Caches I

CSE 351 Autumn 2016

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Administrivia

- Homework 2 due today at 5pm
- Lab 3 due next Thursday

- Midterm will be graded over the weekend
  - Posted solutions not set in stone

Roadmap

C:

```
car *c = malloc(sizeof(car));
c->miles = 100;
c->gals = 17;
float mpg = get_mpg(c);
free(c);
```

Java:

```
Car c = new Car();
c.setMiles(100);
c.setGals(17);
float mpg =
    c.getMPG();
```

Assembly language:

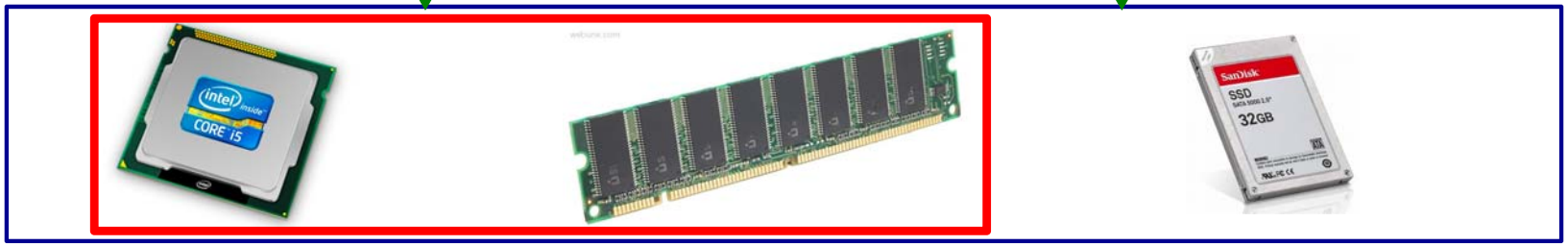
```
get_mpg:
    pushq   %rbp
    movq    %rsp, %rbp
    ...
    popq    %rbp
    ret
```

Machine code:

```
0111010000011000
100011010000010000000010
1000100111000010
11000001111110100011111
```

OS:

Computer system:



Memory & data
Integers & floats
Machine code & C
x86 assembly
Procedures & stacks
Arrays & structs
Memory & caches
Processes
Virtual memory
Memory allocation
Java vs. C

How does execution time grow with SIZE?

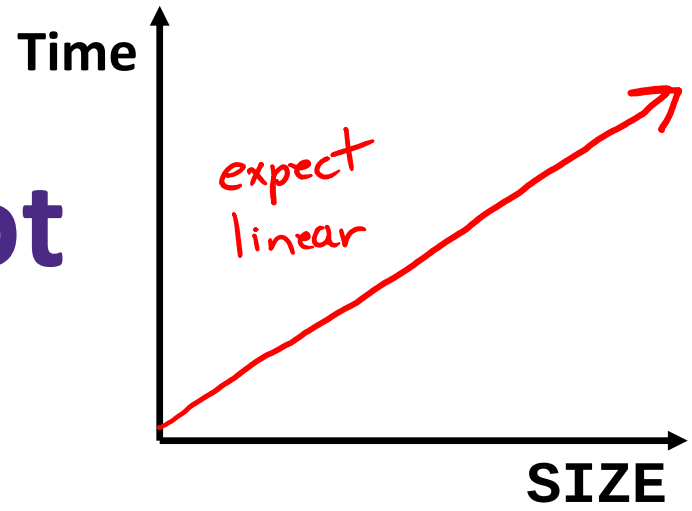
```
int array[SIZE];
int sum = 0;

for (int i = 0; i < 200000; i++) {
  for (int j = 0; j < SIZE; j++) {
    sum += array[j];
  }
}
```

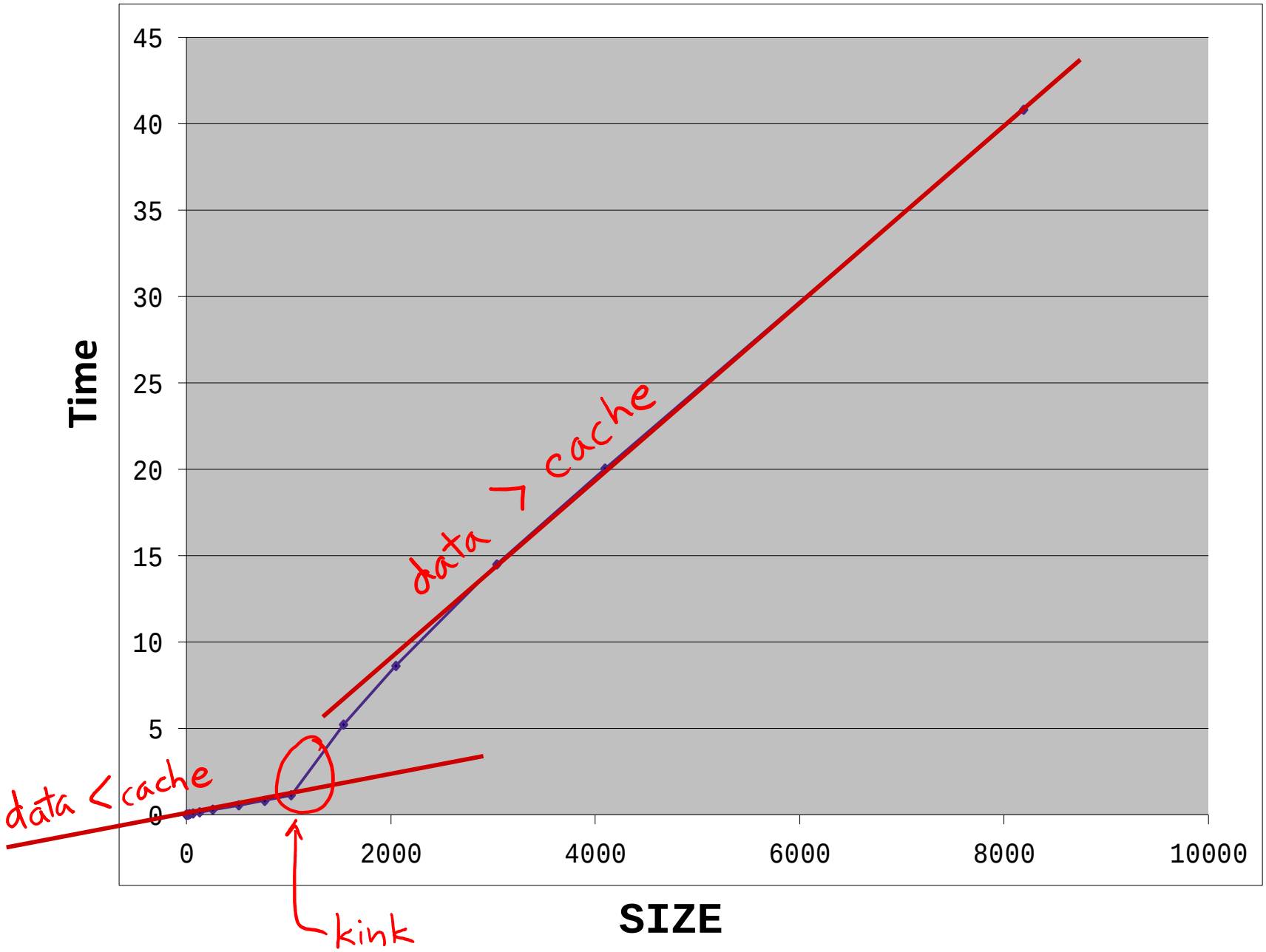
repeat 200,000 times

← execute SIZE × 200,000 times

Plot



Actual Data

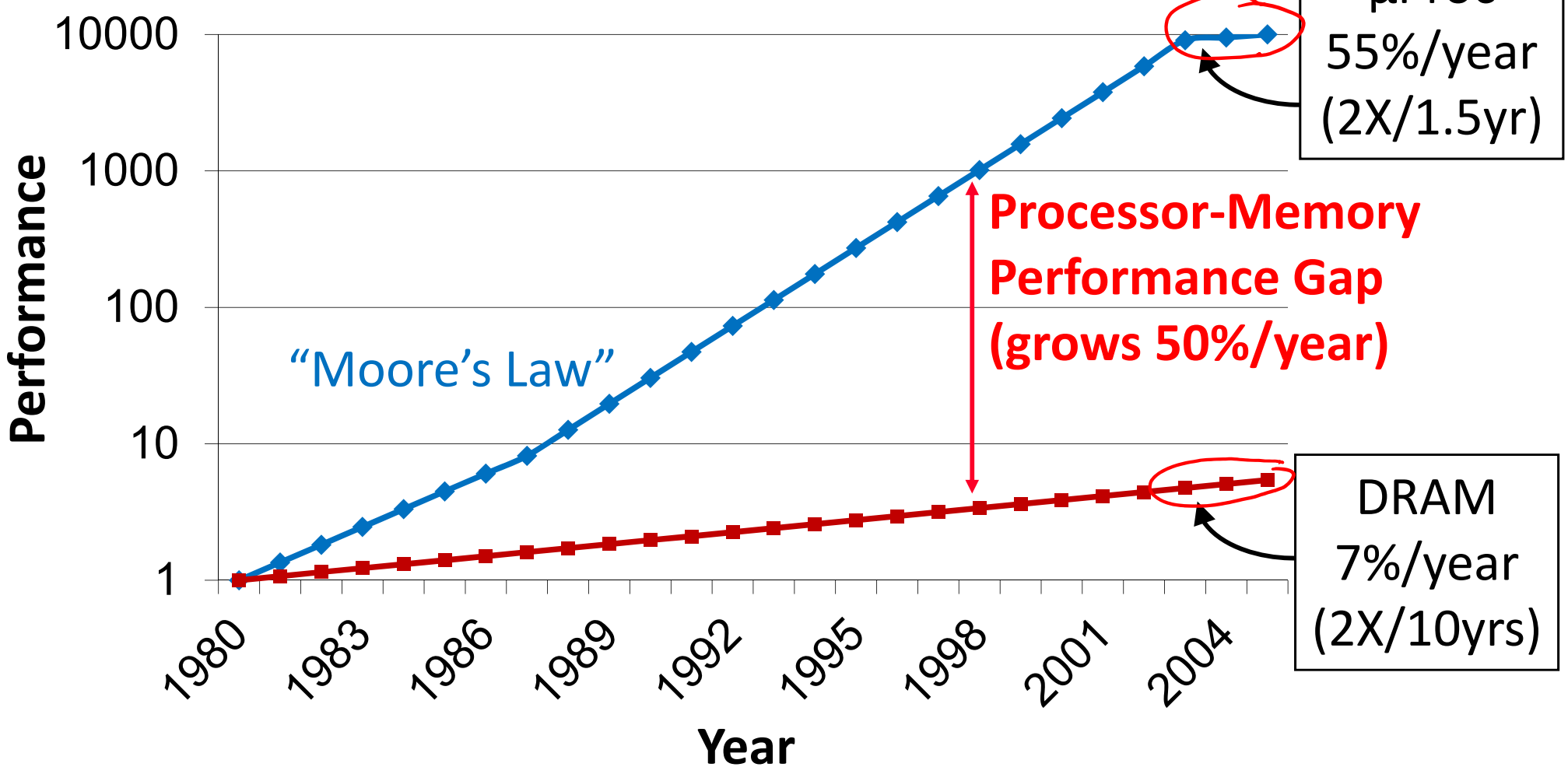

45
40
35
30
25
20
15
10
5
0
Time
0
2000
4000
6000
8000
10000
SIZE
data > cache
data < cache
kink

Making memory accesses fast!

- **Cache basics**
- **Principle of locality**
- **Memory hierarchies**
- Cache organization
- Program optimizations that consider caches

Processor-Memory Gap

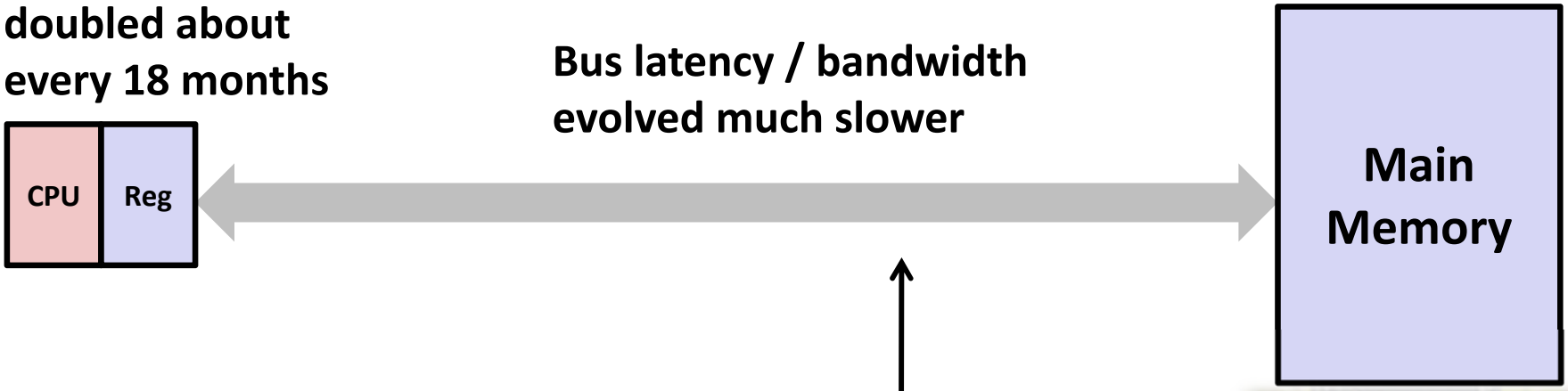
1989 first Intel CPU with cache on chip
1998 Pentium III has two cache levels on chip



Problem: Processor-Memory Bottleneck

Processor performance doubled about every 18 months

Bus latency / bandwidth evolved much slower



Core 2 Duo:
Can process at least
256 Bytes/cycle

Core 2 Duo:
Bandwidth
2 Bytes/cycle
Latency
100-200 cycles (30-60ns)

Problem: lots of waiting on memory

***cycle**: single machine step (fixed-time)*

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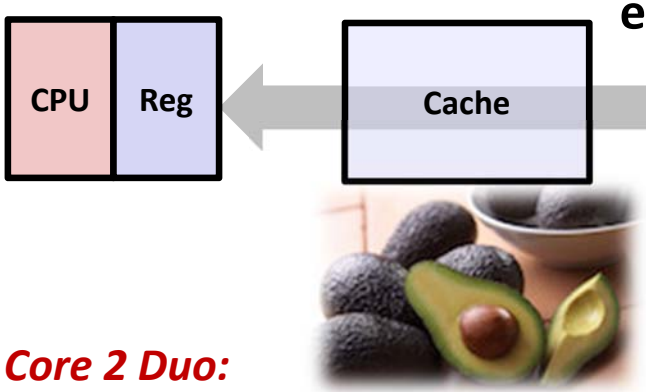

Core 2 Duo:
Can process at least
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Core 2 Duo:
Bandwidth
2 Bytes/cycle
Latency
100-200 cycles (30-60ns)

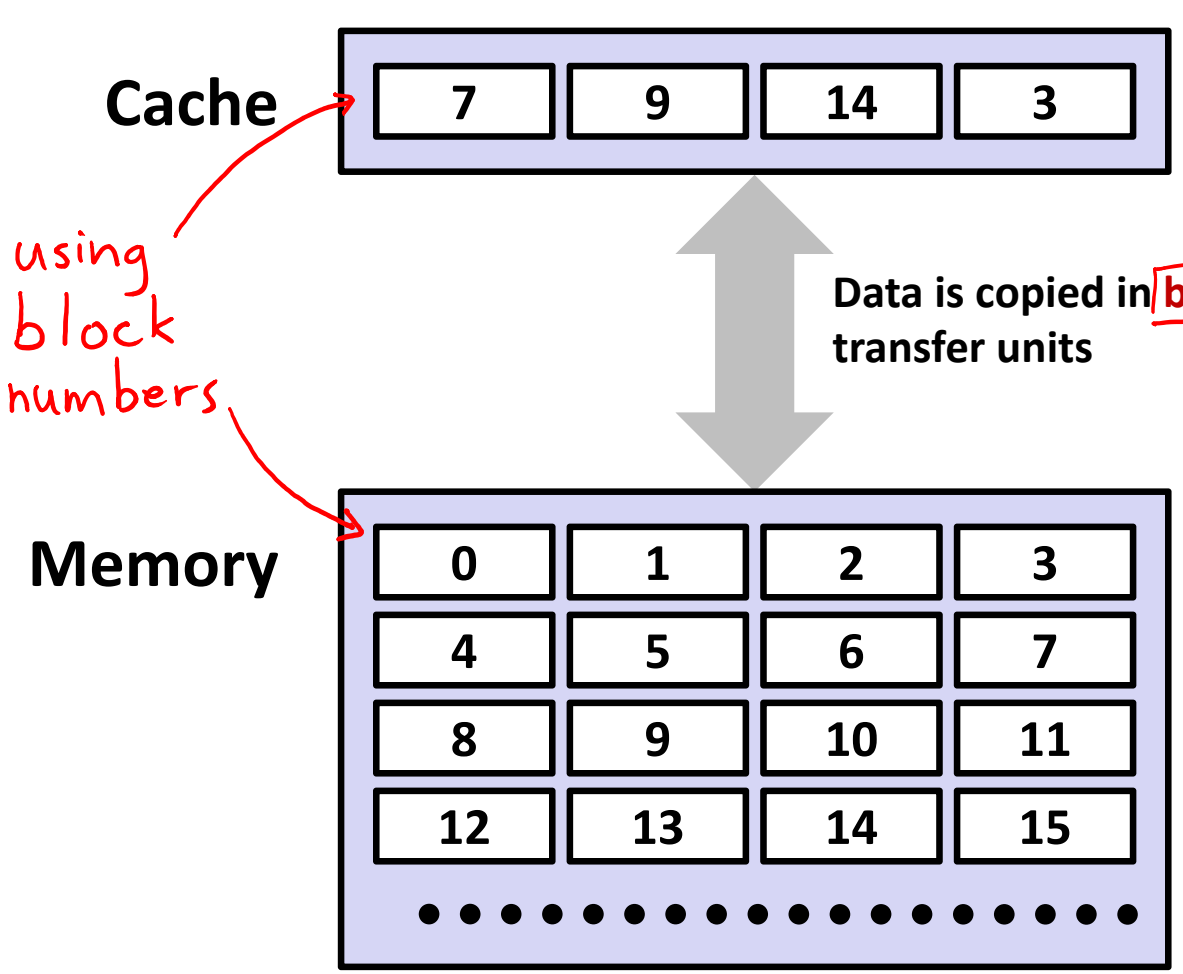
Solution: caches

***cycle**: single machine step (fixed-time)*

Cache 

- Pronunciation: "cash"
  - We abbreviate this as "$"
- English: A hidden storage space for provisions, weapons, and/or treasures
- Computer: Memory with short access time used for the storage of frequently or recently used instructions (i-cache/I$) or data (d-cache/D$)
  - *More generally:* Used to optimize data transfers between any system elements with different characteristics (network interface cache, I/O cache, etc.)

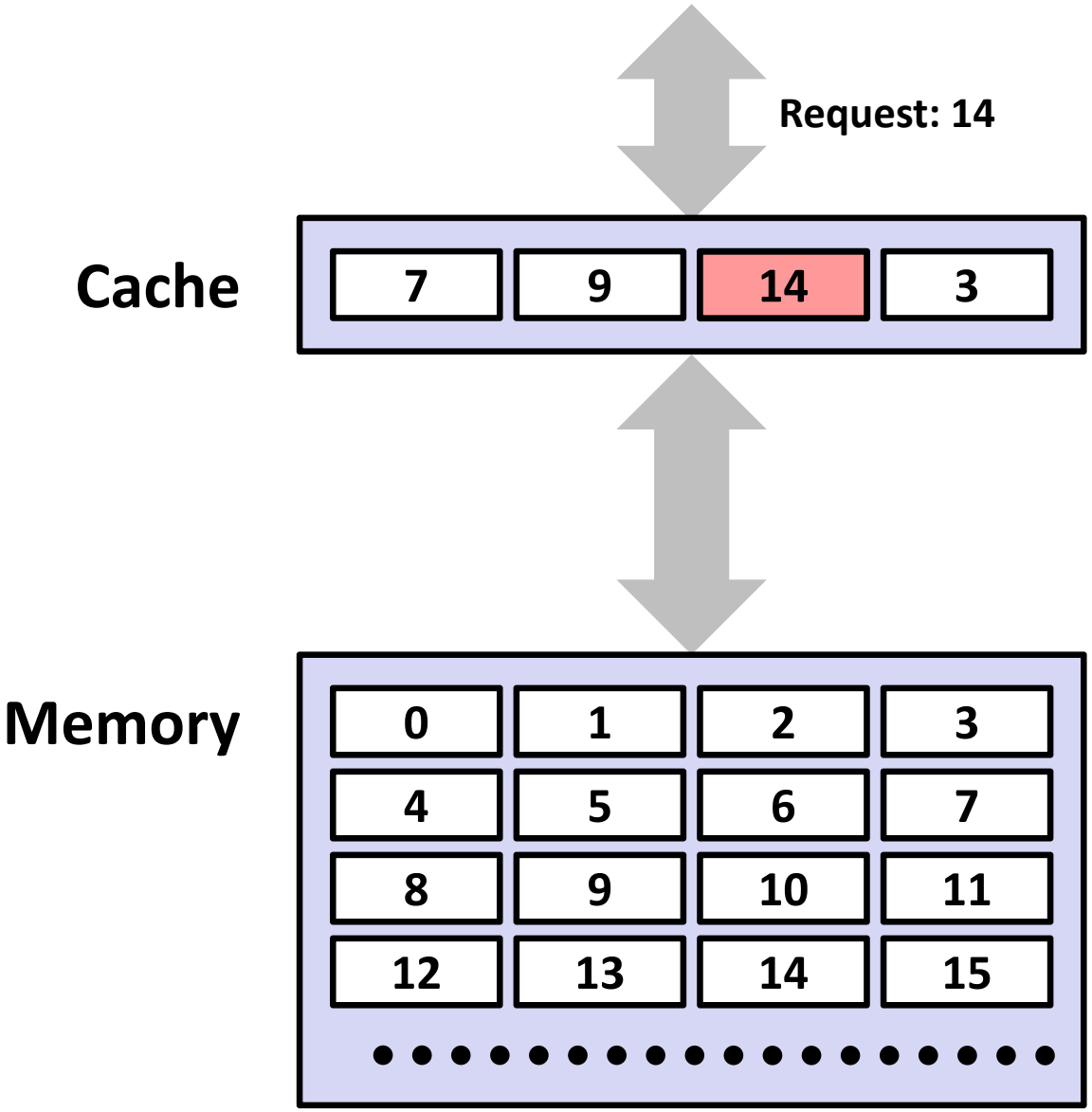
General Cache Mechanics



- Smaller, faster, more expensive memory.
- Caches a subset of the blocks (a.k.a. *lines*)

- Larger, slower, cheaper memory.
- Viewed as partitioned into "blocks" or "lines"

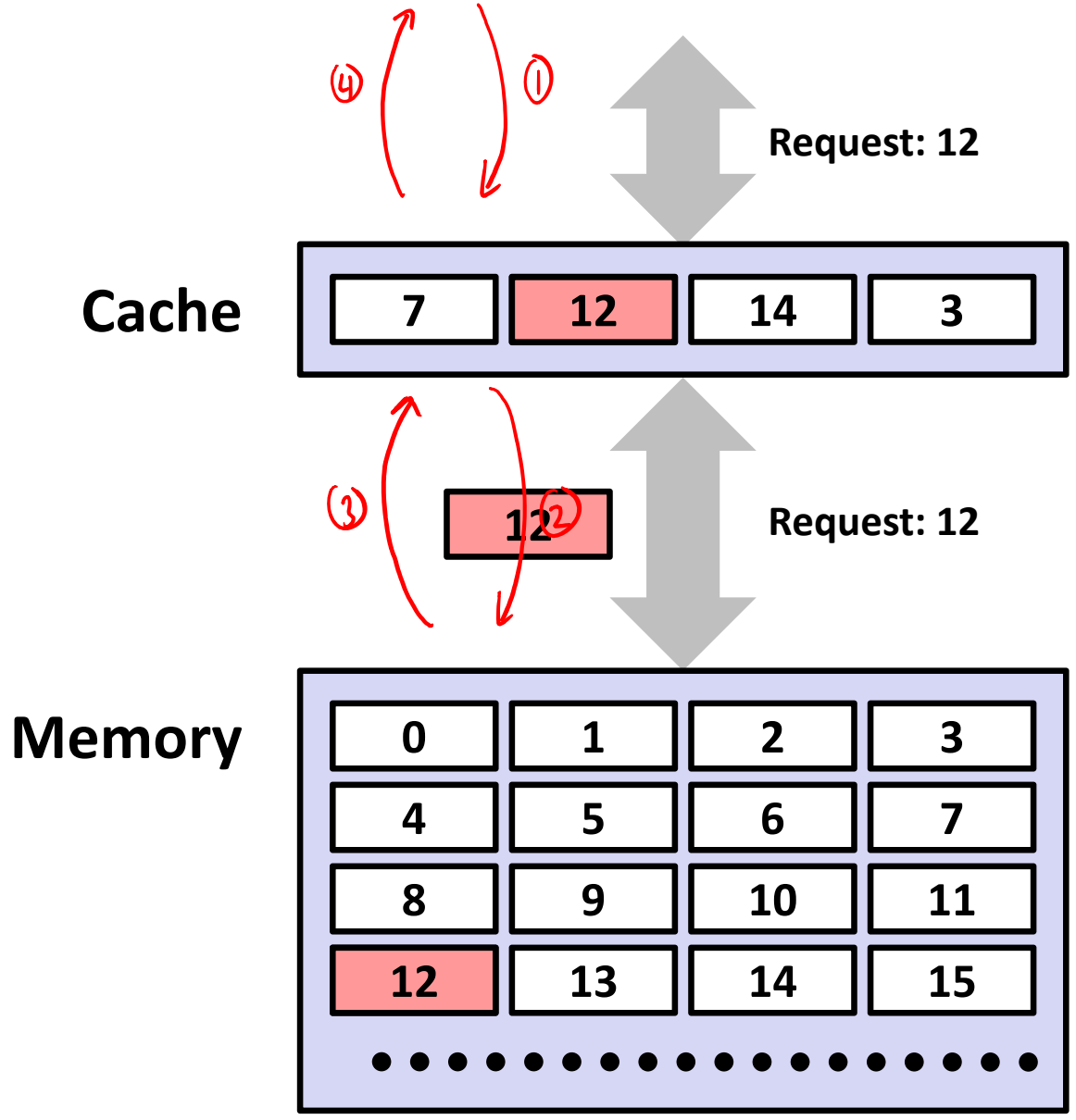
General Cache Concepts: Hit



Data in block b is needed

Block b is in cache:
Hit!

General Cache Concepts: Miss



① ***Data in block b is needed***

Block b is not in cache: Miss!

② ***Block b is fetched from memory***

③ ***Block b is stored in cache***

- Placement policy: determines where b goes
- Replacement policy: determines which block gets evicted (victim)

④ Data returned to CPU

Why Caches Work

- Locality: Programs tend to use data and instructions with addresses near or equal to those they have used recently

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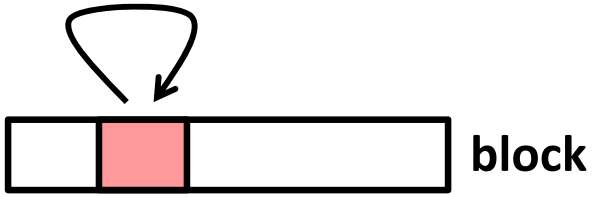
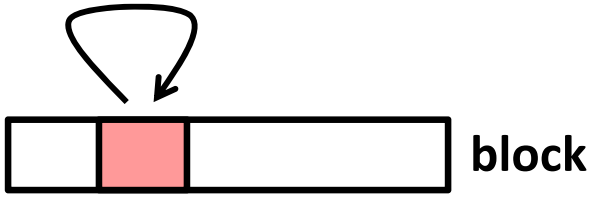


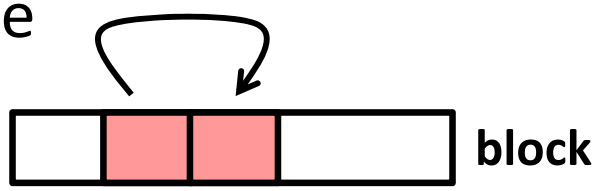
- *Temporal* locality:
  - Recently referenced items are *likely* to be referenced again in the near future

Why Caches Work

- Locality: Programs tend to use data and instructions with addresses near or equal to those they have used recently



- *Temporal* locality:
  - Recently referenced items are *likely* to be referenced again in the near future



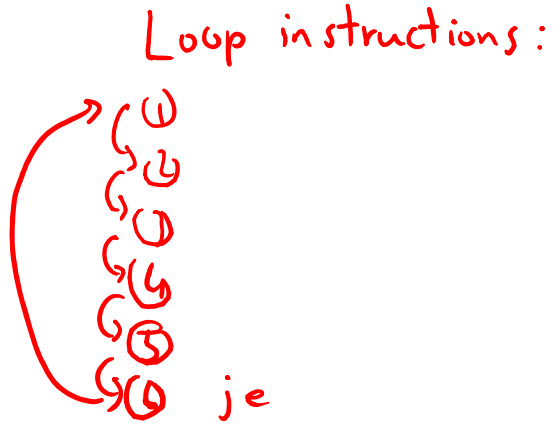
- *Spatial* locality:
  - Items with nearby addresses *tend* to be referenced close together in time

- How do caches take advantage of this?

Example: Any Locality?

```
sum = 0;
for (i = 0; i < n; i++)
{
  sum += a[i];
}
return sum;
```

a[0]
a[1]
a[2]



- **Data:**
  - Temporal: sum referenced in each iteration
  - Spatial: array a[ ] accessed in stride-1 pattern
- **Instructions:**
  - Temporal: cycle through loop repeatedly
  - Spatial: reference instructions in sequence

Locality Example #1

```
int sum_array_rows(int a[M][N])
{
    int i, j, sum = 0;

    for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            sum += a[i][j];

    return sum;
}
```

Locality Example #1

```
int sum_array_rows(int a[M][N])
{
    int i, j, sum = 0;

    for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            sum += a[i][j];

    return sum;
}
```

0, 0
0, 1

M = 3, N=4

a[0][0]	a[0][1]	a[0][2]	a[0][3]
a[1][0]	a[1][1]	a[1][2]	a[1][3]
a[2][0]	a[2][1]	a[2][2]	a[2][3]

Access Pattern:

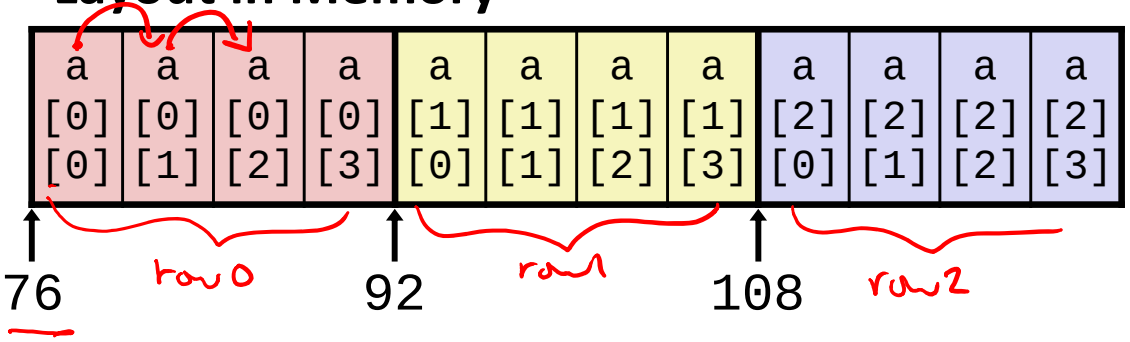
stride = ?

1 int
4 B

"stride-1"

1) a[0][0]
2) a[0][1]
3) a[0][2]
4) a[0][3]
5) a[1][0]
6) a[1][1]
7) a[1][2]
8) a[1][3]
9) a[2][0]
10) a[2][1]
11) a[2][2]
12) a[2][3]

Layout in Memory



Note: 76 is just one possible starting address of array a

Locality Example #2

```
int sum_array_cols(int a[M][N])
{
    int i, j, sum = 0;

    for (j = 0; j < N; j++)
        for (i = 0; i < M; i++)
            sum += a[i][j];

    return sum;
}
```

Locality Example #2

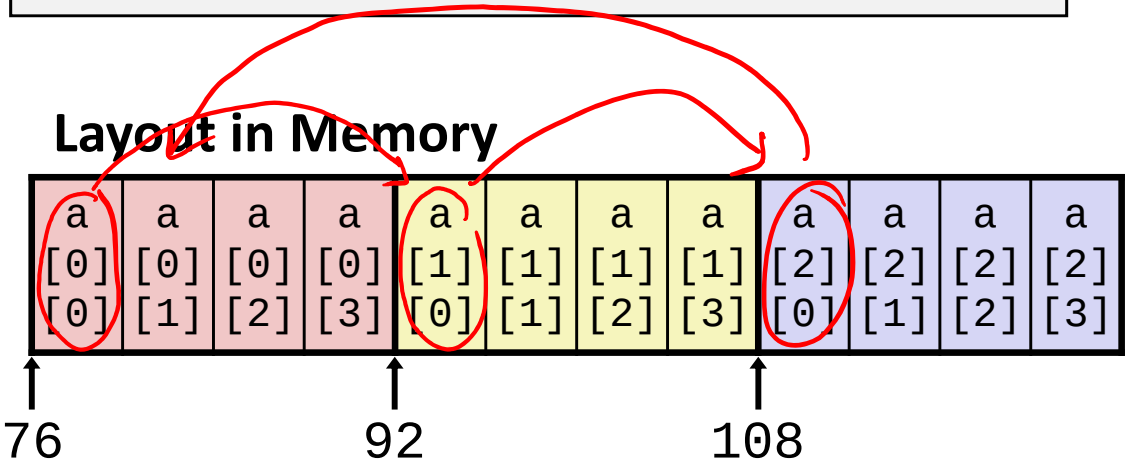
```
int sum_array_cols(int a[M][N])
{
    int i, j, sum = 0;

    for (j = 0; j < N; j++)
        for (i = 0; i < M; i++)
            sum += a[i][j];

    return sum;
}
```

0, 0
1, 0

M = 3, N=4

a[0][0]	a[0][1]	a[0][2]	a[0][3]
a[1][0]	a[1][1]	a[1][2]	a[1][3]
a[2][0]	a[2][1]	a[2][2]	a[2][3]

Layout in Memory



Access Pattern:

stride = ?

4 ints

16 B

stride-4

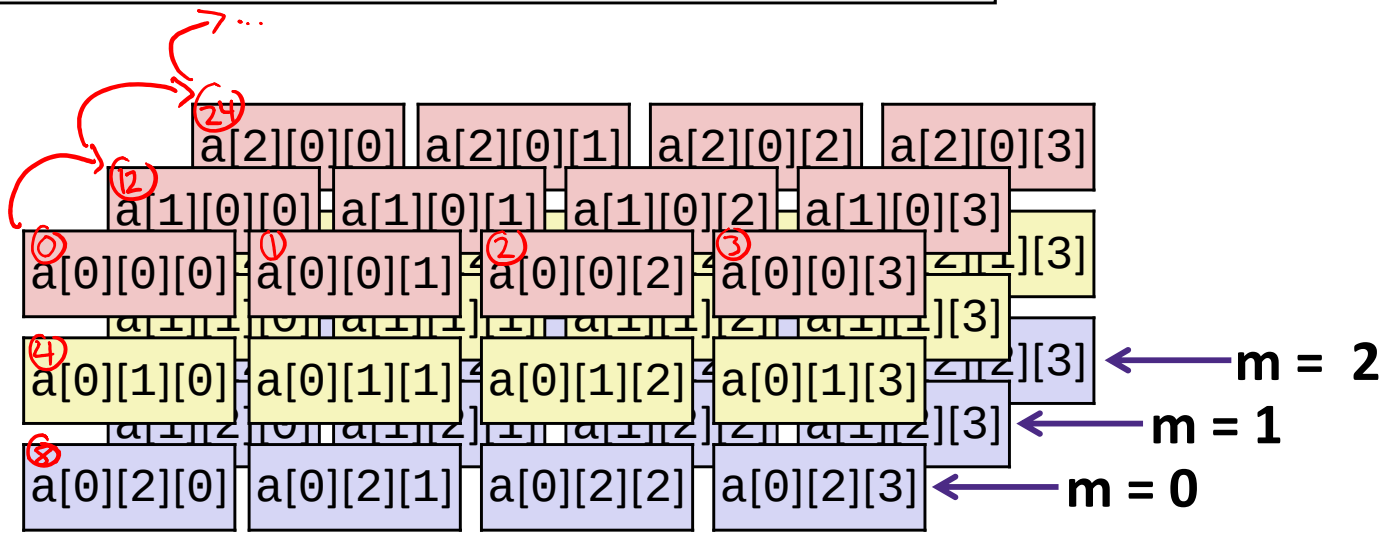
"stride-N"

1)	a[0][0]
2)	a[1][0]
3)	a[2][0]
4)	a[0][1]
5)	a[1][1]
6)	a[2][1]
7)	a[0][2]
8)	a[1][2]
9)	a[2][2]
10)	a[0][3]
11)	a[1][3]
12)	a[2][3]

Locality Example #3

```
int sum_array_3D(int a[M][N][L])
{
    int i, j, k, sum = 0;

    for (i = 0; i < N; i++)
        for (j = 0; j < L; j++)
            for (k = 0; k < M; k++)
                sum += a[k][i][j];

    return sum;
}
```

- What is wrong with this code?
  "stride-N*L"!
- How can it be fixed?



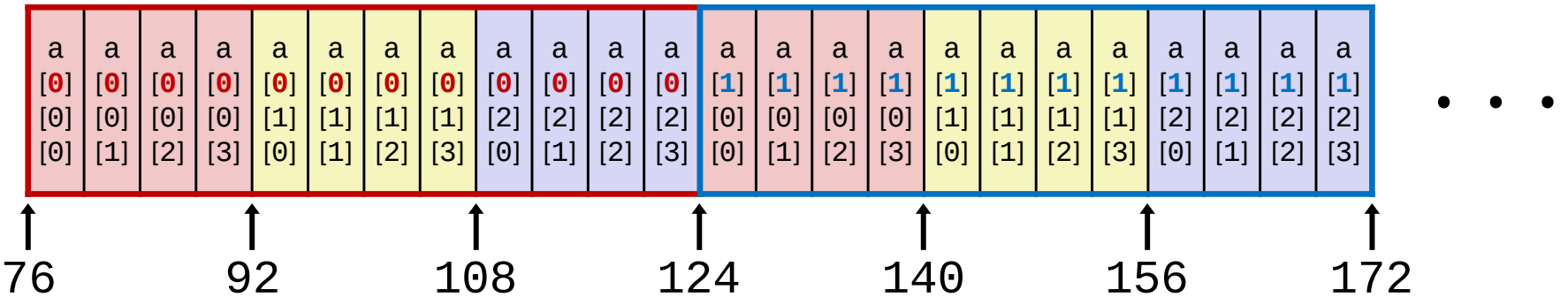
Locality Example #3

```
int sum_array_3D(int a[M][N][L])
{
    int i, j, k, sum = 0;

    for (i = 0; i < N; i++)
        for (j = 0; j < L; j++)
            for (k = 0; k < M; k++)
                sum += a[k][i][j];

    return sum;
}
```

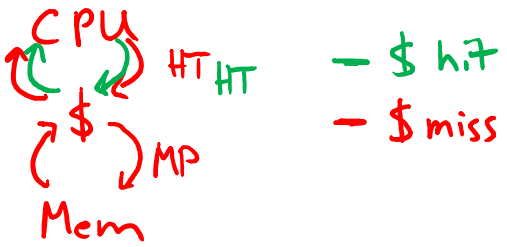
- What is wrong with this code?
- How can it be fixed?

inner loop: k = stride-N*L
i = stride-L
j = stride-1

Layout in Memory (M = ?, N = 3, L = 4)



Cache Performance Metrics



- Huge difference between a cache hit and a cache miss
  - Could be 100x speed difference between accessing cache and main memory (measured in *clock cycles*)
- Miss Rate (MR)
  - Fraction of memory references not found in cache (misses / accesses) = 1 - Hit Rate
- Hit Time (HT)
  - Time to deliver a block in the cache to the processor
    - Includes time to determine whether the block is in the cache
- Miss Penalty (MP)
  - Additional time required because of a miss

Cache Performance

- Two things hurt the performance of a cache:
  - Miss rate and miss penalty

- *Average Memory Access Time* (AMAT): average time to access memory considering both hits and misses

  AMAT = Hit time + Miss rate × Miss penalty

  (abbreviated AMAT = HT + MR × MP)

- 99% hit rate twice as good as 97% hit rate!
  - Assume HT of 1 clock cycle and MP of 100 clock cycles
  - 97%: AMAT = $1 + (1-0.97) \times 100 = 1+3 = 4$ clock cycles
  - 99%: AMAT = $1 + (1-0.99) \times 100 = 1+1 = 2$ clock cycles

Peer Instruction Question

- **Processor specs:** 200 ps clock, MP of 50 clock cycles, MR of 0.02 misses/instruction, and HT of 1 clock cycle

  AMAT = $1 + 50(0.02) = 1+1 = 2$ clock cycles, 400 ps

- Which improvement would be best?
  - 190 ps clock (overclocking) 380 ps
  - MP of 40 clock cycles (changing mem – smaller) $1 + 40(0.02) = 1.8$ cc $= 360$ ps
  - MR of 0.015 misses/instruction (better locality in code) $1 + 50(0.015) = 1.75$ cc $= 350$ ps

Can we have more than one cache?

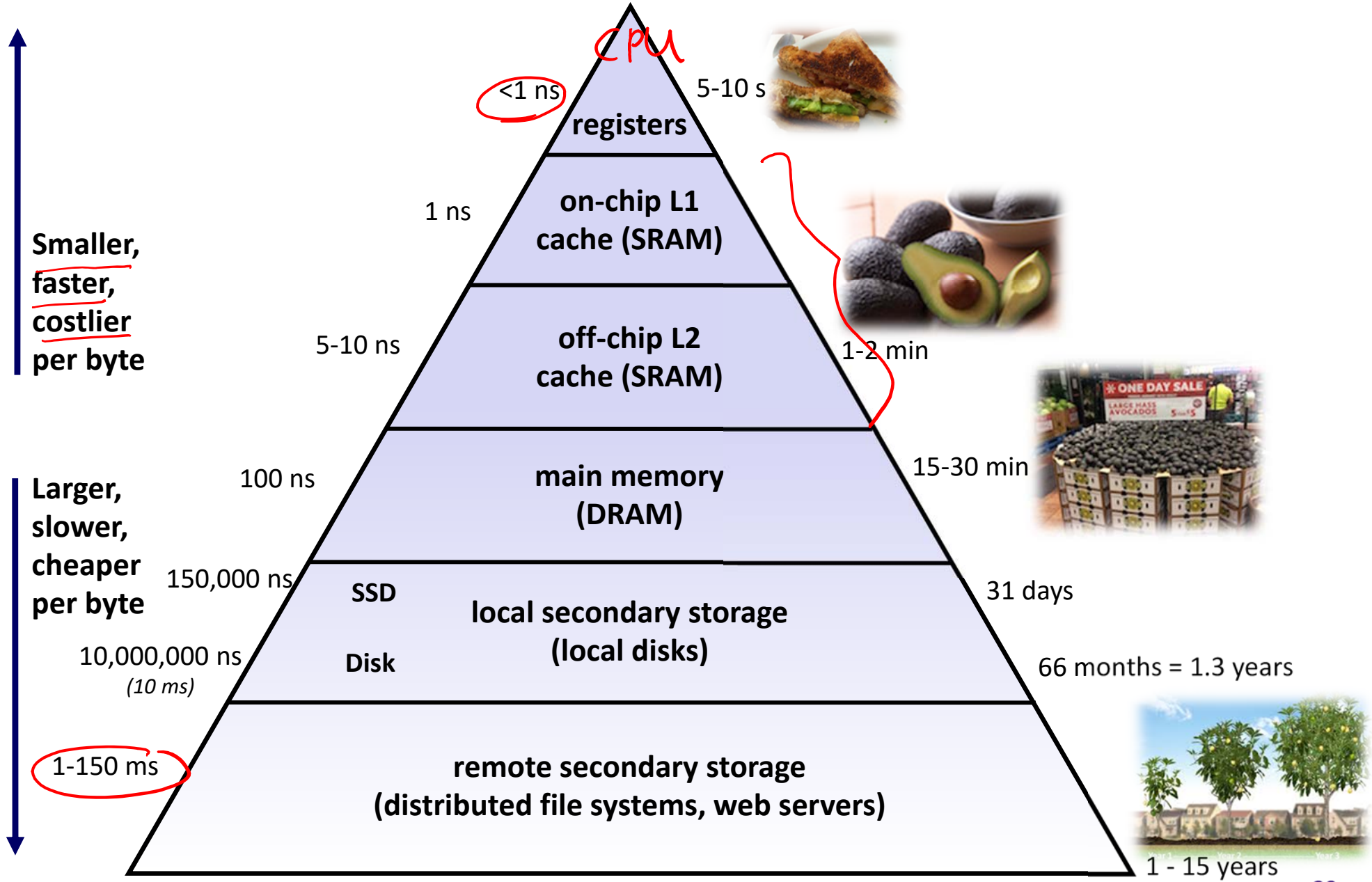
- Why would we want to do that?
  - Avoid going to memory!
- Typical performance numbers:
  - Miss Rate
    - L1 MR = 3-10%
    - L2 MR = Quite small (e.g., < 1%), depending on parameters, etc.
  - Hit Time
    - L1 HT = 4 clock cycles
    - L2 HT = 10 clock cycles
  - Miss Penalty
    - P = 50-200 cycles for missing in L2 & going to main memory
    - Trend: increasing!

Memory Hierarchies

- Some fundamental and enduring properties of hardware and software systems:
  - Faster storage technologies almost always cost more per byte and have lower capacity
  - The gaps between memory technology speeds are widening
    - True for: registers ↔ cache, cache ↔ DRAM, DRAM ↔ disk, etc.
  - Well-written programs tend to exhibit good locality

- These properties complement each other beautifully
  - They suggest an approach for organizing memory and storage systems known as a memory hierarchy

An Example Memory Hierarchy



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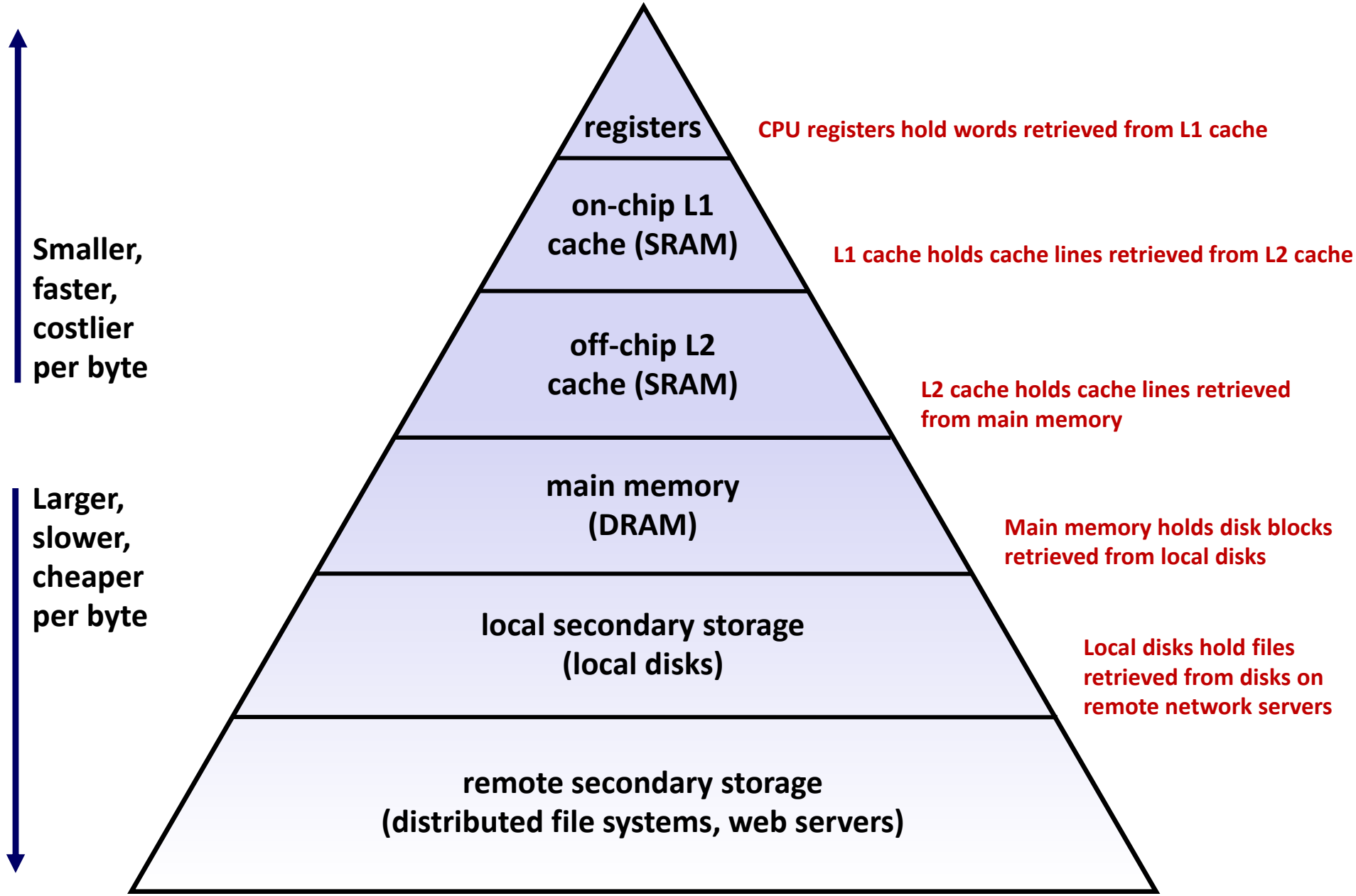

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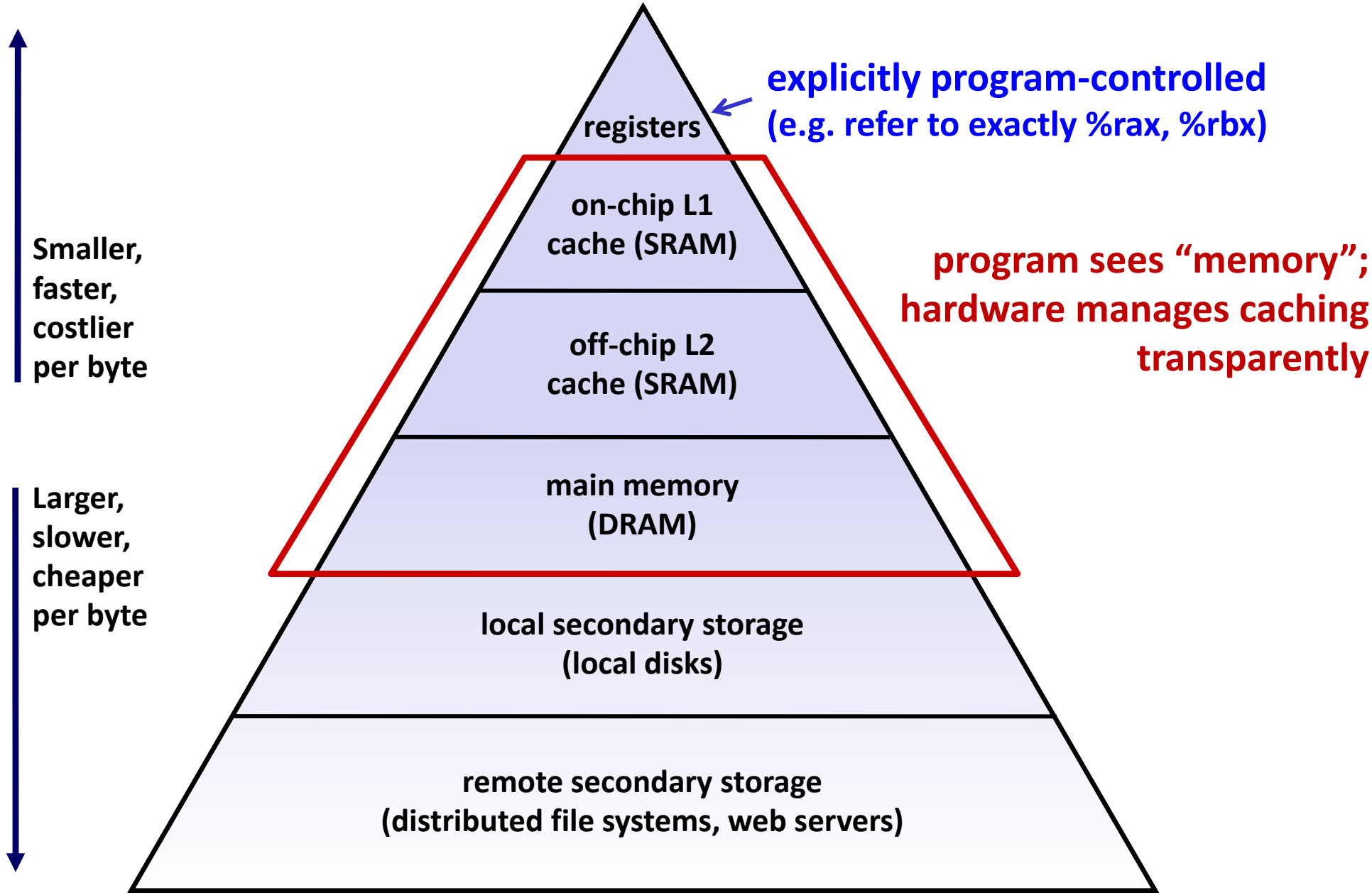
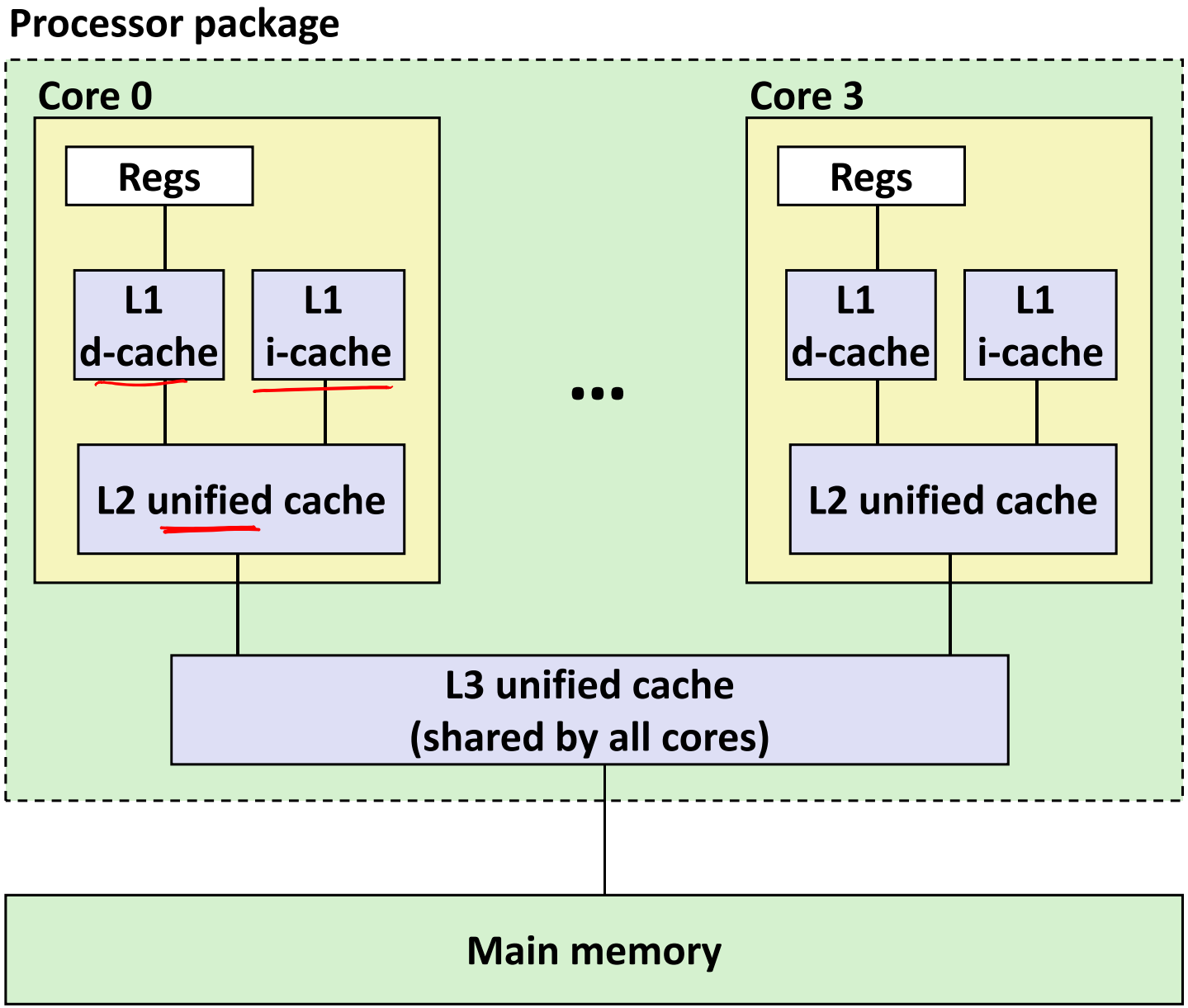


Memory Hierarchies

- Fundamental idea of a memory hierarchy:
  - For each level k, the faster, smaller device at level k serves as a cache for the larger, slower device at level k+1
- Why do memory hierarchies work?
  - Because of locality, programs tend to access the data at level k more often than they access the data at level k+1
  - Thus, the storage at level k+1 can be slower, and thus larger and cheaper per bit
- *Big Idea:* The memory hierarchy creates a large pool of storage that costs as much as the cheap storage near the bottom, but that serves data to programs at the rate of the fast storage near the top

Intel Core i7 Cache Hierarchy



Block size:
64 bytes for all caches.

L1 i-cache and d-cache:
32 KB, 8-way,
Access: 4 cycles

L2 unified cache:
256 KB, 8-way,
Access: 11 cycles

L3 unified cache:
8 MB, 16-way,
Access: 30-40 cycles

Summary

- Memory Hierarchy
  - Successively higher levels contain "most used" data from lower levels
  - Exploits *temporal and spatial locality*
  - Caches are intermediate storage levels used to optimize data transfers between any system elements with different characteristics
- Cache Performance
  - Ideal case: found in cache (hit)
  - Bad case: not found in cache (miss), search in next level
  - Average Memory Access Time (AMAT) = HT + MR × MP
    - Hurt by Miss Rate and Miss Penalty