

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Arrays

CSE 351 Winter 2018

**Instructor:**  
Mark Wyse

**Teaching Assistants:**  
Kevin Bi  
Parker DeWilde  
Emily Furst  
Sarah House  
Waylon Huang  
Vinny Palaniappan

WHY DO YOU LIKE FUNCTIONAL PROGRAMMING SO MUCH? WHAT DOES IT ACTUALLY GET YOU?

TAIL RECURSION IS ITS OWN REWARD.

<http://xkcd.com/1270/>

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Administrative

- ❖ Lab 2 due tonight by 11:59 pm!
- ❖ Homework 3 due next Friday (2/9)
- ❖ **Midterm (Monday 2/5)**
  - ID check, so come at 5pm
  - **Bring your UW Student ID (Husky Card)**
  - **Review session 2:00-4:00pm on Saturday (2/3) in EEB 125**

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Roadmap

**C:**

```
car *c = malloc(sizeof(car));
c->miles = 100;
c->gals = 17;
float mpg = get_mpg(c);
free(c);
```

**Java:**

```
Car c = new Car();
c.setMiles(100);
c.setGals(17);
float mpg = c.getMpg();
```

Memory & data  
Integers & floats  
x86 assembly  
Procedures & stacks  
Executables

**Arrays & structs**  
Memory & caches  
Processes  
Virtual memory  
Memory allocation  
Java vs. C

**Assembly language:**

```
get_mpg:
    dqz %rdi, %rdi
    mov %rsi, %rdi
    ...
    dqz %rdi, %rdi
    ret
```

**Machine code:**

```
01110100000011000
100010100000010000000010
1000100111000010
1100000000000000000011111
```

**OS:**

**Computer system:**

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Data Structures in Assembly

- ❖ **Arrays**
  - **One-dimensional**
  - **Multi-dimensional (nested)**
  - **Multi-level**
- ❖ **Structs**
  - **Alignment**
- ❖ **Unions**

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Allocation

- ❖ **Basic Principle**
  - $T A[N]$ ;  $\rightarrow$  array of data type  $T$  and length  $N$
  - *Contiguously* allocated region of  $N * \text{sizeof}(T)$  bytes
  - Identifier  $A$  returns address of array (type  $T^*$ )

**char msg[12];**

**int val[5];**

**double a[3];**

**char \*p[3];**  
(or **char\* p[3];**)

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Access

- ❖ **Basic Principle**
  - $T A[N]$ ;  $\rightarrow$  array of data type  $T$  and length  $N$
  - Identifier  $A$  returns address of array (type  $T^*$ )

**int x[5];**

Reference	Type	Value
x[4]	int	5
x	int*	a
x+1	int*	a + 4
&x[2]	int*	a + 8
x[5]	int	?? (whatever's in memory at addr a+20)
*(x+1)	int	7
x+i	int*	a + 4*i

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Example

```
typedef int zip_dig[5];
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig uw = { 9, 8, 1, 9, 5 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

initialization

♦ typedef: Declaration "zip\_dig uw" equivalent to "int uw[5]"

7

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Example

```
typedef int zip_dig[5];
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig uw = { 9, 8, 1, 9, 5 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

zip\_dig cmu; 16 20 24 28 32 36

zip\_dig uw; 36 40 44 48 52 56

zip\_dig ucb; 56 60 64 68 72 76

♦ Example arrays happened to be allocated in successive 20 byte blocks

- Not guaranteed to happen in general

8

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Accessing Example

```
typedef int zip_dig[5];
```

```
int get_digit(zip_dig z, int digit)
{
    return z[digit];
}
```

```
get_digit:
    movl (%rdi,%rsi,4), %eax # z[digit]
```

- Register %rdi contains starting address of array
- Register %rsi contains array index
- Desired digit at %rdi+4\*%rsi, so use memory reference (%rdi,%rsi,4)

9

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Referencing Examples

```
typedef int zip_dig[5];
```

Reference	Address	Value	Guaranteed?
uw[3]			
uw[6]			
uw[-1]			
cmu[15]			

♦ No bounds checking

♦ Example arrays happened to be allocated in successive 20 byte blocks

- Not guaranteed to happen in general

10

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Loop Example

```
typedef int zip_dig[5];
```

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

$zi = 10 \cdot 0 + 9 = 9$   
 $zi = 10 \cdot 9 + 8 = 98$   
 $zi = 10 \cdot 98 + 1 = 981$   
 $zi = 10 \cdot 981 + 9 = 9819$   
 $zi = 10 \cdot 9819 + 5 = 98195$

11

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Loop Example

zip\_dig uw; 36 40 44 48 52 56

♦ Original:

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

♦ Transformed:

- Eliminate loop variable i, use pointer zend instead
- Convert array code to pointer code
  - Pointer arithmetic on z
- Express in do-while form (no test at entrance)

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 5;
    do {
        zi = 10 * zi + *z;
        z++;
    } while (z < zend);
    return zi;
}
```

address just past 5<sup>th</sup> digit

Increments by 4 (size of int)

12

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Array Loop Implementation

gcc with -O1

- Registers:
  - %rdi z
  - %rax zi
  - %rcx zend
- Computations
  - 10\*zi + \*z
  - z++

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 5;
    do {
        zi = 10 * zi + *z;
        z++;
    } while (z < zend);
    return zi;
}
```

```
# %rdi = z
leaq 20(%rdi),%rcx    # %rcx = zend = z + 5
movl $0,%eax         # %rax = zi = 0
.L17:
leal (%rax,%rax,4),%edx # %rdx = zi + 4*zi = 5*zi
movl (%rdi),%eax     # %rax = *z
leal (%rax,%rdx,2),%eax # %rax = *z + 2[5*zi] = *z + 10*zi
addq $4,%rdi        # z++ (pointer arithmetic)
cmpq %rdi,%rcx     # zend - z
jne .L17            # if != 0, goto Loop
```

13

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## C Details: Arrays and Pointers

- Arrays are (almost) identical to pointers
  - char \*string and char string[] are nearly identical declarations
  - Differ in subtle ways: initialization, sizeof(), etc.
- An array variable looks like a pointer to the first (0<sup>th</sup>) element
  - ar[0] same as \*ar; ar[2] same as \*(ar+2)
- An array variable is read-only (no assignment)
  - Cannot use "ar = <anything>"

14

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## C Details: Arrays and Functions

- Declared arrays only allocated while the scope is valid:
 

```
char* foo() {
    char string[32]; ...;
    return string;
}
```

**BAD!**
- An array is passed to a function as a pointer:
  - Array size gets lost!

```
int foo(int ar[], unsigned int size) {
    ... ar[size-1] ...
}
```

Really int \*ar  
Must explicitly pass the size!

15

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Data Structures in Assembly

- Arrays
  - One-dimensional
  - Multi-dimensional (nested)
  - Multi-level
- Structs
  - Alignment
- Unions

16

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Nested Array Example

```
typedef int zip_dig[5];
```

```
zip_dig sea[4] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

Remember, T A[N] is an array with elements of type T, with length N

What is the layout in memory?

same as:  
int sea[4][5];

17

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Nested Array Example

```
typedef int zip_dig[5];
```

```
zip_dig sea[4] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

Remember, T A[N] is an array with elements of type T, with length N

Row 0 Row 1 Row 2 Row 3

9	8	1	9	5	9	8	1	0	5	9	8	1	0	3	9	8	1	1	5
76				96					116					136					156

sea[3][2];

- "Row-major" ordering of all elements
- Elements in the same row are contiguous
- Guaranteed (in C)

18

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Two-Dimensional (Nested) Arrays

- Declaration:  $\mathbf{T} \ A[R][C]$ ;
  - 2D array of data type  $\mathbf{T}$
  - $R$  rows,  $C$  columns
  - Each element requires  $\text{sizeof}(\mathbf{T})$  bytes
- Array size?
  - $R * C * \text{sizeof}(\mathbf{T})$  bytes

$A[0][0]$	...	$A[0][C-1]$
$\vdots$		$\vdots$
$A[R-1][0]$	...	$A[R-1][C-1]$

19

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Two-Dimensional (Nested) Arrays

- Declaration:  $\mathbf{T} \ A[R][C]$ ;
  - 2D array of data type  $\mathbf{T}$
  - $R$  rows,  $C$  columns
  - Each element requires  $\text{sizeof}(\mathbf{T})$  bytes
- Array size:
  - $R * C * \text{sizeof}(\mathbf{T})$  bytes
- Arrangement: **row-major** ordering

```
int A[R][C];
```

A	...	A	A	...	A	...	A	A
[0]		[0]	[1]		[1]		[R-1]	[R-1]
[0]		[C-1]	[0]		[C-1]		[0]	[C-1]

20

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Nested Array Row Access

- Row vectors
  - Given  $\mathbf{T} \ A[R][C]$ ,
    - $A[i]$  is an array of  $C$  elements ("row  $i$ ")
    - Each element of type  $\mathbf{T}$  requires  $K$  bytes
    - $A$  is address of array
    - Starting address of row  $i = A + i * (C * K)$

```
int A[R][C];
```

A[0]			...	A[1]			...	A[R-1]		
A	...	A		A	...	A		A	...	A
[0]		[0]		[1]		[1]		[R-1]		[R-1]
[0]		[C-1]		[0]		[C-1]		[0]		[C-1]

21

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Nested Array Row Access Code

```
int* get_sea_zip(int index)
{
    return sea[index];
}
```

```
int sea[4][5] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

- What data type is  $sea[index]$ ?
- What is its starting address?

```
get_sea_zip(int):
    movlq %rdi, %rdi
    leaq (%rdi,%rdi,4), %rdx
    leaq 0,(%rdx,4), %rax
    addq %sea, %rax
    ret
sea:
    .long 9
    .long 8
    .long 1
    .long 9
    .long 5
    .long 9
    .long 9
    .long 8
    ...
```

22

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Nested Array Row Access Code

```
int* get_sea_zip(int index)
{
    return sea[index];
}
```

```
int sea[4][5] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

- What data type is  $sea[index]$ ?
- What is its starting address?

```
# %rdi = index
leaq (%rdi,%rdi,4), %rax
leaq sea(,%rax,4), %rax
```

Translation?

23

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2018

## Nested Array Row Access Code

```
int* get_sea_zip(int index)
{
    return sea[index];
}
```

```
int sea[4][5] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

```
# %rdi = index
leaq (%rdi,%rdi,4), %rax # 5 * index
leaq sea(,%rax,4), %rax # sea + (20 * index)
```

- Row Vector
  - $sea[index]$  is array of 5 ints
  - Starting address =  $sea + 20 * index$
- Assembly Code
  - Computes and returns address
  - Compute as:  $sea + 4 * (index + 4 * index) = sea + 20 * index$

24

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2016

## Nested Array Element Access

- Array Elements
  - $A[i][j]$  is element of type  $T$ , which requires  $K$  bytes
  - Address of  $A[i][j]$  is

```
int A[R][C];
```

25

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2016

## Nested Array Element Access

- Array Elements
  - $A[i][j]$  is element of type  $T$ , which requires  $K$  bytes
  - Address of  $A[i][j]$  is
 
$$A + i*(C*K) + j*K == A + (i*C + j)*K$$

```
int A[R][C];
```

26

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2016

## Nested Array Element Access Code

```
int get_sea_digit(int index, int digit)
{
    return sea[index][digit];
}

int sea[4][5] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

```
leaq (%rdi,%rdi,4), %rax # 5*index
addl %rax,%rsi # 5*index+digit
movl sea(,%rsi,4), %eax # *(sea + 4*(5*index+digit))
```

- Array Elements
  - $sea[index][digit]$  is an `int` (`sizeof(int)=4`)
  - Address =  $sea + 5*4*index + 4*digit$
- Assembly Code
  - Computes address as:  $sea + ((index*4*5) + digit)*4$
  - `movl` performs memory reference

27

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2016

## Strange Referencing Examples

```
typedef int zip_dig[5];
```

```
zip_dig sea[4];
```

Reference	Address	Value	Guaranteed?
<code>sea[3][3]</code>			
<code>sea[2][5]</code>			
<code>sea[2][-1]</code>			
<code>sea[4][-1]</code>			
<code>sea[0][19]</code>			
<code>sea[0][-1]</code>			

- Code does not do any bounds checking
- Ordering of elements within array guaranteed

28

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2016

## Data Structures in Assembly

- Arrays
  - One-dimensional
  - Multi-dimensional (nested)
  - Multi-level
- Structs
  - Alignment
- Unions

29

UNIVERSITY of WASHINGTON L13: Arrays CSE361, Winter 2016

## Multi-Level Array Example

### Multi-Level Array Declaration(s):

```
int cmu[5] = { 1, 5, 2, 1, 3 };
int uw[5] = { 9, 8, 1, 9, 5 };
int ucb[5] = { 9, 4, 7, 2, 0 };
int* univ[3] = {uw, cmu, ucb};
```

Is a multi-level array the same thing as a 2D array? **NO**

### 2D Array Declaration:

```
zip_dig univ2D[3] = {
{ 9, 8, 1, 9, 5 },
{ 1, 5, 2, 1, 3 },
{ 9, 4, 7, 2, 0 }
};
```

One array declaration = one contiguous block of memory

30

UNIVERSITY of WASHINGTON L13: Arrays CSE351, Winter 2018

## Multi-Level Array Example

```

int cmu[5] = { 1, 5, 2, 1, 3 };
int uw[5] = { 9, 8, 1, 9, 5 };
int ucb[5] = { 9, 4, 7, 2, 0 };
int* univ[3] = {uw, cmu, ucb};

```

- Variable univ denotes array of 3 elements
- Each element is a pointer
  - 8 bytes each
- Each pointer points to array of ints

Note: this is how Java represents multi-dimensional arrays

31

UNIVERSITY of WASHINGTON L13: Arrays CSE351, Winter 2018

## Element Access in Multi-Level Array

```

int get_univ_digit
(int index, int digit)
{
    return univ[index][digit];
}

```

```

sllq $2, %rsi # rsi = 4*digit
addq univ(%rdi,8), %rsi # p = univ[index] + 4*digit
movl (%rsi), %eax # return *p
ret

```

- Computation
  - Element access Mem[Mem[univ+8\*index]+4\*digit]
  - Must do **two memory reads**
    - First get pointer to row array
    - Then access element within array
  - But allows inner arrays to be different lengths (not in this example)

32

UNIVERSITY of WASHINGTON L13: Arrays CSE351, Winter 2018

## Array Element Accesses

### Nested array

```

int get_sea_digit
(int index, int digit)
{
    return sea[index][digit];
}

```

### Multi-level array

```

int get_univ_digit
(int index, int digit)
{
    return univ[index][digit];
}

```

Access looks the same, but it isn't:

Mem[sea+20\*index+4\*digit]      Mem[Mem[univ+8\*index]+4\*digit]

33

UNIVERSITY of WASHINGTON L13: Arrays CSE351, Winter 2018

## Strange Referencing Examples

Reference	Address	Value	Guaranteed?
univ[2][3]			
univ[1][5]			
univ[2][-2]			
univ[3][-1]			
univ[1][12]			

- C code does not do any bounds checking
- Location of each lower-level array in memory is *not* guaranteed

34

UNIVERSITY of WASHINGTON L13: Arrays CSE351, Winter 2018

## Summary

- Contiguous allocations of memory
- No bounds checking** (and no default initialization)
- Can usually be treated like a pointer to first element
- int** a[4][5]; → array of arrays
  - all levels in one contiguous block of memory
- int\*** b[4]; → array of pointers to arrays
  - First level in one contiguous block of memory
  - Each element in the first level points to another "sub" array
  - Parts anywhere in memory

35