Name: 1  NUMBER REPRESENTATION(10 POINTS)

Sp15 Midterm Q1

1  Number Representation(10 points)

Let \( x=0xE \) and \( y=0x7 \) be integers stored on a machine with a word size of 4\text{bits}. Show your work with the following math operations. The answers—including truncation—should match those given by our hypothetical machine with 4-bit registers.

A. (2pt) What hex value is the result of adding these two numbers?

B. (2pt) Interpreting these numbers as unsigned ints, what is the decimal result of adding \( x + y \)?

C. (2pt) Interpreting \( x \) and \( y \) as two’s complement integers, what is the decimal result of computing \( x - y \)?

D. (2pt) In one word, what is the phenomenon happening in 1B?

E. (2pt) Circle all statements below that are TRUE on a 32-bit architecture:

- It is possible to lose precision when converting from an int to a float.
- It is possible to lose precision when converting from a float to an int.
- It is possible to lose precision when converting from an int into a double.
- It is possible to lose precision when converting from a double into an int.
Sp16 Midterm Q1

Now assume that our fictional machine with 6-bit integers also has a 6-bit IEEE-like floating point type, with 1 bit for the sign, 3 bits for the exponent (exp) with a bias of 3, and 2 bits to represent the mantissa (frac), not counting implicit bits.

(d) If we reinterpret the bits of our binary value from above as our 6-bit floating point type, what value, in decimal, do we get?

\[
\begin{array}{cccccc}
1 & 1 & 0 & 1 & 0 & 1 \\
sign & exp & frac & \\
\end{array}
\]

(e) If we treat 110101₂ as a signed integer, as we did in (b), and then cast it to a 6-bit floating point value, do we get the correct value in decimal? (That is, can we represent that value in our 6-bit float?) If yes, what is the binary representation? If not, why not? (and in that case you do not need to determine the rounded bit representation)

(f) Assuming the same rules as standard IEEE floating point, what value (in decimal) does the following represent?

\[
\begin{array}{cccccc}
0 & 0 & 0 & 0 & 0 & 0 \\
sign & exp & frac & \\
\end{array}
\]
4. Pointers, Memory & Registers (14 points)

Assuming a 64-bit x86-64 machine (little endian), you are given the following variables and initial state of memory (values in hex) shown below:

<table>
<thead>
<tr>
<th>Address</th>
<th>+0</th>
<th>+1</th>
<th>+2</th>
<th>+3</th>
<th>+4</th>
<th>+5</th>
<th>+6</th>
<th>+7</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x00</td>
<td>AB</td>
<td>EE</td>
<td>1E</td>
<td>AC</td>
<td>D5</td>
<td>8E</td>
<td>10</td>
<td>E7</td>
</tr>
<tr>
<td>0x08</td>
<td>F7</td>
<td>84</td>
<td>32</td>
<td>2D</td>
<td>A5</td>
<td>F2</td>
<td>3A</td>
<td>CA</td>
</tr>
<tr>
<td>0x10</td>
<td>83</td>
<td>14</td>
<td>53</td>
<td>B9</td>
<td>70</td>
<td>03</td>
<td>F4</td>
<td>31</td>
</tr>
<tr>
<td>0x18</td>
<td>01</td>
<td>20</td>
<td>FE</td>
<td>34</td>
<td>46</td>
<td>E4</td>
<td>FC</td>
<td>52</td>
</tr>
<tr>
<td>0x20</td>
<td>4C</td>
<td>A8</td>
<td>B5</td>
<td>C3</td>
<td>D0</td>
<td>ED</td>
<td>53</td>
<td>17</td>
</tr>
</tbody>
</table>

int* ip = 0x00;
short* sp = 0x20;
long* yp = 0x10;

a) Fill in the type and value for each of the following C expressions. If a value cannot be determined from the given information answer UNKNOWN.

<table>
<thead>
<tr>
<th>Expression (in C)</th>
<th>Type</th>
<th>Value (in hex)</th>
</tr>
</thead>
<tbody>
<tr>
<td>yp + 2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>*(sp - 1)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ip[5]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>&amp;ip</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

b) Assuming that all registers start with the value 0, except %rax which is set to 0x4, fill in the values (in hex) stored in each register after the following x86 instructions are executed. Remember to give enough hex digits to fill up the width of the register name listed.

<table>
<thead>
<tr>
<th>Register</th>
<th>Value (in hex)</th>
</tr>
</thead>
<tbody>
<tr>
<td>%rax</td>
<td>0x0000 0000 0000 0004</td>
</tr>
<tr>
<td>%ebx</td>
<td></td>
</tr>
<tr>
<td>%ecx</td>
<td></td>
</tr>
<tr>
<td>%rdi</td>
<td></td>
</tr>
<tr>
<td>%si</td>
<td></td>
</tr>
</tbody>
</table>

movl 2(%rax), %ebx
leal (%rax,%rax,2), %ecx
movsbl 4(%rax), %edi
subw (%rax,2), %si
Examine the following recursive function:

```c
cparm long sunny(long a, long *b) {
    long temp;
    if (a < 1) {
        return *b - 8;
    } else {
        temp = a - 1;
        return temp + sunny(temp - 2, &temp);
    }
}
```

Here is the x86_64 assembly for the same function:

```assembly
0000000000400536 <sunny>:
400536: test    %rdi,%rdi
400539: jg 400543 <sunny+0xd>
40053b: mov (%rsi),%rax
40053e: sub $0x8,%rax
400542: retq
400543: push %rbx
400544: sub $0x10,%rsp
400548: lea -0x1(%rdi),%rbx
40054c: mov %rbx,0x8(%rsp)
400551: sub $0x3,%rdi
400555: lea 0x8(%rsp),%rsi
40055a: callq 400536 <sunny>
40055f: add %rbx,%rax
400562: add $0x10,%rsp
400566: pop %rbx
400567: retq
```

We call `sunny` from `main()`, with registers `%rsi = 0x7ff...ffad8` and `%rdi = 6`. The value stored at address `0x7ff...ffad8` is the long value 32 (0x20). We set a breakpoint at “return *b - 8” (i.e. we are just about to return from `sunny()` without making another recursive call). We have executed the `sub` instruction at `40053e` but have not yet executed the `retq`.

Fill in the register values on the next page and draw what the stack will look like when the program hits that breakpoint. Give both a description of the item stored at that location and the value stored at that location. If a location on the stack is not used, write “unused” in the Description for that address and put “-----” for its Value. You may list the Values in hex or decimal. Unless preceded by `0x` we will assume decimal. It is fine to use `f...f` for sequences of `f`’s as shown above for `%rsi`. Add more rows to the table as needed. Also, fill in the box on the next page to include the value this call to `sunny` will finally return to `main`.
<table>
<thead>
<tr>
<th>Register</th>
<th>Original Value</th>
<th>Value at Breakpoint</th>
</tr>
</thead>
<tbody>
<tr>
<td>rsp</td>
<td>0x7ff...ffad0</td>
<td></td>
</tr>
<tr>
<td>rdi</td>
<td>6</td>
<td></td>
</tr>
<tr>
<td>rsi</td>
<td>0x7ff...ffad8</td>
<td></td>
</tr>
<tr>
<td>rbx</td>
<td>4</td>
<td></td>
</tr>
<tr>
<td>rax</td>
<td>5</td>
<td></td>
</tr>
</tbody>
</table>

What value is **finally** returned to `main` by this call?

<table>
<thead>
<tr>
<th>Memory address on stack</th>
<th>Name/description of item</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x7fffffffffffffffaad8</td>
<td>Local var in <code>main</code></td>
<td>0x20</td>
</tr>
<tr>
<td>0x7fffffffffffffffaad0</td>
<td>Return address back to <code>main</code></td>
<td>0x400827</td>
</tr>
<tr>
<td>0x7fffffffffffffffac8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffac0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffab8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffab0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffaa8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffaa0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff98</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff90</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff88</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff80</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff78</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff70</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff68</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff60</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
**Au16 Midterm Q5**

**Question 5: The Stack [12 pts]**

The recursive factorial function `fact()` and its x86-64 disassembly is shown below:

```c
int fact(int n) {
    if(n==0 || n==1)
        return 1;
    return n*fact(n-1);
}
```

```
000000000040052d <fact>:
  40052d:  83 ff 00    cmpl  $0, %edi
  400530:  74 05      je  400537 <fact+0xa>
  400532:  83 ff 01    cmpl  $1, %edi
  400535:  75 07      jne  40053e <fact+0x11>
  400537:  b8 01 00 00 00  movl  $1, %eax
  40053c:  eb 0d      jmp  40054b <fact+0x1e>
  40053e:  57         pushq  %rdi
  40053f:  83 ef 01    subl  $1, %edi
  400542:  e8 e6 ff ff ff  call  40052d <fact>
  400547:  5f         popq  %rdi
  400548:  0f af c7    imull  %edi, %eax
  40054b:  f3 c3      rep ret
```

(A) Circle one: [1 pt] `fact()` is saving `%rdi` to the Stack as a **Caller // Callee**

(B) How much space (in bytes) does this function take up in our final executable? [2 pt]

(C) **Stack overflow** is when the stack exceeds its limits (i.e. runs into the Heap). Provide an argument to `fact(n)` here that will cause stack overflow. [2 pt]

«Problem continued on next page»
(D) If we use the `main` function shown below, answer the following for the execution of the entire program: [4 pt]

```c
void main() {
    printf("result = %d\n", fact(3));
}
```

| Total frames created: | Maximum stack frame depth: |

(E) In the situation described above where `main()` calls `fact(3)`, we find that the word `0x2` is stored on the Stack at address `0x7fffdc7ba888`. At what address on the Stack can we find the return address to `main()`? [3 pt]
Wi15 Midterm Q2
2. Assembly and C (20 points)

Consider the following x86-64 assembly and C code:

```
<do_something>:
    cmp    $0x0,%rsi
    ___  <end>
    xor    %rax,%rax
    sub    $0x1,%rsi

<loop>:
    lea    (%rdi,%rsi,___),%rdx
    add    (%rdx),%ax
    sub    $0x1,%rsi
    jns    <loop>

<end>:
    retq
```

```
short do_something(short* a, int len) {
    short result = 0;
    for (int i = ____; i >= 0; ____) {
        ___________;
    }
    return result;
}
```

(a) Both code segments are implementations of the unknown function `do_something`. Fill in the missing blanks in both versions. (Hint: `%rax` and `%rdi` are used for `result` and `a` respectively. `%rsi` is used for both `len` and `i`)

(b) Briefly describe the value that `do_something` returns and how it is computed. Use only variable names from the C version in your answer.
Wi17 Midterm Q3
3. Assembly and C (30 points)

Consider the following x86-64 assembly, (partially blank) C code, and memory listing. Addresses and values are 64-bit.

```assembly
foo:
    movl $0, %eax
L1:
    testq %rdi, %rdi
    je L2
    movq (%rdi), %rdi
    addl $1, %eax
    jmp L1
L2:
    ret
```

```c
int foo(long *p) {
    int result = ___;
    while (______) {
        p = ____________;
        ______ = ____________;
        movq (%rdi), %rdi
        return result;
    }
    jmp L1
}
```

<table>
<thead>
<tr>
<th>Address</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x1000</td>
<td>0x1030</td>
</tr>
<tr>
<td>0x1008</td>
<td>0x1020</td>
</tr>
<tr>
<td>0x1010</td>
<td>0x1000</td>
</tr>
<tr>
<td>0x1018</td>
<td>0x0000</td>
</tr>
<tr>
<td>0x1020</td>
<td>0x1030</td>
</tr>
<tr>
<td>0x1028</td>
<td>0x1008</td>
</tr>
<tr>
<td>0x1030</td>
<td>0x0000</td>
</tr>
<tr>
<td>0x1038</td>
<td>0x1038</td>
</tr>
<tr>
<td>0x1040</td>
<td>0x1048</td>
</tr>
<tr>
<td>0x1048</td>
<td>0x1040</td>
</tr>
</tbody>
</table>

(a) Given the assembly of `foo`, fill in the blanks of the C version.

(b) Trace the execution of the call to `foo((long*)0x1000)` in the table to the right. Show which instruction is executed in each step until `foo` returns. In each space, place the **assembly instruction** and the values of the appropriate registers **after that instruction executes**. You may leave those spots blank when the value does not change. You might not need all steps listed on the table.

<table>
<thead>
<tr>
<th>Instruction</th>
<th>%rdi (hex)</th>
<th>%eax (decimal)</th>
</tr>
</thead>
<tbody>
<tr>
<td>movl</td>
<td>0x1000</td>
<td>0</td>
</tr>
<tr>
<td>testq</td>
<td></td>
<td></td>
</tr>
<tr>
<td>je</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(c) Briefly describe the value that `foo` returns and how it is computed. Use only variable names from the C version in your answer.
Wi16 Midterm Q4
4. (9 points) Computer-Architecture Design

(a) In roughly one English sentence, give a reason that it is better to have fewer registers in an instruction-set architecture.

(b) In roughly one English sentence, give a reason that it is better to have many registers in an instruction-set architecture.

(c) Yes or no: If we decided to change the x86-64 calling convention to make %rbx caller-saved, would the implementation of the CPU need to change?