

1. Number Representation – Integers (13 Autumn)

- a) Explain why we have a Carry-Flag and an Overflow-Flag in x86 condition codes. What is the difference between the two? (Explain in at most two sentences.)

The carry flag is used for unsigned numbers and indicates a carry-out of 1 during addition from the most-significant-bit. The overflow flag applies to signed arithmetic and indicates that the addition yielded a number that was too large a positive or too small a negative value.

- b) Add **11011001** and **01100011** as two's complement 8-bit integers & convert the result to decimal notation.

$$\begin{array}{r} 11011001 = -39 \\ + 01100011 = +99 \\ \hline 00111100 = +60 \end{array}$$

- c) Convert your answer from the previous problem to a 2-digit hex value.
 $60 = 0x3c$

2. Floating-Point Number Representation (based on 12 Spring)

A new pizzeria has opened on the Ave. It is mysteriously called "Pizza 0x40490FDB". Given that you are in CSE351, you have a hunch what the mystery might be. Consider the string of hex digits as a 32-bit IEEE floating point number (8-bit exponent and 23-bit fraction).

- a) Fill in the hexadecimal digits in the bytes below and then translate them to individual bits.

8 hex digits in 4 bytes: **40 49 0F DB**

32 bits: **01000000 01001001 00001111 11011011**

- b) Is this number positive or negative?

Positive

- c) What is the exponent?
(*exponents are biased in this representation so make sure to make this adjustment*)

$$1000\ 0000 \quad 128\text{-Bias} = 128 - 127 = 1$$

- d) What is the significand in binary?
(*only use the first 7 bits of the fraction, ignore the lower-order 16 bits*)

$$\text{frac} = 1001001\dots011 \quad \text{So significand} = 1.1001001$$

e) What is the value of the number in binary?

$$1.1001001 * 2^1 = 11.001001 \text{ (shifted the binary point left by 1)}$$

f) What is the decimal number represented?
(only show two decimal digits after the decimal point)

$$11.001001 = 2 + 1 + .125 + .015625 = 3.14...$$

g) What is the pizzeria's mystery name?

Pizza Pi

3. Arrays – C to Assembly (based on 14 Autumn)

Given the following C function:

```
long sum_pair(long *z, long index) {  
    return z[index] + z[index + 1];  
}
```

Write **x86-64** assembly code for this function here. You can assume that **z** points to an array of 16 elements, and $0 \leq \mathbf{index} < 15$.

Comments are not required but could help for partial credit.

```
sum_pair:  
    movq    (%rdi,%rsi,8), %rax  
    addq   8(%rdi,%rsi,8), %rax  
    ret
```

4. Assembly and C (15 Winter)

Consider the following x86-64 assembly and C code:

```
<do_something>:
    xor    %rax,%rax
    cmp    $0x0,%rsi
    jle   <end>
    sub    $0x1,%rsi

<loop>:
    lea   (%rdi,%rsi, 2 ),%rdx
    add   (%rdx),%ax
    sub   $0x1,%rsi
    jns   <loop>

<end>:
    ret

short do_something(short* a, int len) {
    short result = 0;
    for (int i = len - 1; i >= 0; i--) {
        result += a[i] ;
    }
    return result;
}
```

a) Both code segments are implementations of the unknown function `do_something`. Fill in the missing blanks in both versions. (Hint: `%rax` and `%rdi` are used for `result` and `a` respectively. `%rsi` is used for both `len` and `i`)

b) Briefly describe the value that `do_something` returns and how it is computed. Use only variable names from the C version in your answer.

do_something returns the sum of the shorts pointed to by a. It does so by traversing the array backwards.

5. Stack Discipline (14 Spring)

a)

Memory address on stack line)	Value (8 bytes per line)	
0x7fffffffad0	Return address back to main	<-%rsp points here at start of procedure
0x7fffffffac8	1 st of 3 local variables on stack (argument a= 144)	
0x7fffffffac0	2nd of 3 local variables on stack (argument b = 64)	
0x7fffffffab8	3rd of 3 local variables on stack (unused)	
0x7fffffffab0	Return address back to gcd(144, 64)	
0x7fffffffaa8	1st of 3 local variables on stack (argument a = 64)	
0x7fffffffaa0	2nd of 3 local variables on stack (argument b = 16)	
0x7fffffff998	3rd of 3 local variables on stack (unused)	
0x7fffffff990	Return address back to gcd(64,16)	
0x7fffffff988	1st of 3 local variables on stack (argument a = 16)	
0x7fffffff980	2nd of 3 local variables on stack (argument b = 0)	
0x7fffffff978	3rd of 3 local variables on stack (unused)	<-%rsp at "return a" in 3 rd recursive call
0x7fffffff970		

b) How many total bytes of local stack space are created in each frame (in decimal)?

32 (24 allocated explicitly and 8 for the return address.)

c) When the function begins, where are the arguments (a, b) stored?

They are stored in the registers %rdi and %rsi, respectively.

d) From a memory-usage perspective, why are iterative algorithms generally preferred over recursive algorithms?

Recursive algorithm continue to grow the stack for the maximum number of recursions which may be hard to estimate.