## CSE 351 Section 3 - Integers, FP, and Assembly

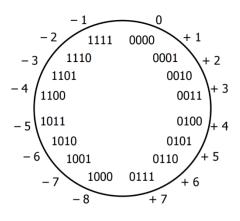
Welcome back to section! We're happy that you're here ©

### **Signed Integers with Two's Complement**

Two's complement is the standard for representing signed integers:

- The most significant bit (MSB) has a negative value; all others have positive values (same as unsigned)
- Binary addition is performed the same way for signed and unsigned
- The bit representation for the negative (additive inverse) of a two's complement number can be found by:

flipping all the bits and adding 1 (i.e. -2 = 2 + 1).



The "number wheel" showing the relationship between 4-bit numerals and their Two's Complement interpretations is shown on the right:

- The largest number is 7 whereas the smallest number is -8
- There is a nice symmetry between numbers and their negative counterparts except for -8

**Exercises**: (assume 8-bit integers)

1) How do you represent (if possible) the following numbers: 39, -39, 127? Answer in binary

Unsigned:	Two's Complement:
39:	39:
-39:	-39:
127:	127:

2) Compute the following sums in binary using your Two's Complement answers above. Answer in unsigned hex

	The second secon
a. 39 -> 0b +(-39) -> 0b	<b>b</b> . 127 -> 0b + (-39)-> 0b
0x<- 0b	0x<-0b
c. 39 -> 0b +(-127)-> 0b	<b>d</b> . 127 -> 0b + 39 -> 0b
0x<- 0b	0x<- 0b

3) Interpret each of your answers above and indicate whether or not overflow has occurred.

interpret each of your answers above and indicate whether of not overnow has occurred.		
<b>a.</b> 39 + (-39)	<b>b.</b> 127 + (-39)	
Unsigned:	Unsigned:	
Two's Complement:	Two's Complement:	
c. 39 + (-127)	<b>d.</b> 127 + 39	
Unsigned:	Unsigned:	
Two's Complement:	Two's Complement:	

### **Goals of Floating Point**

Representation should include: [1] a large range of values (both very small and very large numbers), [2] a high amount of precision, and [3] real arithmetic results ( $e.g. \infty$  and NaN).

### **IEEE 754 Floating Point Standard**

The <u>value</u> of a real number can be represented in scientific binary notation as:

Value = 
$$(-1)^{sign} \times Mantissa_2 \times 2^{Exponent} = (-1)^S \times 1.M_2 \times 2^{E-bias}$$

The binary representation for floating point values uses three fields:

- **S**: encodes the *sign* of the number (0 for positive, 1 for negative)
- **E**: encodes the *exponent* in **biased notation** with a bias of  $2^{w-1}-1$
- **M**: encodes the *mantissa* (or *significand*, or *fraction*) stores the fractional portion, but does not include the implicit leading 1.

	S	E	M
float	1 bit	8 bits	23 bits
double	1 bit	11 bits	52 bits

How a float is interpreted depends on the values in the exponent and mantissa fields:

E	M	Meaning
0	anything	denormalized number (denorm)
1-254	anything	normalized number
255	zero	infinity (∞)
255	nonzero	not-a-number (NaN)

#### **Exercises:**

4) Convert the decimal number 1.25 into single precision floating point representation:

5) What are the decimal values of the following floats?

0x80000000

0xFF94BEEF

0x41180000

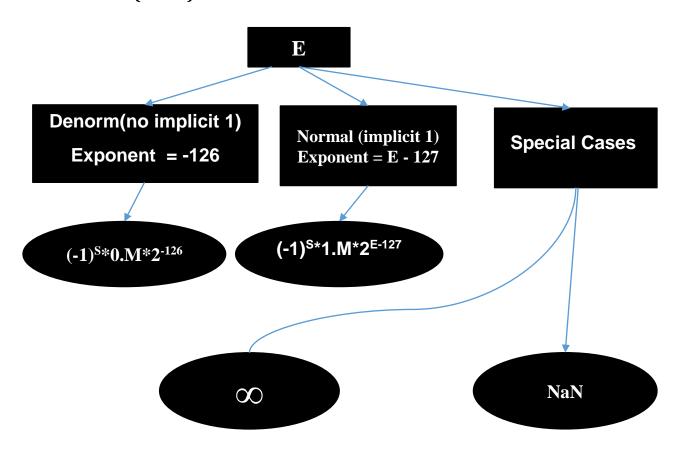
### **Floating Point Mathematical Properties**

- Not <u>associative</u>:  $(2 + 2^{50}) 2^{50} != 2 + (2^{50} 2^{50})$
- Not <u>distributive</u>:  $100 \times (0.1 + 0.2) != 100 \times 0.1 + 100 \times 0.2$
- Not <u>cumulative</u>:  $2^{25} + 1 + 1 + 1 + 1 = 2^{25} + 4$

#### **Exercises:**

- 6) Based on floating point representation, explain why each of the three statements above occurs.
- 7) If x and y are variable type float, give two *different* reasons why (x+2\*y)-y == x+y might evaluate to false.

IEEE 754 Float (32 bit) Flowchart



# x86\_64 Assembly

- These are the actual instructions which are running on your computer
- In practice, it's another language you get to learn and become familiar with
- Recall:

- Registers hold 64 bits, and are names things like rax, rbx, rcx, rdx, rdi, rsi, rbp, rsp. In x86-64 assembly, they are prefixed with "%".
- Instructions consist of an opcode, and then multiple operands, e.g.
  - movq %rdi, %rbp
  - This moves (copies) the 64 bit contents of register rdi into register rbp
- Destination registers are always on the <u>Right Hand Side</u> (opposite of assignment statements in C, Java, Python, Ruby, C++, C#, Bash, Scala, and most any other language you can think of)
- In order to follow (dereference) a pointer value contained in a register, use parentheses, e.g.
  - movq %rdi, (%rbp)
  - This moves (copies) the 64 bit contents of rdi into the memory location which rbp points to
- You may only use one set of parens per instruction (an instruction is either a load or a store, but not both)
- Immediate (constant) operands are denoted with "\$" (e.g. movq \$13, %rax)

### The Swap Example (again)

In class, we discussed a series of instructions to swap two locations in memory. Below are two similar sequences, except each has at least one bug. However, buggy assembly doesn't mean the program crashes; it just means it does something different from what we want. Explain what each sequence of instructions actually does, and fix it to swap the two intended locations. It may help you to draw a picture.

```
  movq %rdx, (%rdi)
  movq %rax, (%rsi)
  movq (%rdi), %rax
  movq (%rsi), %rdx
```

```
2. movq (%rdi), %rax
movq %rdx, (%rdi)
movq (%rsi), %rdx
movq %rax, (%rsi)
```