

CSE 351 Section 3 – Integers and Floating Point

Welcome back to section, we're happy that you're here ☺

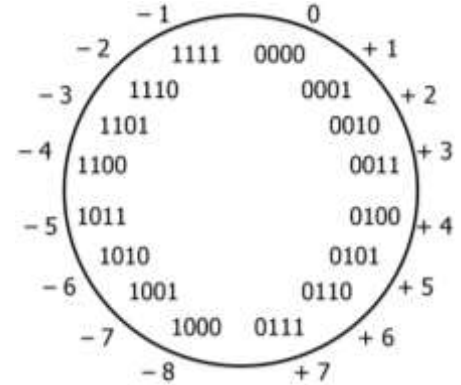
Signed Integers with Two's Complement

Two's complement is the standard for representing signed integers:

- The most significant bit (MSB) has a negative value; all others have positive values (same as unsigned)
- Binary addition is performed the same way for signed and unsigned
- The bit representation for the negative (additive inverse) of a two's complement number can be found by:

flipping all the bits and adding 1 (i.e. $-x = \sim x + 1$).

The "number wheel" showing the relationship between 4-bit numerals and their Two's Complement interpretations is shown on the right:



- The largest number is 7 whereas the smallest number is -8
- There is a nice symmetry between numbers and their negative counterparts except for -8

Exercises: (assume 8-bit integers)

1) What is the **largest integer**? The **largest integer + 1**?

<u>Unsigned:</u>	<u>Two's Complement:</u>
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2) How do you represent (if possible) the following numbers: **39, -39, 127**?

<u>Unsigned:</u>	<u>Two's Complement:</u>
39:	39:
-39:	-39:
127:	127:

3) Compute the following sums in binary using your Two's Complement answers from above. *Answer in hex.*

<p>a. 39 -> 0b _____</p> <p>+ (-39) -> 0b _____</p> <p>0x __ <- 0b _____</p>	<p>b. 127 -> 0b _____</p> <p>+ (-39) -> 0b _____</p> <p>0x __ <- 0b _____</p>
<p>c. 39 -> 0b _____</p> <p>- 127 -> 0b _____</p> <p>0x __ <- 0b _____</p>	<p>d. 127 -> 0b _____</p> <p>+ 39 -> 0b _____</p> <p>0x __ <- 0b _____</p>

4) Interpret each of your answers above and indicate whether or not overflow has occurred.

<p>a. 39+(-39)</p> <p>Unsigned:</p> <p>Two's Complement:</p>	<p>b. 127+(-39)</p> <p>Unsigned:</p> <p>Two's Complement:</p>
<p>c. 39-127</p> <p>Unsigned:</p> <p>Two's Complement:</p>	<p>d. 127+39</p> <p>Unsigned:</p> <p>Two's Complement:</p>

Floating Point Mathematical Properties

- Not associative: $(2 + 2^{50}) - 2^{50} \neq 2 + (2^{50} - 2^{50})$
- Not distributive: $100 \times (0.1 + 0.2) \neq 100 \times 0.1 + 100 \times 0.2$
- Not cumulative: $2^{25} + 1 + 1 + 1 + 1 \neq 2^{25} + 4$

Exercises:

9) Based on floating point representation, explain why each of the three statements above occurs.

10) If x and y are variable type `float`, give two *different* reasons why $(x+2*y) - y == x+y$ might evaluate to false.

1EEE 754 Float (32 bit) Flowchart

