

The Hardware/Software Interface

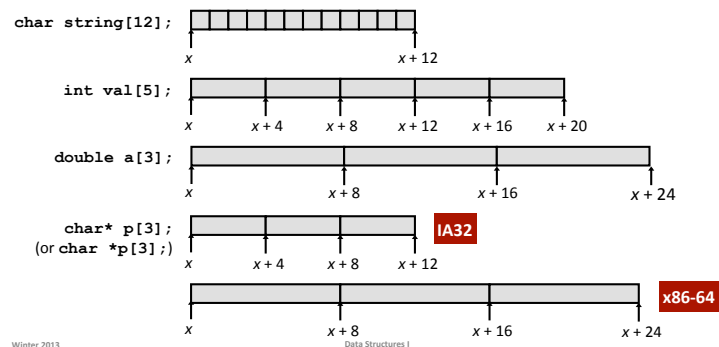
CSE351 Winter 2013

Data Structures I: Arrays

Array Allocation

Basic Principle

- $T A[N]$;
- Array of data type T and length N
- *Contiguously* allocated region of $N * \text{sizeof}(T)$ bytes



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Data Structures in Assembly

- **Arrays**
 - One-dimensional
 - Multi-dimensional (nested)
 - Multi-level
- **Structs**
 - Alignment
- **Unions**

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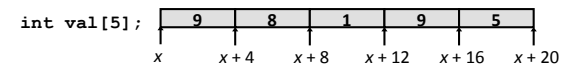
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Array Access

Basic Principle

- $T A[N]$;
- Array of data type T and length N
- Identifier A can be used as a pointer to array element 0: Type T^*



Reference Type Value

- $\text{val}[4]$ int 5
- val int* x
- $\text{val}+1$ int* $x+4$
- $\&\text{val}[2]$ int* $x+8$
- $\text{val}[5]$ int ??
- $\text{*(val}+1)$ int 8
- $\text{val}+i$ int* $x+4*i$

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Array Example

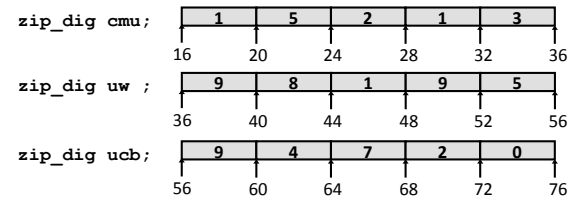
```
typedef int zip_dig[5];

zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig uw = { 9, 8, 1, 9, 5 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

Array Example

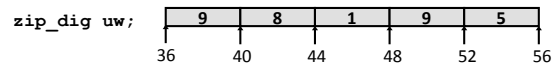
```
typedef int zip_dig[5];

zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig uw = { 9, 8, 1, 9, 5 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```



- Declaration "zip_dig uw" equivalent to "int uw[5]"
- Example arrays were allocated in successive 20 byte blocks
 - Not guaranteed to happen in general

Array Accessing Example



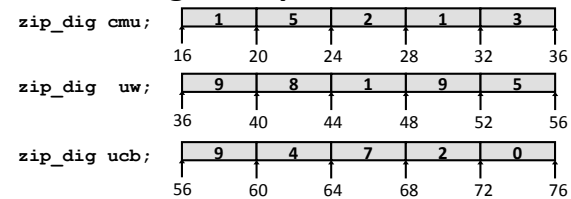
```
int get_digit
(zip_dig z, int dig)
{
    return z[dig];
}
```

IA32

```
# %edx = z
# %eax = dig
movl (%edx,%eax,4),%eax # z[dig]
```

- Register %edx contains starting address of array
- Register %eax contains array index
- Desired digit at $4 * \text{\%eax} + \text{\%edx}$
- Use memory reference ($\text{\%edx}, \text{\%eax}, 4$)

Referencing Examples



- | Reference | Address | Value | Guaranteed? |
|-----------|--------------------|-------|-------------|
| uw[3] | $36 + 4 * 3 = 48$ | 9 | Yes |
| uw[6] | $36 + 4 * 6 = 60$ | 4 | No |
| uw[-1] | $36 + 4 * -1 = 32$ | 3 | No |
| cmu[15] | $16 + 4 * 15 = 76$ | ?? | No |
- No bounds checking
 - Location of each separate array in memory is not guaranteed

Array Loop Example

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

Array Loop Example

Original

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

Transformed

- Eliminate loop variable *i*, use pointer *zend* instead
- Convert array code to pointer code
 - Pointer arithmetic on *z*
- Express in do-while form (no test at entrance)

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 4;
    do {
        zi = 10 * zi + *z;
        z++;
    } while (z <= zend);
    return zi;
}
```

Array Loop Implementation (IA32)

Registers

%ecx *z*
%eax *zi*
%ebx *zend*

Computations

- $10 * zi + *z$ implemented as $*z + 2 * (5 * zi)$
- z++* increments by 4

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 4;
    do {
        zi = 10 * zi + *z;
        z++;
    } while (z <= zend);
    return zi;
}
```

```
# %ecx = z
xorl %eax,%eax      # zi = 0
leal 16(%ecx),%ebx  # zend = z+4
.L59:
leal (%eax,%eax,4),%edx # zi + 4*zi = 5*zi
movl (%ecx),%eax     # *z
addl $4,%ecx        # z++
leal (%eax,%edx,2),%eax # zi = *z + 2*(5*zi)
cmpl %ebx,%ecx     # z : zend
jle .L59           # if <= goto loop
```

Nested Array Example

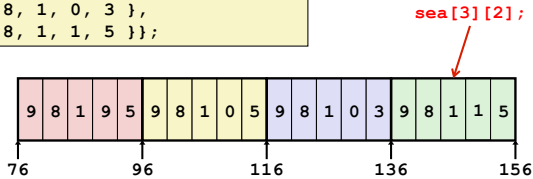
```
#define PCOUNT 4
zip_dig sea[PCOUNT] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

Remember, $T \mathbf{A}[N]$ is an array with elements of type *T*, with length *N*

Nested Array Example

```
#define Pcount 4
zipDig sea[Pcount] =
{ { 9, 8, 1, 9, 5 },
  { 9, 8, 1, 0, 5 },
  { 9, 8, 1, 0, 3 },
  { 9, 8, 1, 1, 5 } };
```

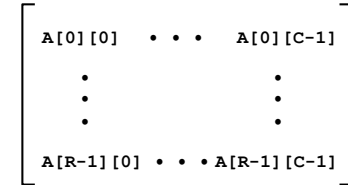
Remember, $T A[N]$ is an array with elements of type T , with length N



- "Row-major" ordering of all elements
- Guaranteed?

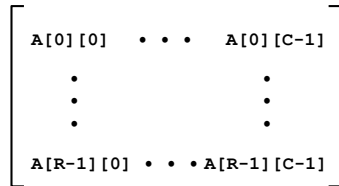
Multidimensional (Nested) Arrays

- Declaration
 - $T A[R][C]$;
 - 2D array of data type T
 - R rows, C columns
 - Type T element requires K bytes
- Array size?

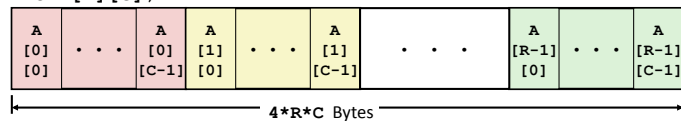


Multidimensional (Nested) Arrays

- Declaration
 - $T A[R][C]$;
 - 2D array of data type T
 - R rows, C columns
 - Type T element requires K bytes
- Array size
 - $R * C * K$ bytes
- Arrangement
 - Row-major ordering



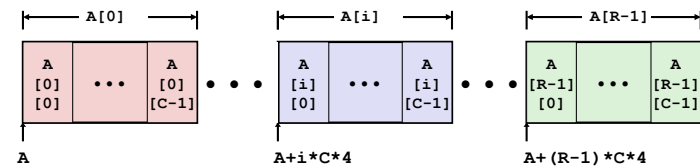
```
int A[R][C];
```



Nested Array Row Access

- Row vectors
 - $T A[R][C]$: $A[i]$ is array of C elements
 - Each element of type T requires K bytes
 - Starting address $A + i * (C * K)$

```
int A[R][C];
```



Nested Array Row Access Code

```
int *get_sea_zip(int index)
{
    return sea[index];
}
```

```
#define PCOUNT 4
zip_dig sea[PCOUNT] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

Nested Array Row Access Code

```
int *get_sea_zip(int index)
{
    return sea[index];
}
```

```
#define PCOUNT 4
zip_dig sea[PCOUNT] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

- What data type is sea[index]?
- What is its starting address?

```
# %eax = index
leal (%eax,%eax,4),%eax
leal sea(,%eax,4),%eax
```

Translation?

Nested Array Row Access Code

```
int *get_sea_zip(int index)
{
    return sea[index];
}
```

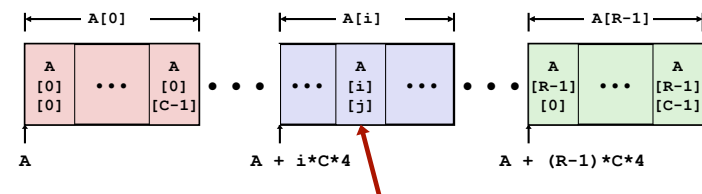
```
#define PCOUNT 4
zip_dig sea[PCOUNT] =
{{ 9, 8, 1, 9, 5 },
 { 9, 8, 1, 0, 5 },
 { 9, 8, 1, 0, 3 },
 { 9, 8, 1, 1, 5 }};
```

```
# %eax = index
leal (%eax,%eax,4),%eax # 5 * index
leal sea(,%eax,4),%eax # sea + (20 * index)
```

- **Row Vector**
 - sea[index] is array of 5 ints
 - Starting address sea+20*index
- **IA32 Code**
 - Computes and returns address
 - Compute as sea+4*(index+4*index)=sea+20*index

Nested Array Row Access

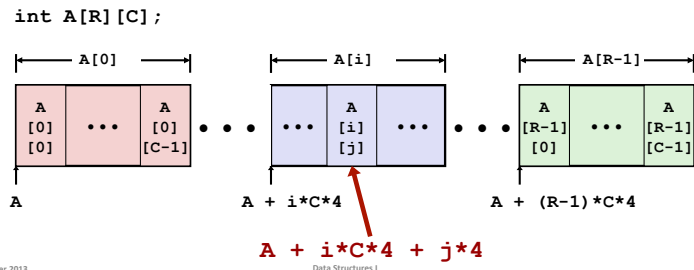
```
int A[R][C];
```



Nested Array Row Access

Array Elements

- $A[i][j]$ is element of type T, which requires K bytes
- Address $A + i * (C * K) + j * K = A + (i * C + j) * K$



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Nested Array Element Access Code

```
int get_sea_digit
(int index, int dig)
{
    return sea[index][dig];
}
```

```
# %ecx = dig
# %eax = index
leal 0(,%ecx,4),%edx    # 4*dig
leal (%eax,%eax,4),%eax # 5*index
movl sea(%edx,%eax,4),%eax # *(sea + 4*dig + 20*index)
```

Array Elements

- `sea[index][dig]` is int
- Address: $sea + 20 * index + 4 * dig$

IA32 Code

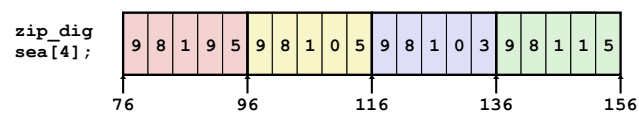
- Computes address $sea + 4 * dig + 4 * (index + 4 * index)$
- `movl` performs memory reference

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Strange Referencing Examples



Reference	Address	Value	Guaranteed?
<code>sea[3][3]</code>	$76 + 20 * 3 + 4 * 3 = 148$	1	Yes
<code>sea[2][5]</code>	$76 + 20 * 2 + 4 * 5 = 136$	9	Yes
<code>sea[2][-1]</code>	$76 + 20 * 2 + 4 * -1 = 112$	5	Yes
<code>sea[4][-1]</code>	$76 + 20 * 4 + 4 * -1 = 152$	5	Yes
<code>sea[0][19]</code>	$76 + 20 * 0 + 4 * 19 = 152$	5	Yes
<code>sea[0][-1]</code>	$76 + 20 * 0 + 4 * -1 = 72$??	No

- Code does not do any bounds checking
- Ordering of elements within array guaranteed

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Multi-Level Array Example

```
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig uw = { 9, 8, 1, 9, 5 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

```
#define UCOUNT 3
int *univ[UCOUNT] = {uw, cmu, ucb};
```

Same thing as a 2D array?

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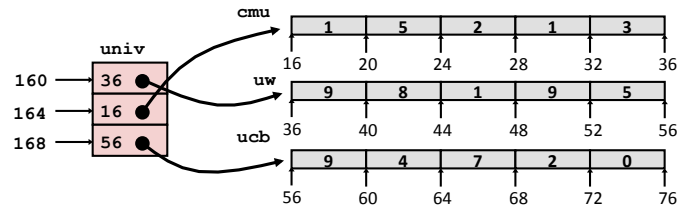
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Multi-Level Array Example

```
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig uw  = { 9, 8, 1, 9, 5 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

```
#define UCOUNT 3
int *univ[UCOUNT] = {uw, cmu, ucb};
```

- Variable univ denotes array of 3 elements
- Each element is a pointer
 - 4 bytes
- Each pointer points to array of ints



Note: this is how Java represents multi-dimensional arrays.

Element Access in Multi-Level Array

```
int get_univ_digit
(int index, int dig)
{
    return univ[index][dig];
}
```

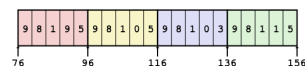
```
# %ecx = index
# %eax = dig
leal 0(,%ecx,4),%edx # 4*index
movl univ(%edx),%edx # Mem[univ+4*index]
movl (%edx,%eax,4),%eax # Mem[...+4*dig]
```

- Computation (IA32)
 - Element access Mem[Mem[univ+4*index]+4*dig]
 - Must do two memory reads
 - First get pointer to row array
 - Then access element within array

Array Element Accesses

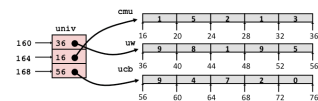
Nested array

```
int get_sea_digit
(int index, int dig)
{
    return sea[index][dig];
}
```



Multi-level array

```
int get_univ_digit
(int index, int dig)
{
    return univ[index][dig];
}
```

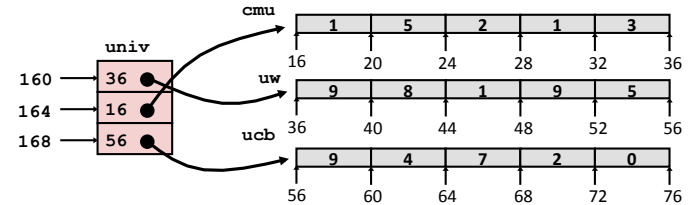


Access looks similar, but it isn't:

Mem[sea+20*index+4*dig]

Mem[Mem[univ+4*index]+4*dig]

Strange Referencing Examples



Reference	Address	Value	Guaranteed?
univ[2][3]	56+4*3 = 68	2	Yes
univ[1][5]	16+4*5 = 36	9	No
univ[2][-1]	56+4*-1 = 52	5	No
univ[3][-1]	??	??	No
univ[1][12]	16+4*12 = 64	7	No

- Code does not do any bounds checking
- Location of each lower-level array in memory is not guaranteed

Using Nested Arrays

```
#define N 16
typedef int fix_matrix[N][N];

/* Compute element i,k of
   fixed matrix product */
int fix_prod_ele
(fix_matrix a, fix_matrix b,
 int i, int k)
{
    int j;
    int result = 0;
    for (j = 0; j < N; j++)
        result += a[i][j]*b[j][k];
    return result;
}
```

Using Nested Arrays

Strengths

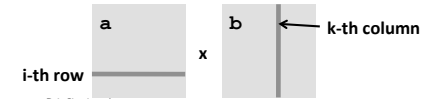
- Generates very efficient assembly code
- Avoids multiply in index computation

Limitation

- Only works for fixed array size

```
#define N 16
typedef int fix_matrix[N][N];

/* Compute element i,k of
   fixed matrix product */
int fix_prod_ele
(fix_matrix a, fix_matrix b,
 int i, int k)
{
    int j;
    int result = 0;
    for (j = 0; j < N; j++)
        result += a[i][j]*b[j][k];
    return result;
}
```



Dynamic Nested Arrays

Strength

- Can create matrix of any size

Programming

- Must do index computation explicitly

Performance

- Accessing single element costly
- Must do multiplication

```
int * new_var_matrix(int n)
{
    return (int *)
        calloc(sizeof(int), n*n);
}
```

```
int var_ele
(int *a, int i, int j, int n)
{
    return a[i*n+j];
}
```

```
movl 12(%ebp),%eax    # i
movl 8(%ebp),%edx     # a
imull 20(%ebp),%eax   # n*i
addl 16(%ebp),%eax    # n*i+j
movl (%edx,%eax,4),%eax # Mem[a+4*(i*n+j)]
```

Arrays in C

Contiguous allocations of memory

No bounds checking

Can usually be treated like a pointer to first element