Direct-mapped: One line per set
Block Size K = 8 B



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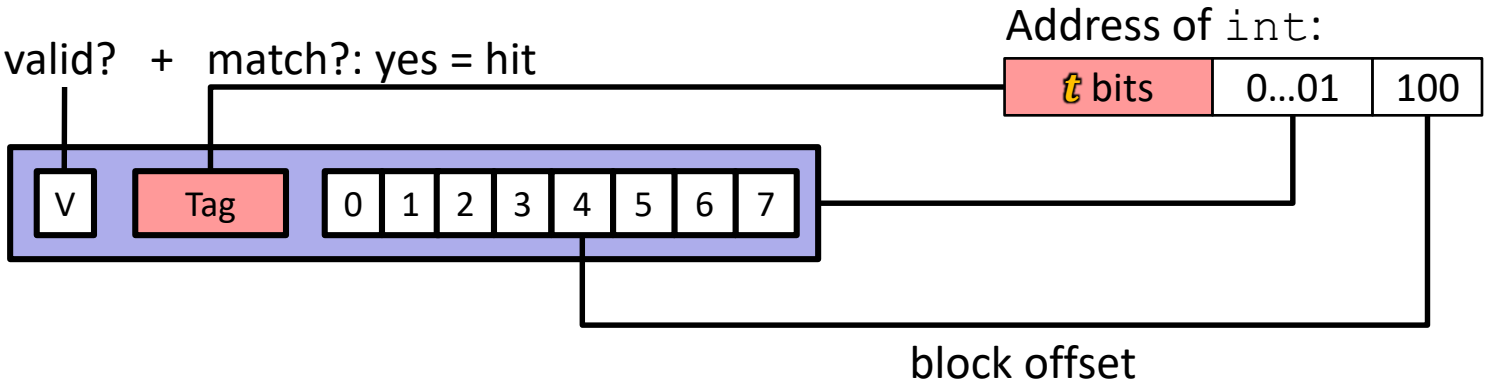

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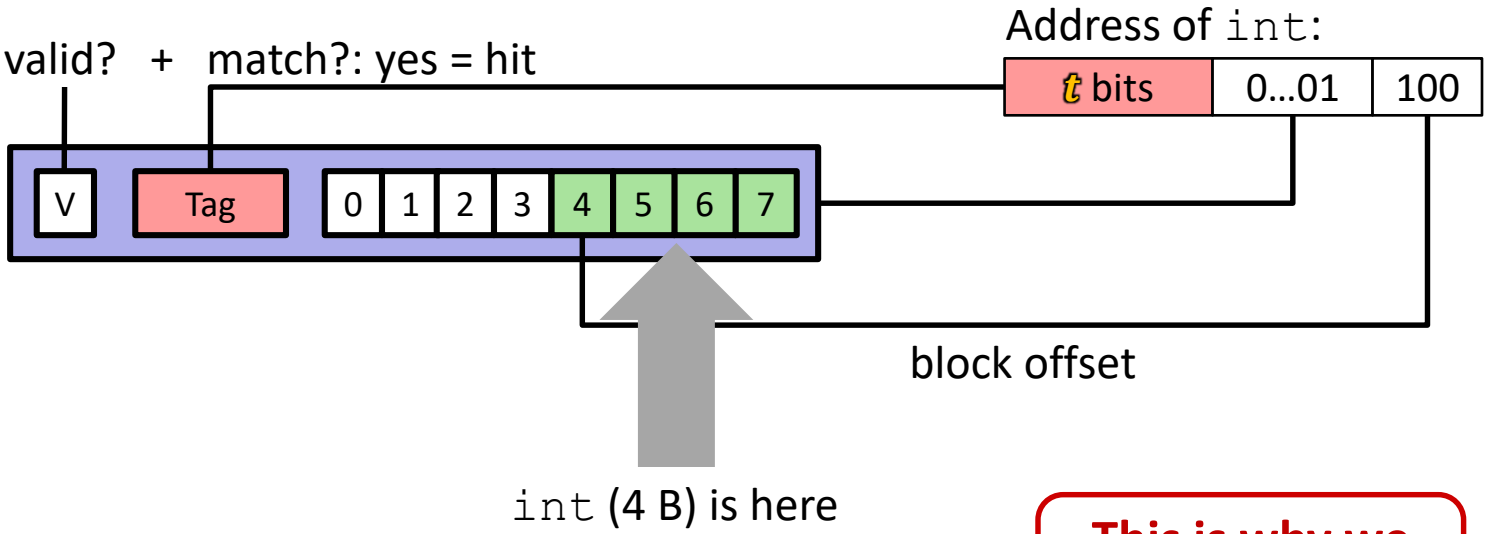
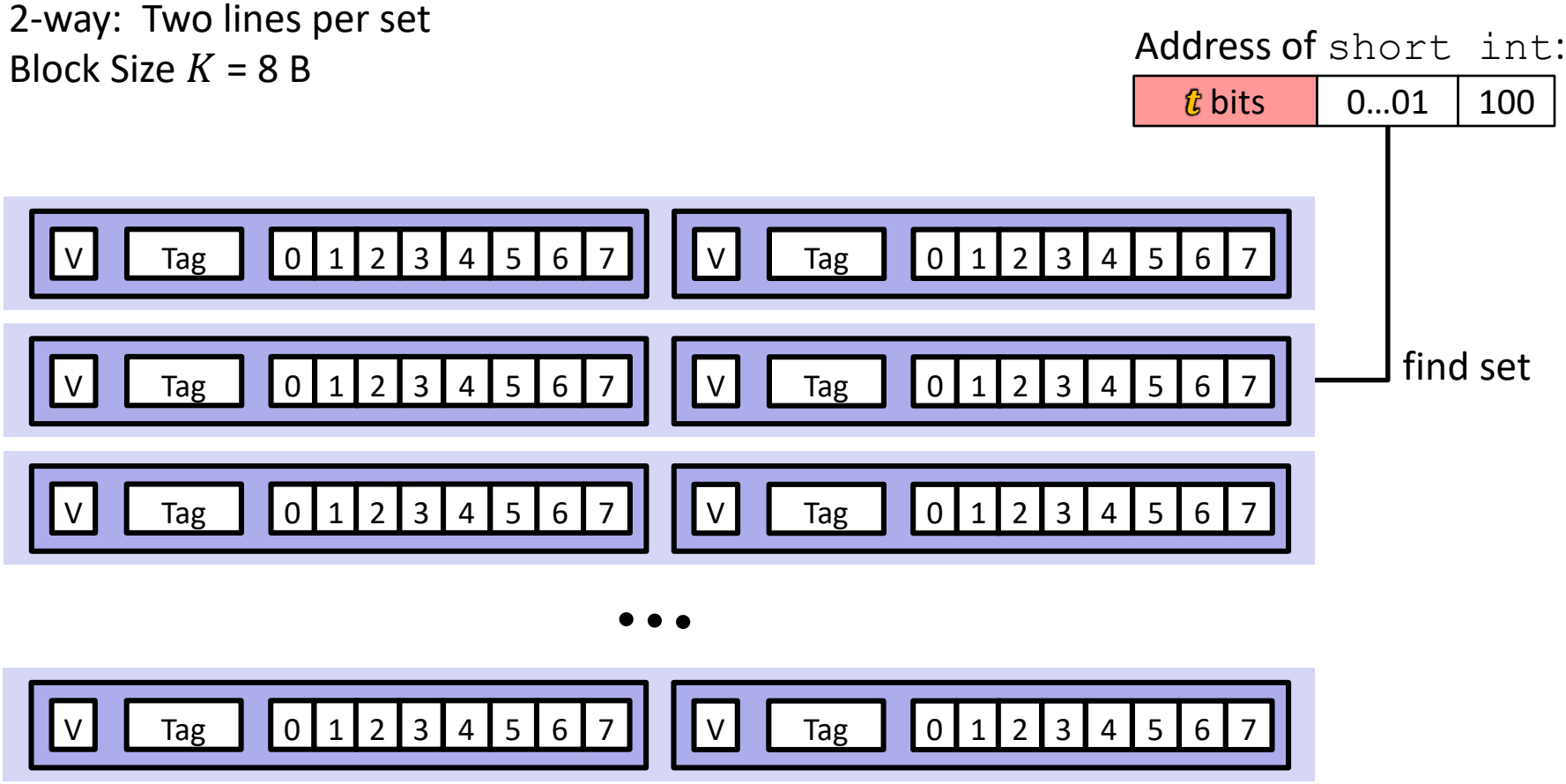


This is why we want alignment!

No match? Then old line gets evicted and replaced

Example: Set-Associative Cache (E = 2)

2-way: Two lines per set
Block Size K = 8 B



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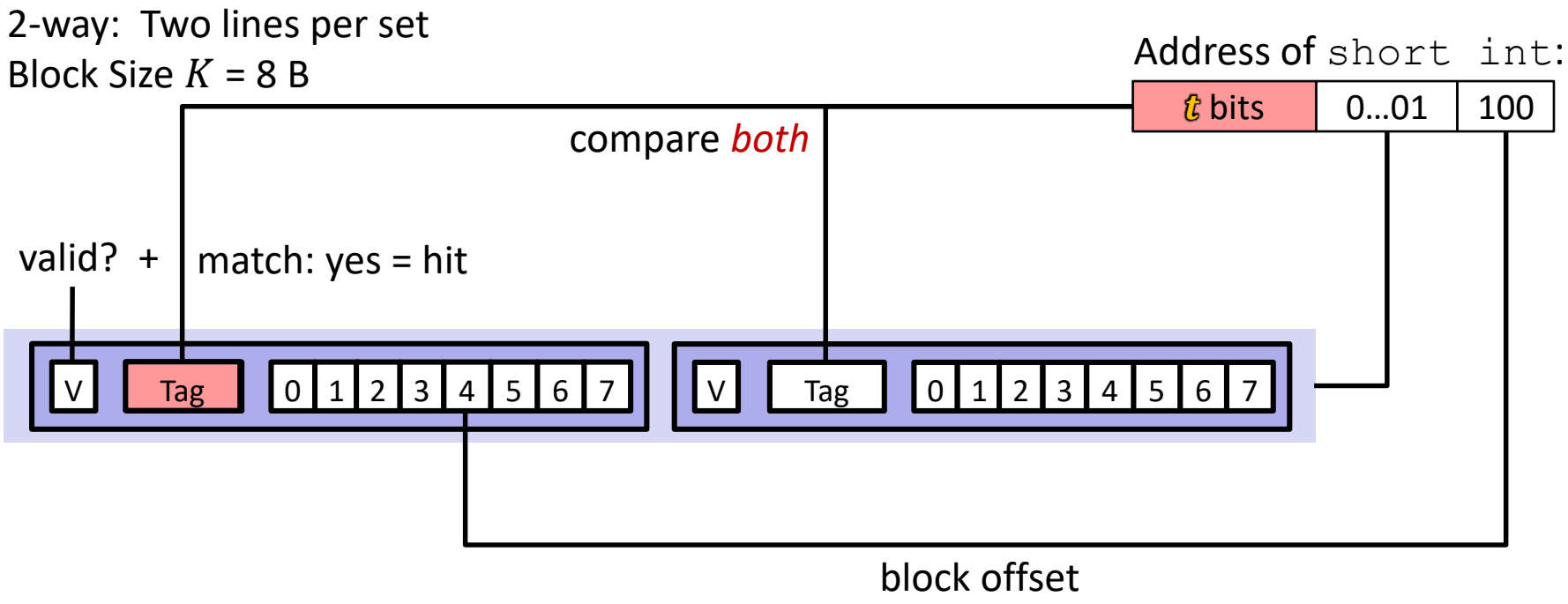

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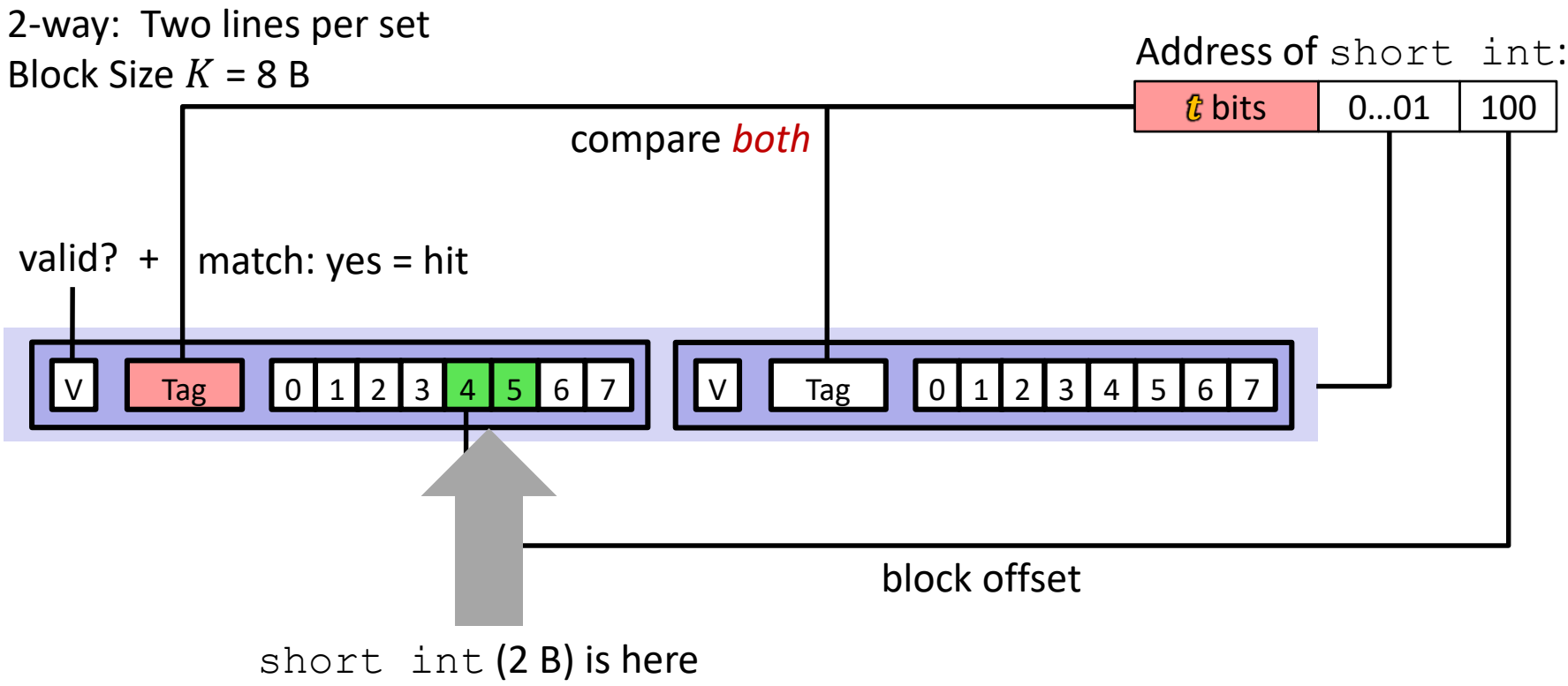

No match?

- One line in set is selected for eviction and replacement
- Replacement policies: random, least recently used (LRU), …

Types of Cache Misses: 3 C's!

- Compulsory (cold) miss
  - Occurs on first access to a block
- Conflict miss
  - Conflict misses occur when the cache is large enough, but multiple data objects all map to the same slot
    - *e.g.* referencing blocks 0, 8, 0, 8, ... could miss every time
  - Direct-mapped caches have more conflict misses than E-way set-associative (where $E > 1$)
- Capacity miss
  - Occurs when the set of active cache blocks (the *working set*) is larger than the cache (just won't fit, even if cache was *fully-associative*)
  - **Note:** *Fully-associative* only has Compulsory and Capacity misses

Example Code Analysis Problem

- Assuming the cache starts cold (all blocks invalid) and `sum`, `i`, and `j` are stored in registers, calculate the **miss rate**:
  - m = 12 bits, C = 256 B, K = 32 B, E = 2

```
#define SIZE 8
long ar[SIZE][SIZE], sum = 0;  // &ar=0x800
for (int i = 0; i < SIZE; i++)
   for (int j = 0; j < SIZE; j++)
      sum += ar[i][j];
```