

Arrays

CSE 351 Autumn 2016

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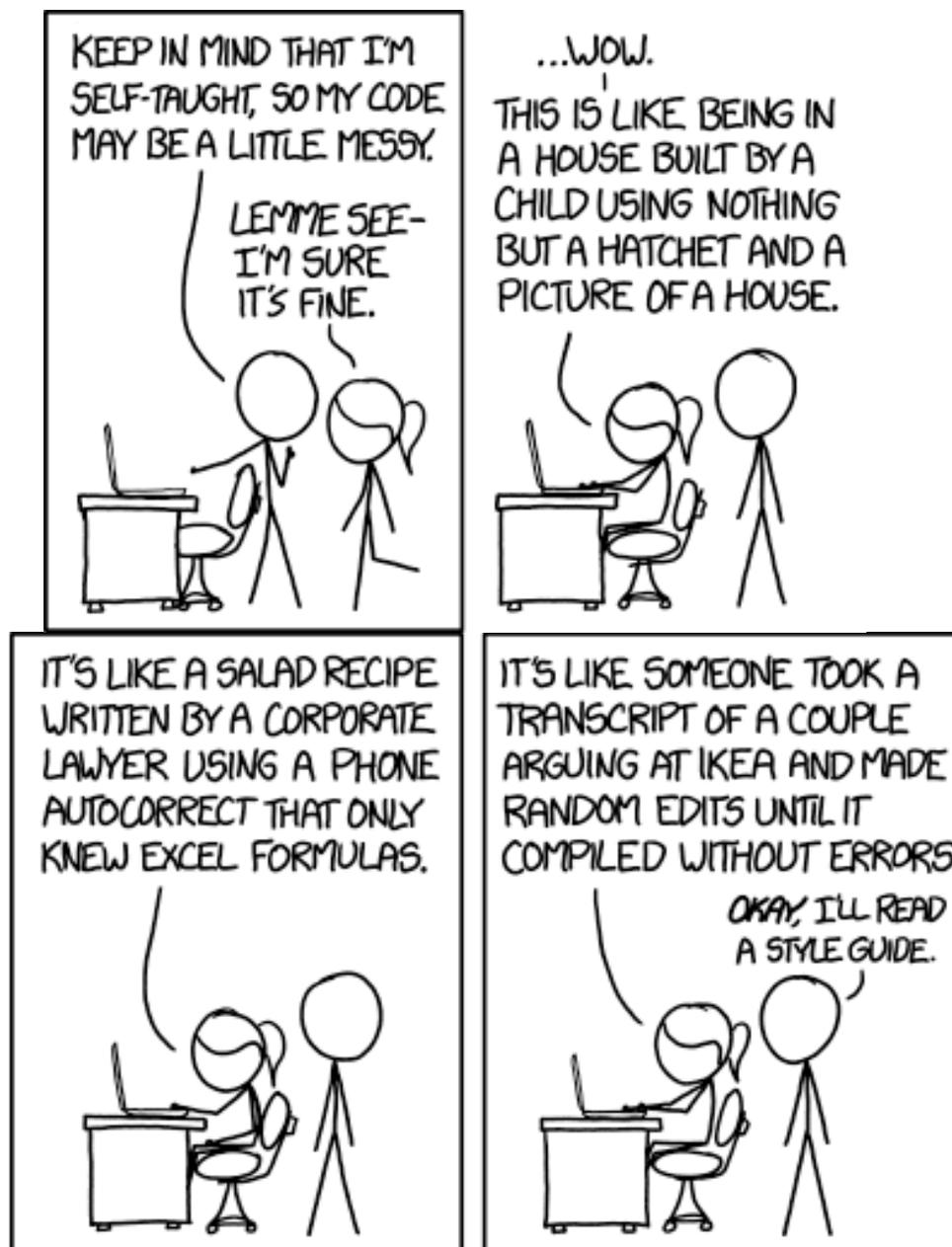
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<http://xkcd.com/1513/>

Administrivia

- ❖ Lab 2 due Friday
- ❖ Homework 2 released on Friday

- ❖ **Midterm** on Nov. 2 in lecture
 - Make a cheat sheet! – two-sided letter page, *handwritten*
 - Midterm details Piazza post: [@225](#)
 - Past Num Rep and Floating Point questions posted (solutions tonight)

- ❖ **Midterm review session**
 - 5-7pm on Monday, Oct. 31 in EEB 105

Roadmap

C:

```
car *c = malloc(sizeof(car));
c->miles = 100;
c->gals = 17;
float mpg = get_mpg(c);
free(c);
```

Java:

```
Car c = new Car();
c.setMiles(100);
c.setGals(17);
float mpg =
    c.getMPG();
```

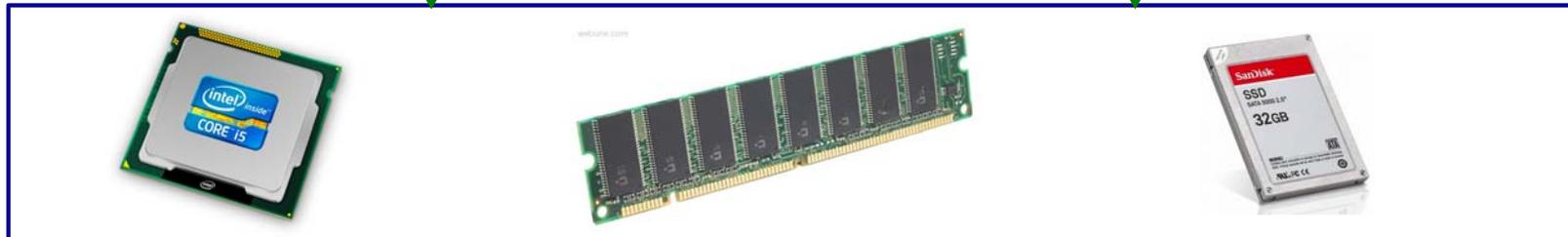
Assembly language:

```
get_mpg:
    pushq   %rbp
    movq   %rsp, %rbp
    ...
    popq   %rbp
    ret
```

Machine code:

```
0111010000011000
100011010000010000000010
1000100111000010
110000011111101000011111
```

Computer system:



- Memory & data
- Integers & floats
- Machine code & C
- x86 assembly
- Procedures & stacks
- Arrays & structs**
- Memory & caches
- Processes
- Virtual memory
- Memory allocation
- Java vs. C

OS:



Data Structures in Assembly

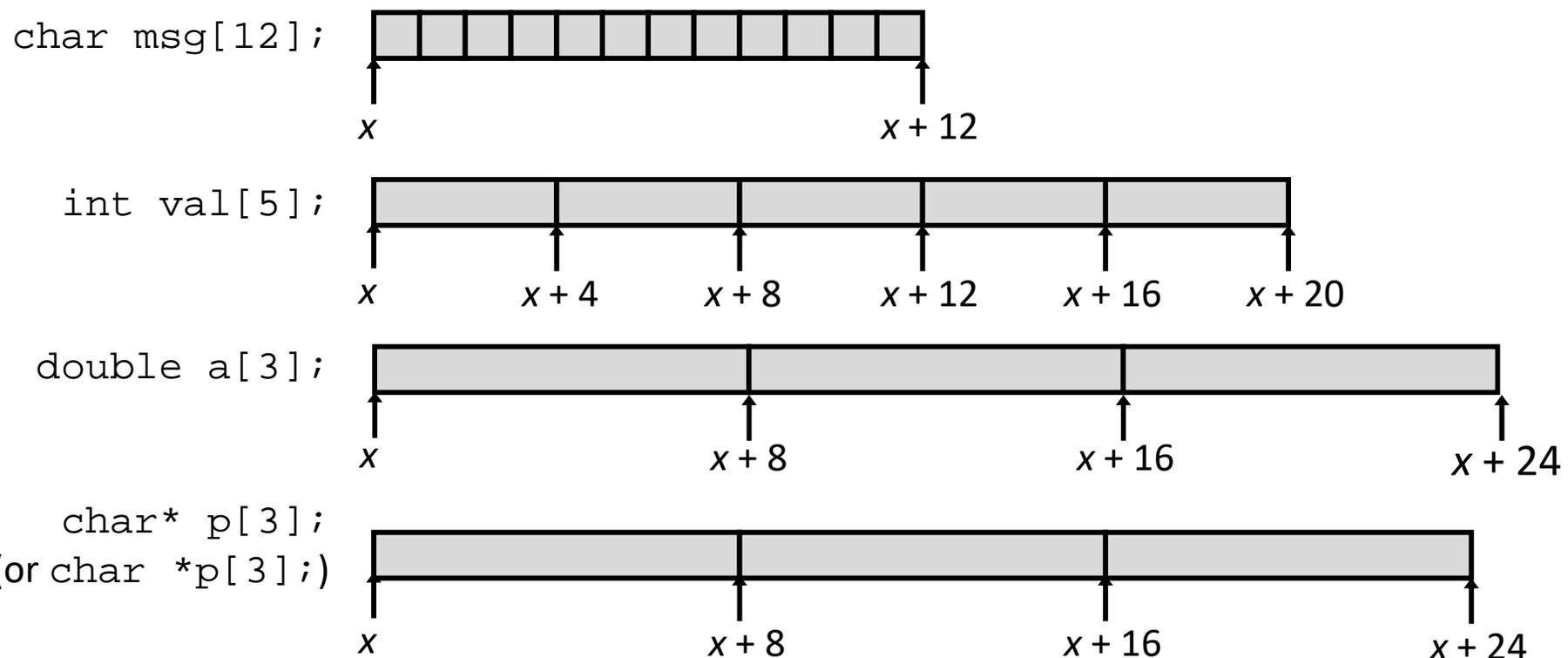
- ❖ Arrays
 - One-dimensional
 - Multi-dimensional (nested)
 - Multi-level
- ❖ Structs
 - Alignment
- ❖ Unions

- ❖ Also: Some C details and how they relate to Java and assembly
 - C arrays are convenient but with some unique/strange rules

Array Allocation

❖ Basic Principle

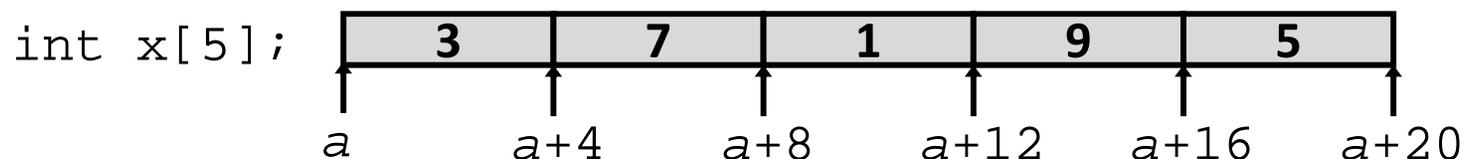
- $T \ A[N]; \rightarrow$ array of data type T and length N
- *Contiguously* allocated region of $N * \text{sizeof}(T)$ bytes
- Identifier A returns address of array (type T^*)



Array Access

❖ Basic Principle

- `T A[N];` → array of data type `T` and length `N`
- Identifier `A` returns address of array (type `T*`)



❖ Reference

Type

Value

<code>x[4]</code>	<code>int</code>	5
<code>x</code>	<code>int *</code>	<code>a</code>
<code>x+1</code>	<code>int *</code>	<code>a + 4</code>
<code>&x[2]</code>	<code>int *</code>	<code>a + 8</code>
<code>x[5]</code>	<code>int</code>	?? (whatever's in memory at addr <code>x+20</code>)
<code>*(x+1)</code>	<code>int</code>	7
<code>x+i</code>	<code>int *</code>	<code>a + 4*i</code>

Array Example

```
typedef int zip_dig[5];
```

```
zip_dig cmu = { 1, 5, 2, 1, 3 };
```

```
zip_dig uw = { 9, 8, 1, 9, 5 };
```

```
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

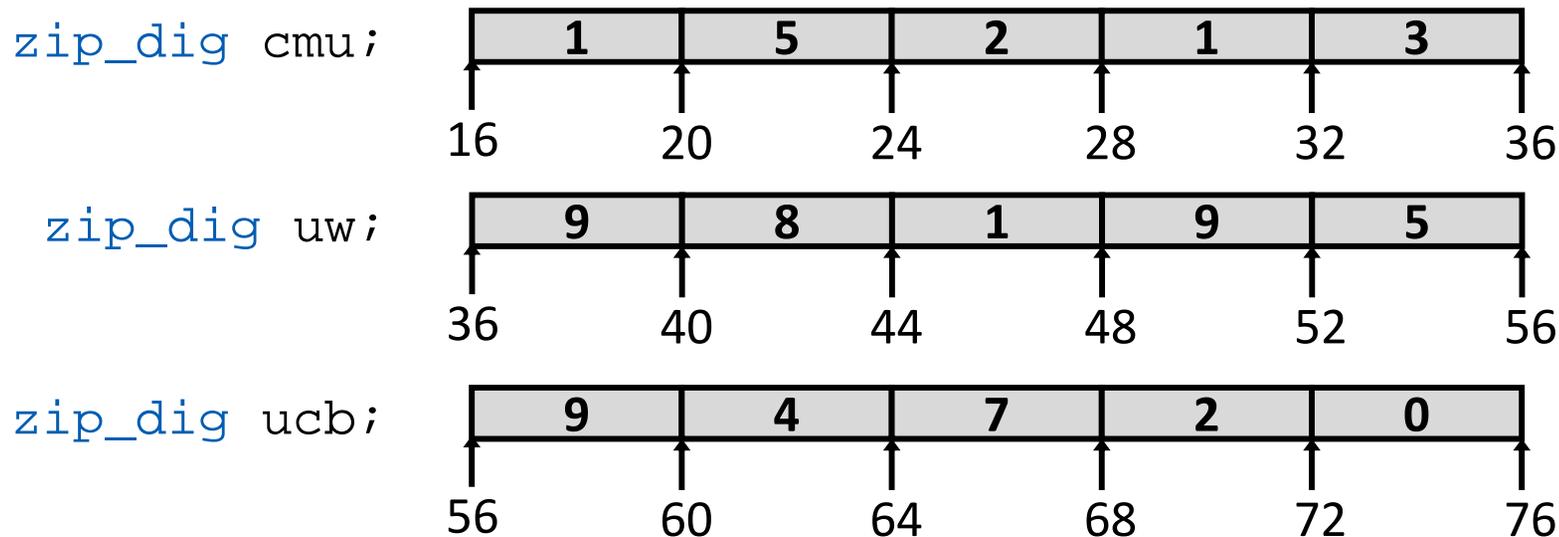
initialization



```
int uw[5] ...
```

Array Example

```
typedef int zip_dig[5];  
  
zip_dig cmu = { 1, 5, 2, 1, 3 };  
zip_dig uw  = { 9, 8, 1, 9, 5 };  
zip_dig ucb = { 9, 4, 7, 2, 0 };
```



- ❖ typedef: Declaration “`zip_dig uw`” equivalent to “`int uw[5]`”
- ❖ Example arrays happened to be allocated in successive 20 byte blocks
 - Not guaranteed to happen in general

Array Accessing Example

```
typedef int zip_dig[5];
```



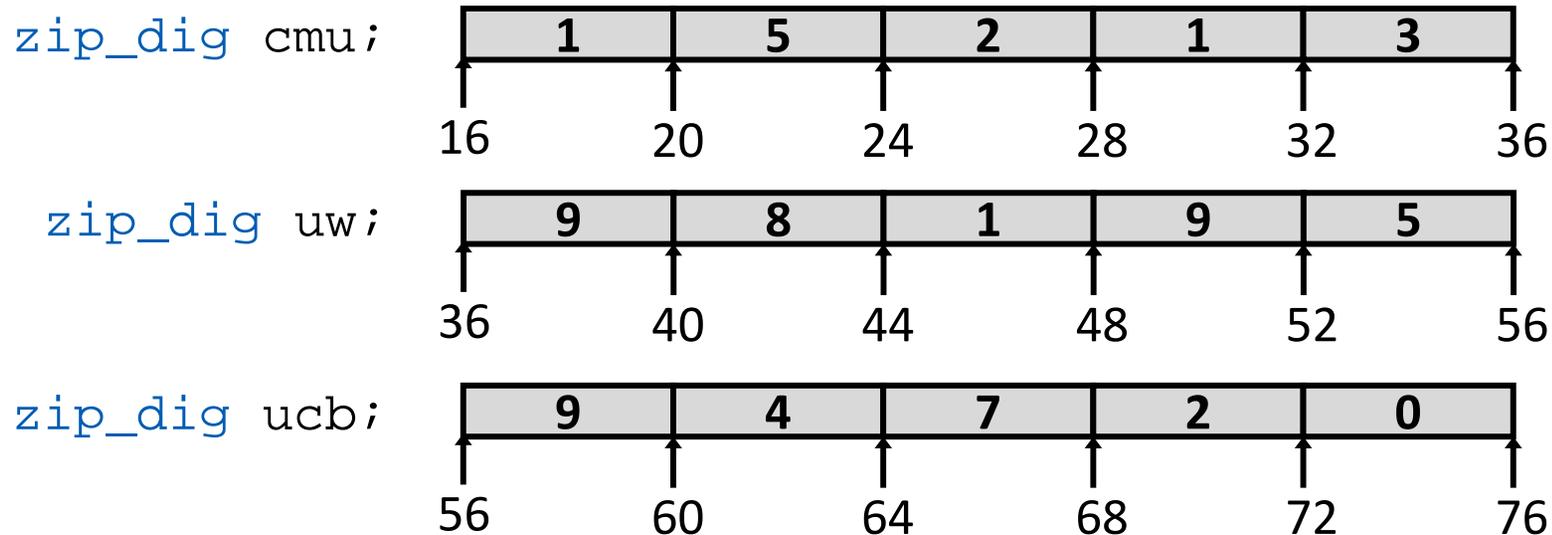
```
int get_digit(zip_dig z, int digit)
{
    return z[digit];
}
```

```
get_digit:
    movl (%rdi,%rsi,4), %eax # z[digit]
```

- Register `%rdi` contains starting address of array
- Register `%rsi` contains array index
- Desired digit at `%rdi+4*%rsi`, so use memory reference `(%rdi,%rsi,4)`

```
typedef int zip_dig[5];
```

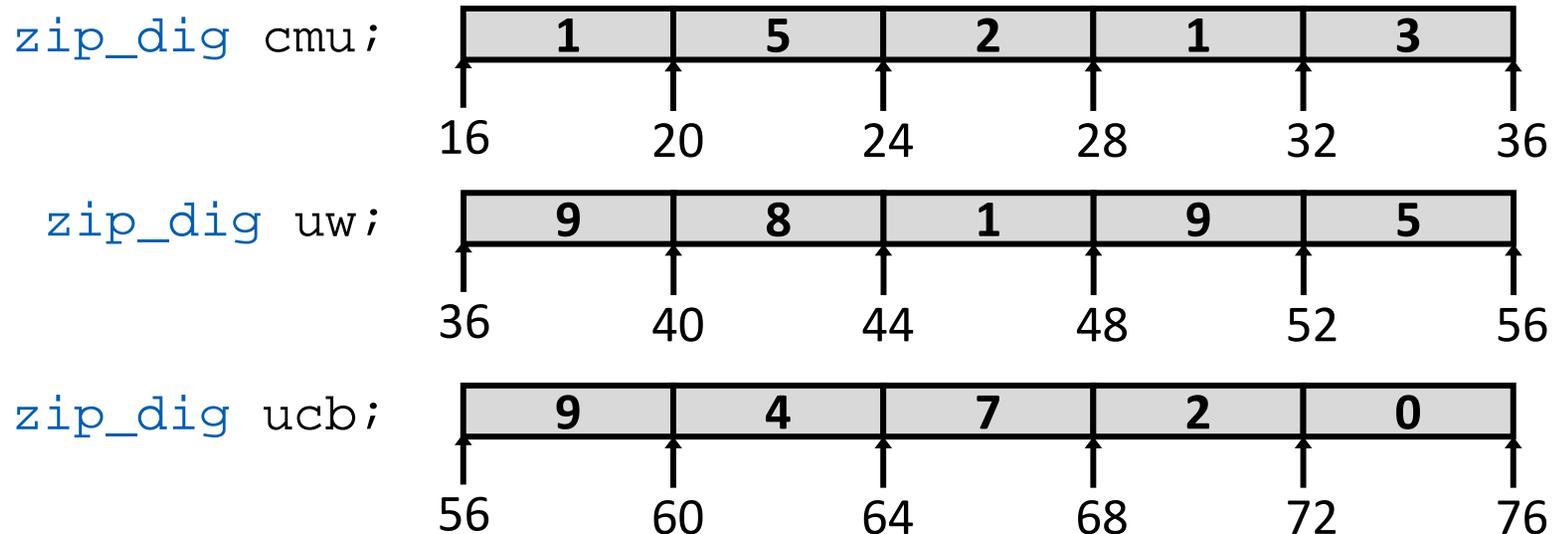
Referencing Examples



<u>Reference</u>	<u>Address</u>	<u>Value</u>	<u>Guaranteed?</u>
uw[3]			
uw[6]			
uw[-1]			
cmu[15]			

```
typedef int zip_dig[5];
```

Referencing Examples



<u>Reference</u>	<u>Address</u>	<u>Value</u>	<u>Guaranteed?</u>
<code>uw[3]</code>	$36 + 4 * 3 = 48$	9	Yes
<code>uw[6]</code>	$36 + 4 * 6 = 60$	4	No
<code>uw[-1]</code>	$36 + 4 * -1 = 32$	3	No
<code>cmu[15]</code>	$16 + 4 * 15 = 76$??	No

- ❖ No bounds checking
- ❖ Example arrays happened to be allocated in successive 20 byte blocks
 - Not guaranteed to happen in general

Array Loop Example

$$zi = 10 * 0 + 9 = 9$$

$$zi = 10 * 9 + 8 = 98$$

$$zi = 10 * 98 + 1 = 981$$

$$zi = 10 * 981 + 9 = 9819$$

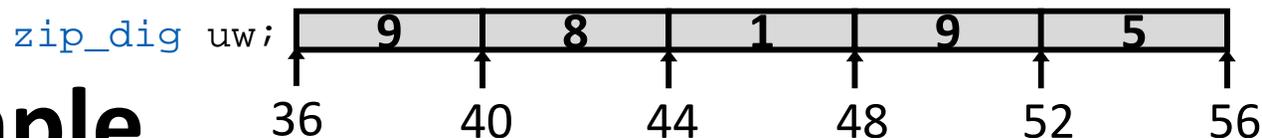
$$zi = 10 * 9819 + 5 = 98195$$

```
typedef int zip_dig[5];
```

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

9	8	1	9	5
---	---	---	---	---

Array Loop Example



❖ Original:

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

❖ Transformed:

- Eliminate loop variable *i*, use pointer *zend* instead
- Convert array code to pointer code
 - Pointer arithmetic on *z*
- Express in do-while form (no test at entrance)

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 5;
    do {
        zi = 10 * zi + *z;
        z++;
    } while (z < zend);
    return zi;
}
```

address just past 5th digit

← Increments by 4 (size of int)

Array Loop Implementation

gcc with -O1

❖ Registers:

```
%rdi z
%rax zi
%rcx zend
```

❖ Computations

- $10 * z_i + *z$ implemented as:
 $*z + 2 * (5 * z_i)$
- $z++$ increments by 4 (size of int)

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 5;
    do {
        zi = 10 * zi + *z;
        z++;
    } while (z < zend);
    return zi;
}
```

```
# %ecx = z
leaq 20(%rdi),%rcx      # rcx = zend = z+5
movl $0,%eax          # rax = zi = 0
.L17:
leal (%rax,%rax,4),%edx # zi + 4*zi = 5*zi
movl (%rdi),%eax       # eax = *z
leal (%rax,%rdx,2),%eax # zi = *z + 2*(5*zi)
addq $4,%rdi           # z++
cmpq %rdi,%rcx        # zend : z
jne .L17               # if != goto loop
```

[[Long Code Demo]]

- ❖ See `arrays_in_c.c` for warning-free code that demonstrates:
 - Arrays created on the Heap and on the Stack
 - Reminder of relative positions of Memory sections
 - `typedef`
 - Macro substitution (`#define`)
 - Implicit pass-by-reference of arrays in C
 - `sizeof ()` with arrays

Code Demo Takeaways

- ❖ Array variables don't have addresses – return address of array
 - Pointers actually have addresses
- ❖ Arrays can be created on Stack, Heap, or Static Data
 - Stack (local var) is temporary
 - Heap (`malloc`) is more permanent, but requires memory management
 - Static Data (global var) can have dangerously broad scope
 - Not automatically initialized!
- ❖ Passing an array to a procedure actually passes a pointer to the array

Nested Array Example

```
typedef int zip_dig[5];
```

```
zip_dig sea[4] =  
{  
  { 9, 8, 1, 9, 5 },  
  { 9, 8, 1, 0, 5 },  
  { 9, 8, 1, 0, 3 },  
  { 9, 8, 1, 1, 5 }  
};
```

Remember, $T A[N]$ is
an array with elements
of type T , with length N

same as:

```
int sea[4][5];
```

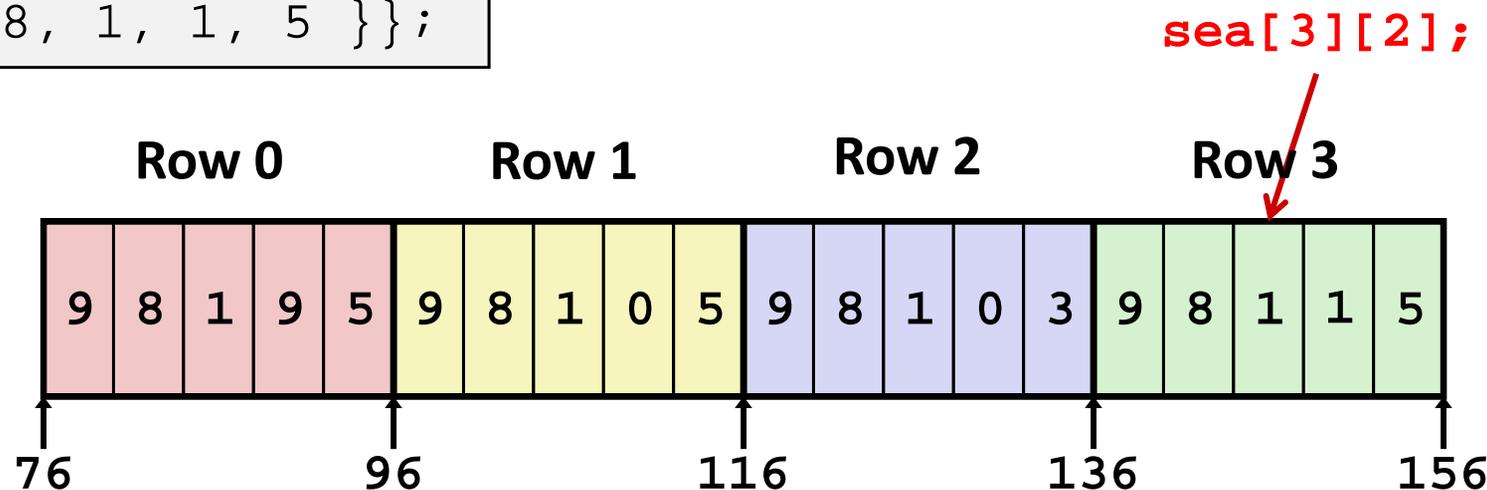
What is the layout in memory?

```
typedef int zip_dig[5];
```

Nested Array Example

```
zip_dig sea[4] =
  { { 9, 8, 1, 9, 5 },
    { 9, 8, 1, 0, 5 },
    { 9, 8, 1, 0, 3 },
    { 9, 8, 1, 1, 5 } };
```

Remember, $T A[N]$ is an array with elements of type T , with length N

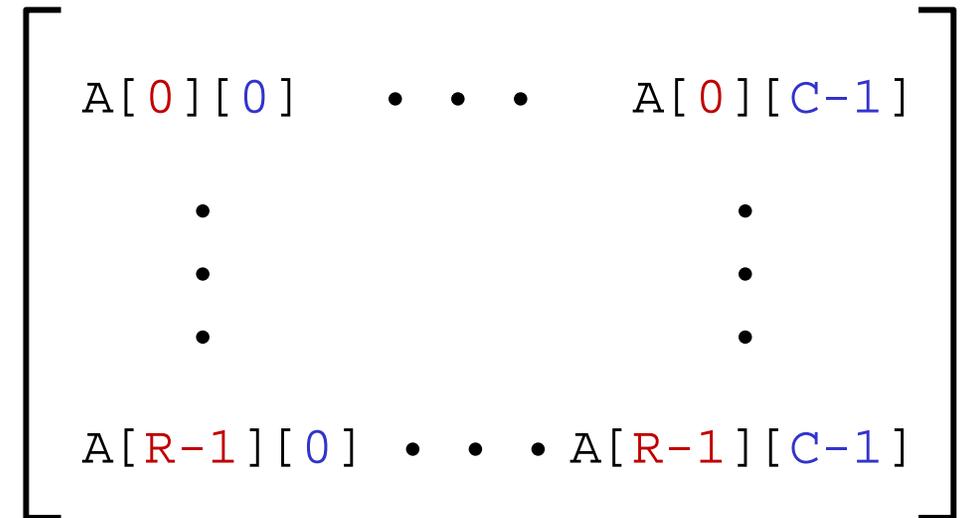


- ❖ “Row-major” ordering of all elements
- ❖ Elements in the same row are contiguous
- ❖ Guaranteed (in C)

Two-Dimensional (Nested) Arrays

❖ Declaration: `T A[R][C];`

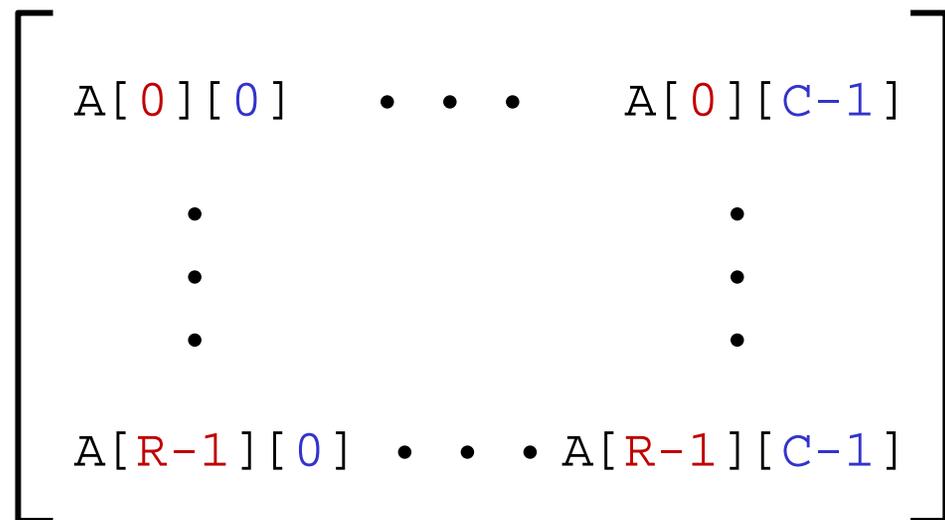
- 2D array of data type `T`
- `R` rows, `C` columns
- Each element requires `sizeof(T)` bytes



❖ Array size?

Two-Dimensional (Nested) Arrays

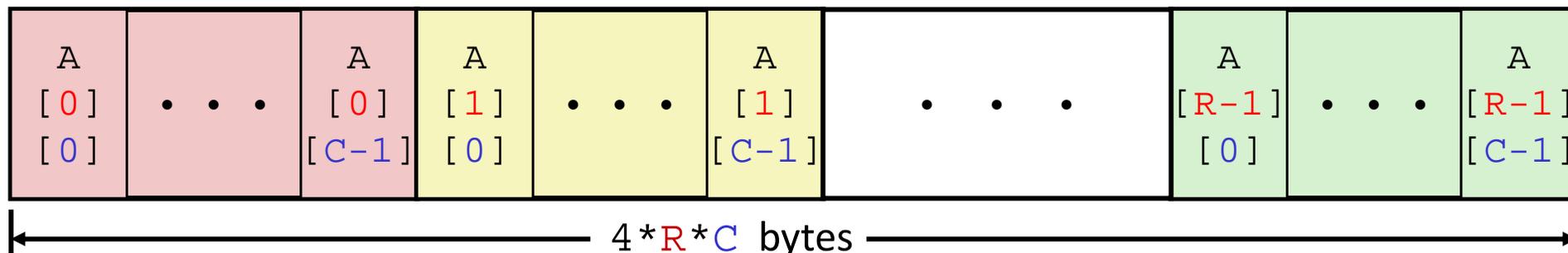
- ❖ Declaration: `T A[R][C];`
 - 2D array of data type `T`
 - `R` rows, `C` columns
 - Each element requires `sizeof(T)` bytes



- ❖ Array size:
 - $R * C * \text{sizeof}(T)$ bytes

- ❖ Arrangement: **row-major** ordering

```
int A[R][C];
```



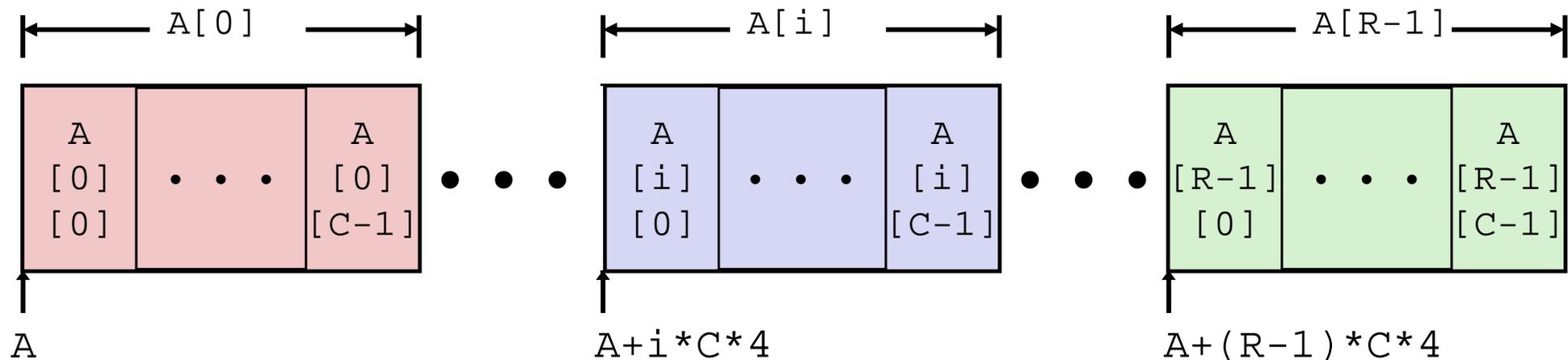
Nested Array Row Access

❖ Row vectors

■ Given $T \ A[R][C]$,

- $A[i]$ is an array of C elements (“row i ”)
- Each element of type T requires K bytes
- A is address of array
- Starting address of row $i = A + i * (C * K)$

```
int A[R][C];
```



Nested Array Row Access Code

```
int* get_sea_zip(int index)
{
    return sea[index];
}
```

```
int sea[4][5] =
    {{ 9, 8, 1, 9, 5 },
     { 9, 8, 1, 0, 5 },
     { 9, 8, 1, 0, 3 },
     { 9, 8, 1, 1, 5 }};
```

- What data type is `sea[index]`?
- What is its starting address?

```
get_sea_zip(int):
    movslq    %edi, %rdi
    leaq     (%rdi,%rdi,4), %rdx
    leaq     0(,%rdx,4), %rax
    addq     $sea, %rax
    ret

sea:
    .long    9
    .long    8
    .long    1
    .long    9
    .long    5
    .long    9
    .long    8
    ...
```

Nested Array Row Access Code

```
int* get_sea_zip(int index)
{
    return sea[index];
}
```

```
int sea[4][5] =
    {{ 9, 8, 1, 9, 5 },
     { 9, 8, 1, 0, 5 },
     { 9, 8, 1, 0, 3 },
     { 9, 8, 1, 1, 5 }};
```

- What data type is `sea[index]`?
- What is its starting address?

```
# %rdi = index
leaq (%rdi,%rdi,4),%rax
leaq sea(,%rax,4),%rax
```

Translation?

Nested Array Row Access Code

```
int* get_sea_zip(int index)
{
    return sea[index];
}
```

```
int sea[4][5] =
    {{ 9, 8, 1, 9, 5 },
     { 9, 8, 1, 0, 5 },
     { 9, 8, 1, 0, 3 },
     { 9, 8, 1, 1, 5 }};
```

```
# %rdi = index
leaq (%rdi,%rdi,4),%rax # 5 * index
leaq sea(,%rax,4),%rax # sea + (20 * index)
```

❖ Row Vector

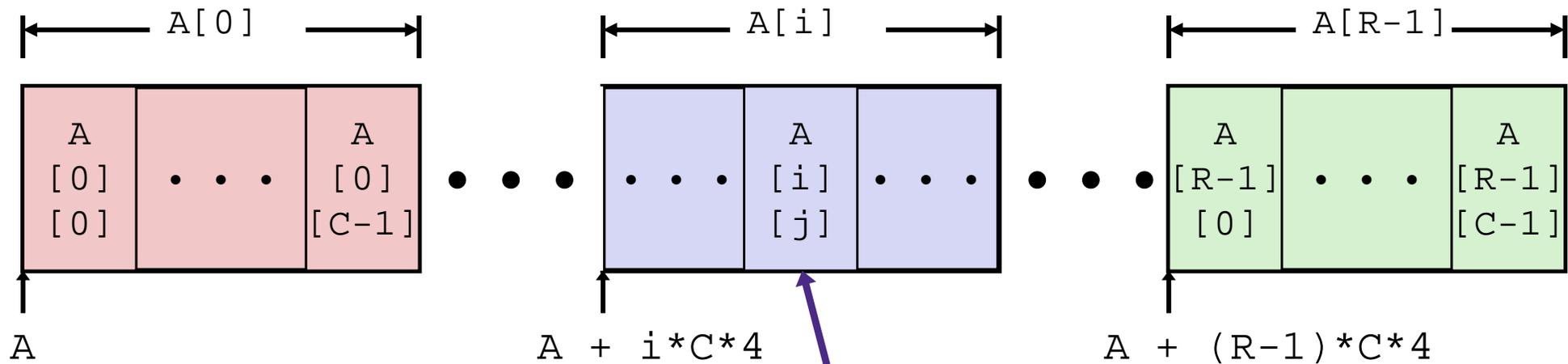
- `sea[index]` is array of 5 ints
- Starting address = `sea+20*index`

❖ Assembly Code

- Computes and returns address
- Compute as: `sea+4*(index+4*index) = sea+20*index`

Nested Array Element Access

```
int A[R][C];
```



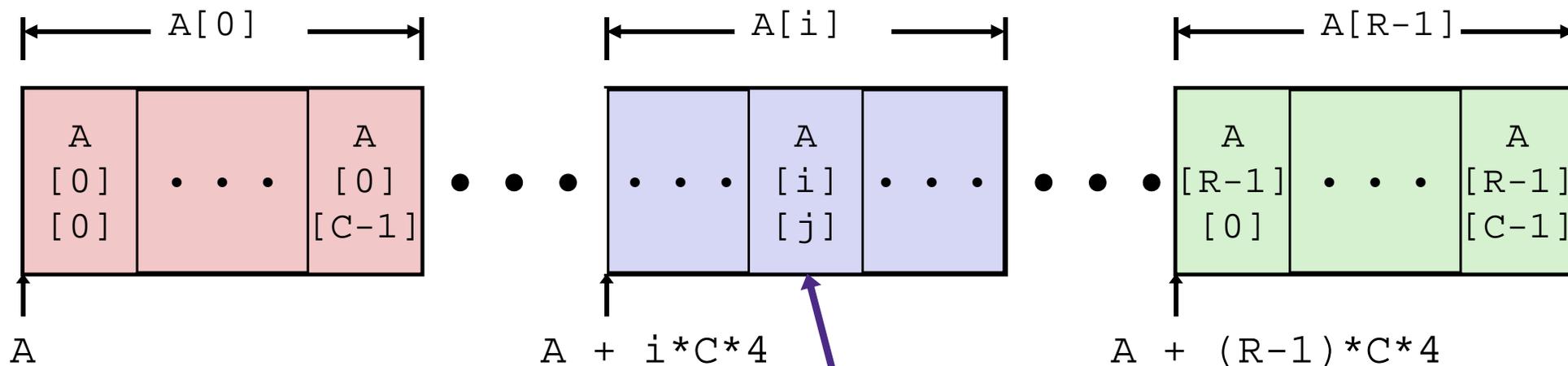
Nested Array Element Access

❖ Array Elements

- $A[i][j]$ is element of type T , which requires K bytes
- Address of $A[i][j]$ is

$$A + i * (C * K) + j * K == A + (i * C + j) * K$$

```
int A[R][C];
```



$$A + i * C * 4 + j * 4$$

Nested Array Element Access Code

```
int* get_sea_digit
(int index, int digit)
{
    return sea[index][digit];
}
```

```
int sea[4][5] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

```
leaq    (%rdi,%rdi,4), %rax    # 5*index
addl    %rax, %rsi            # 5*index+digit
movl    sea(,%rsi,4), %eax    # *(sea + 4*(5*index+digit))
```

❖ Array Elements

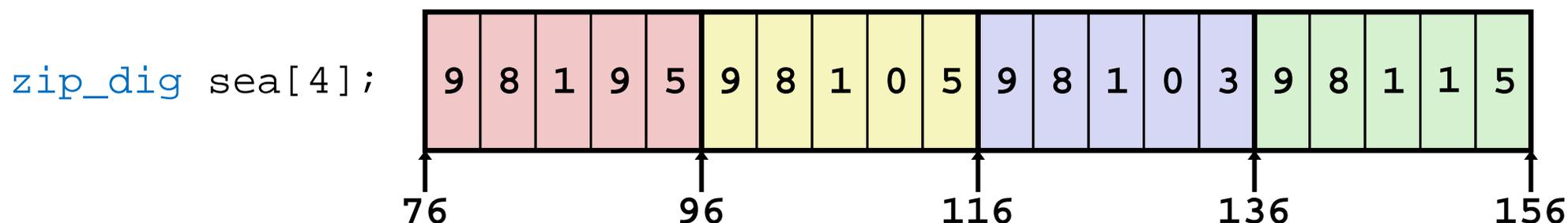
- `sea[index][digit]` is an `int` (`sizeof(int)=4`)
- `Address = sea + 5*4*index + 4*digit`

❖ Assembly Code

- Computes address as: `sea + ((index+4*index) + digit)*4`
- `movl` performs memory reference

```
typedef int zip_dig[5];
```

Strange Referencing Examples



<u>Reference</u>	<u>Address</u>	<u>Value</u>	<u>Guaranteed?</u>
------------------	----------------	--------------	--------------------

`sea[3][3]`

`sea[2][5]`

`sea[2][-1]`

`sea[4][-1]`

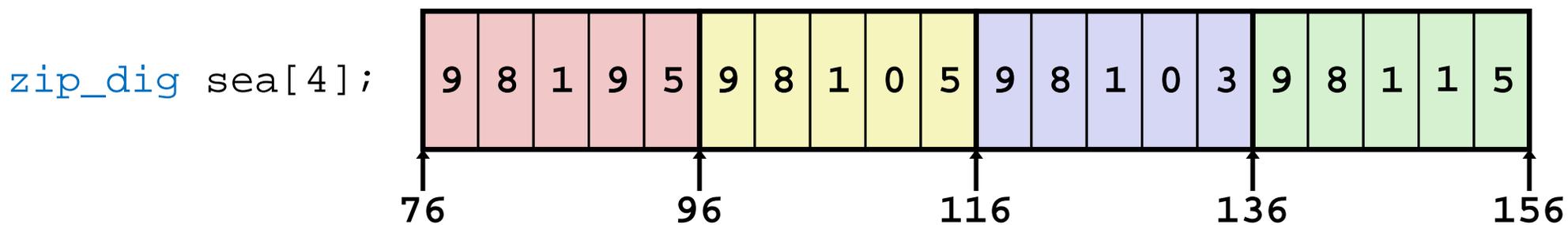
`sea[0][19]`

`sea[0][-1]`

- Code does not do any bounds checking
- Ordering of elements within array guaranteed

```
typedef int zip_dig[5];
```

Strange Referencing Examples



<u>Reference</u>	<u>Address</u>	<u>Value</u>	<u>Guaranteed?</u>
sea[3][3]	$76+20*3+4*3 = 148$	1	Yes
sea[2][5]	$76+20*2+4*5 = 136$	9	Yes
sea[2][-1]	$76+20*2+4*-1 = 112$	5	Yes
sea[4][-1]	$76+20*4+4*-1 = 152$	5	Yes
sea[0][19]	$76+20*0+4*19 = 152$	5	Yes
sea[0][-1]	$76+20*0+4*-1 = 72$??	No

- Code does not do any bounds checking
- Ordering of elements within array guaranteed

Multi-Level Array Example

Multi-Level Array Declaration(s):

```
int cmu[5] = { 1, 5, 2, 1, 3 };  
int uw[5] = { 9, 8, 1, 9, 5 };  
int ucb[5] = { 9, 4, 7, 2, 0 };
```

```
int* univ[3] = {uw, cmu, ucb};
```

2D Array Declaration:

```
zip_dig univ2D[3] = {  
    { 9, 8, 1, 9, 5 },  
    { 1, 5, 2, 1, 3 },  
    { 9, 4, 7, 2, 0 }  
};
```

Is a multi-level array the same thing as a 2D array?

NO

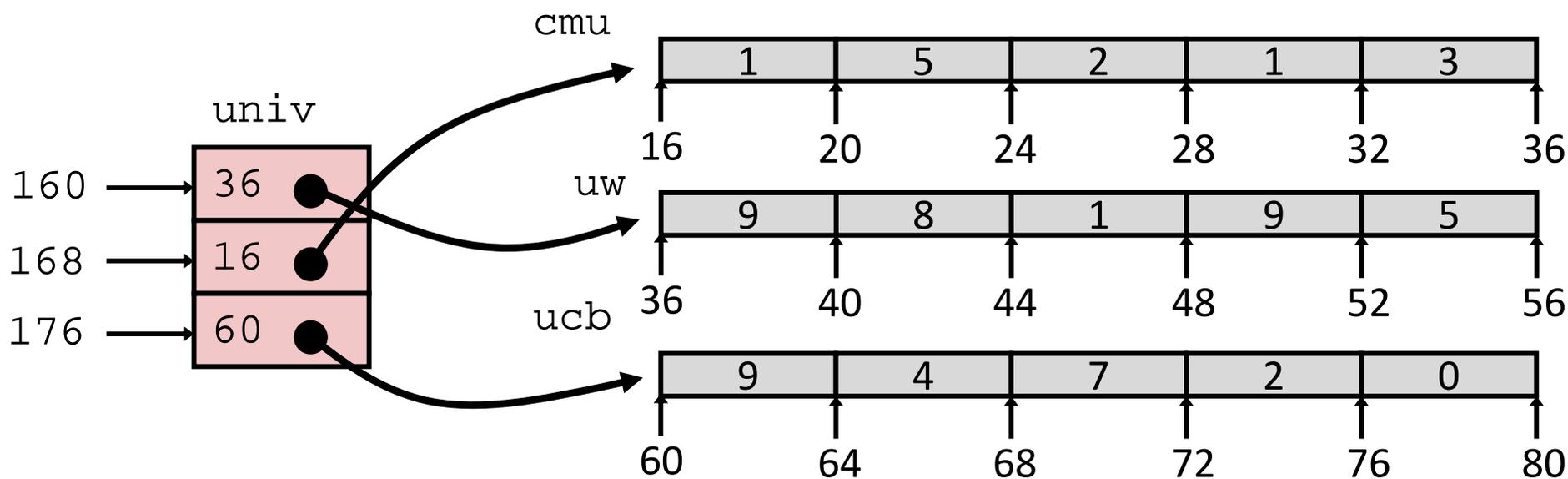
One array declaration = one contiguous block of memory

Multi-Level Array Example

```
int cmu[5] = { 1, 5, 2, 1, 3 };
int uw[5] = { 9, 8, 1, 9, 5 };
int ucb[5] = { 9, 4, 7, 2, 0 };
```

```
int* univ[3] = {uw, cmu, ucb};
```

- ❖ Variable `univ` denotes array of 3 elements
- ❖ Each element is a pointer
 - 8 bytes each
- ❖ Each pointer points to array of `ints`



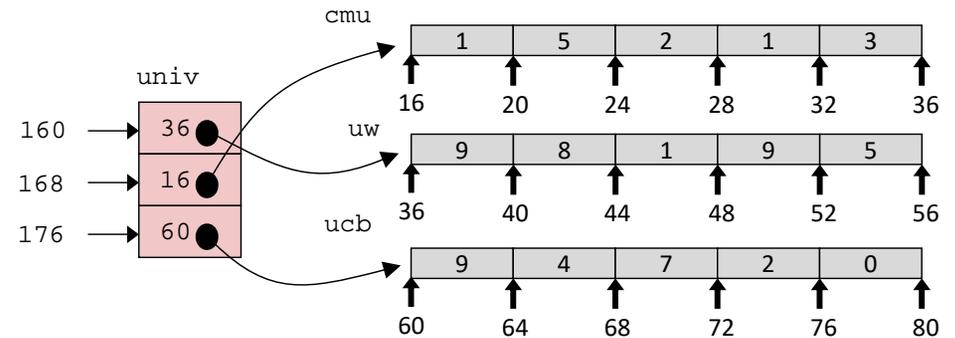
Note: this is how Java represents multi-dimensional arrays

Element Access in Multi-Level Array

```

int get_univ_digit
(int index, int digit)
{
    return univ[index][digit];
}

```



```

salq    $2, %rsi           # rsi = 4*digit
addq    univ(,%rdi,8), %rsi # p = univ[index] + 4*digit
movl    (%rsi), %eax       # return *p
ret

```

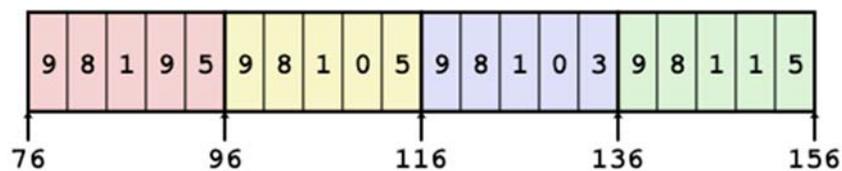
❖ Computation

- Element access $\text{Mem}[\text{Mem}[\text{univ} + 8 * \text{index}] + 4 * \text{digit}]$
- Must do **two memory reads**
 - First get pointer to row array
 - Then access element within array
- But allows inner arrays to be different lengths (not in this example)

Array Element Accesses

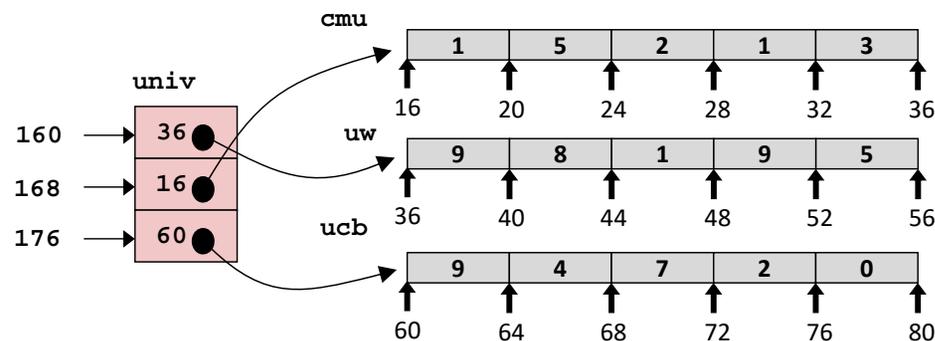
Nested array

```
int get_sea_digit
(int index, int digit)
{
    return sea[index][digit];
}
```



Multi-level array

```
int get_univ_digit
(int index, int digit)
{
    return univ[index][digit];
}
```

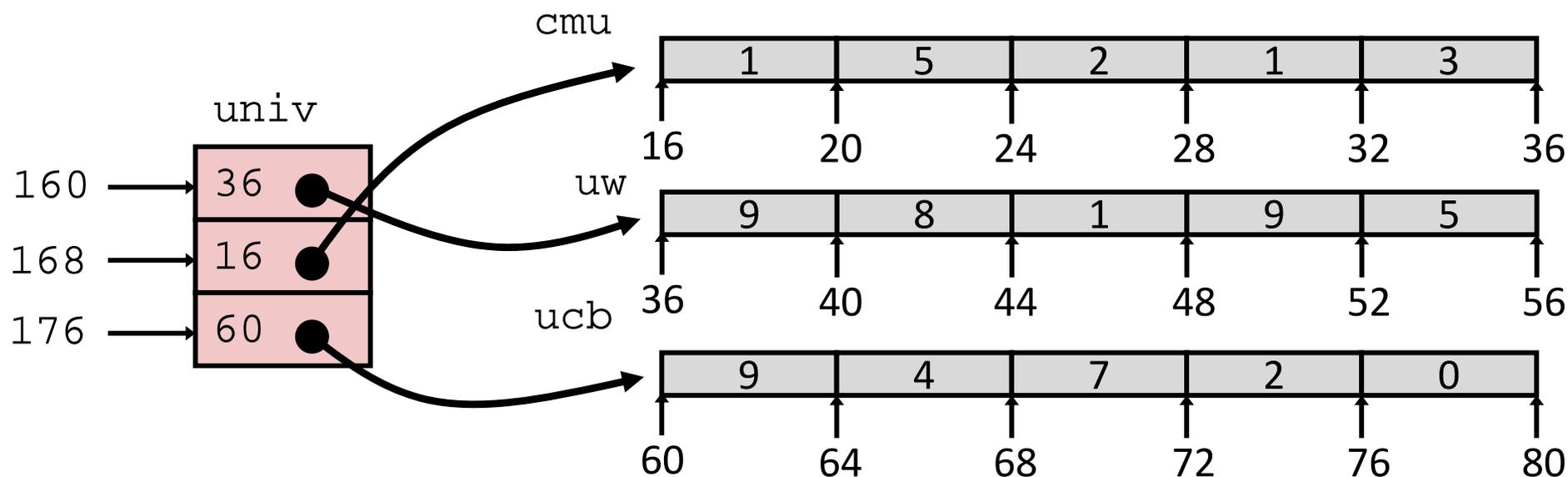


Access *looks* the same, but it isn't:

$$\text{Mem}[\text{sea} + 20 * \text{index} + 4 * \text{digit}]$$

$$\text{Mem}[\text{Mem}[\text{univ} + 8 * \text{index}] + 4 * \text{digit}]$$

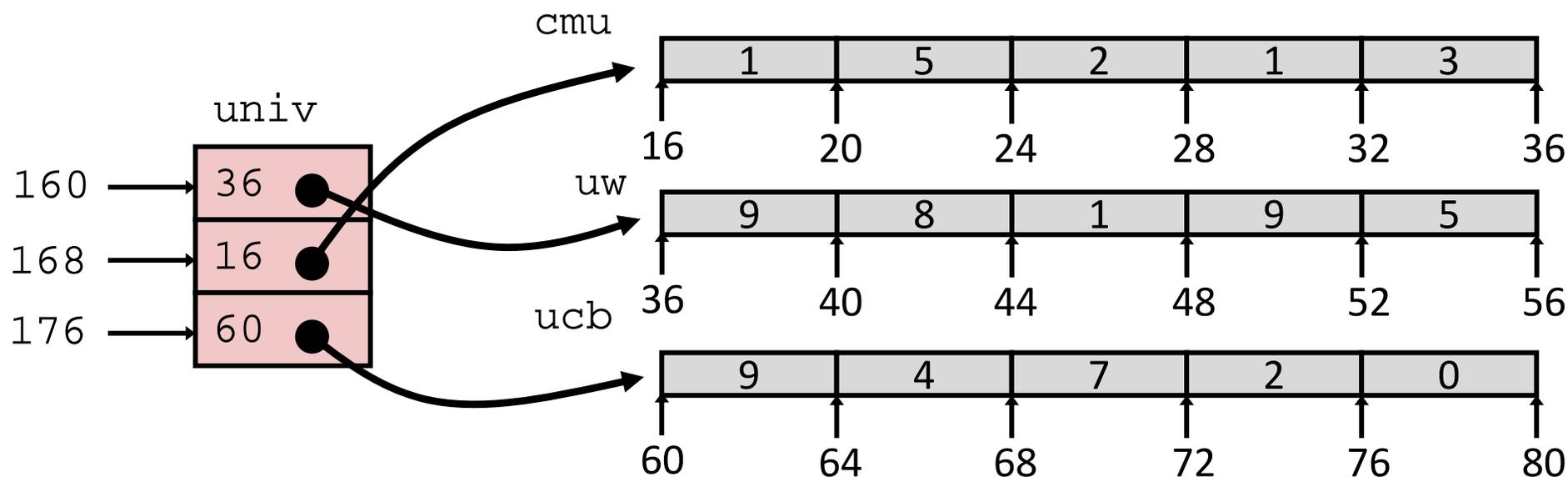
Strange Referencing Examples



<u>Reference</u>	<u>Address</u>	<u>Value</u>	<u>Guaranteed?</u>
<code>univ[2][3]</code>			
<code>univ[1][5]</code>			
<code>univ[2][-2]</code>			
<code>univ[3][-1]</code>			
<code>univ[1][12]</code>			

- C Code does not do any bounds checking
- Location of each lower-level array in memory is not guaranteed

Strange Referencing Examples



<u>Reference</u>	<u>Address</u>	<u>Value</u>	<u>Guaranteed?</u>
<code>univ[2][3]</code>	$60+4*3 = 72$	2	Yes
<code>univ[1][5]</code>	$16+4*5 = 36$	9	No
<code>univ[2][-2]</code>	$60+4*-2 = 52$	5	No
<code>univ[3][-1]</code>	#@%!^??	??	No
<code>univ[1][12]</code>	$16+4*12 = 64$	4	No

- C Code does not do any bounds checking
- Location of each lower-level array in memory is *not* guaranteed

Summary

- ❖ Contiguous allocations of memory
- ❖ **No bounds checking** (and no default initialization)
- ❖ Can usually be treated like a pointer to first element
- ❖ `int a[4][5];` → array of arrays
 - all levels in one contiguous block of memory
- ❖ `int* b[4];` → array of pointers to arrays
 - First level in one contiguous block of memory
 - Each element in the first level points to another “sub” array
 - Parts anywhere in memory