Introduction to Data Management CSE 344

Lectures 18: Design Theory

Announcements

- HW6 and WQ6 are out
 - Due on Monday, 11/21
- Back to Tues/Wed cycle for HW7-8 and WQ7
- Today and next lecture:
 - Design theory (3.1-3.4)

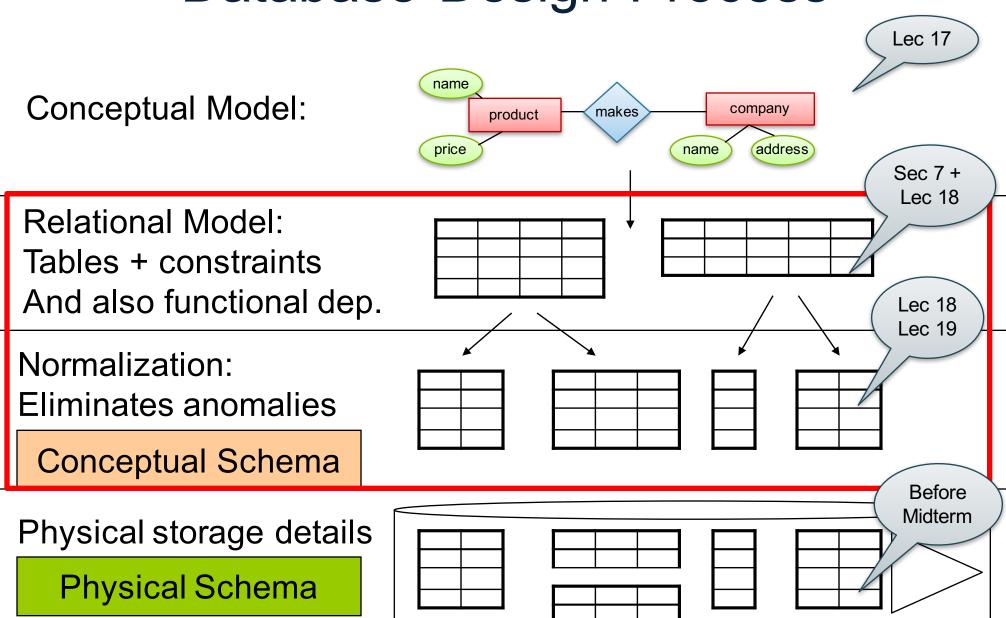
Where are we?

- First half of 344:
 - Data models: instance, schema, languages
 - Relational and NoSQL
 - Query processing
- Second half of 344: Using DBMSs effectively
 - Conceptual design
 - Transactions
 - Parallel databases

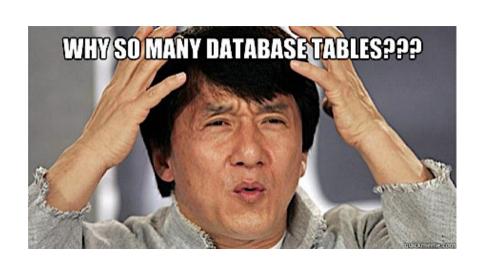
What is this class about?

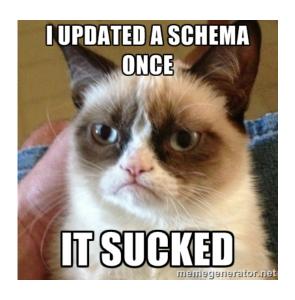
- Focus: Using DBMSs
- Relational Data Model
 - SQL, Relational Algebra, Relational Calculus, datalog
- Semistructured Data Model
 - JSon, CouchDB (NoSQL)
- Conceptual design
 - E/R diagrams, Views, and Database normalization
- Transactions
- Parallel databases, MapReduce, and Spark
- Data integration and data cleaning

Database Design Process



What makes good schemas?





Relational Schema Design

Name	SSN	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

Primary key is thus (SSN, PhoneNumber)

What is the problem with this schema?

Relational Schema Design

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

Anomalies:

- Redundancy = repeat data
- Update anomalies = what if Fred moves to "Bellevue"?
- Deletion anomalies = what if Joe deletes his phone number?

Relation Decomposition

Break the relation into two:

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

<u>SSN</u>	<u>PhoneNumber</u>	
123-45-6789	206-555-1234	
123-45-6789	206-555-6543	
987-65-4321	908-555-2121	

Anomalies have gone:

- No more repeated data
- Easy to move Fred to "Bellevue" (how ?)
- Easy to delete all Joe's phone numbers (how ?)

Relational Schema Design (or Logical Design)

How do we do this systematically?

Start with some relational schema

- Find out its <u>functional dependencies</u> (FDs)
- Use FDs to normalize the relational schema

Functional Dependencies (FDs)

Definition

If two tuples agree on the attributes

$$A_1, A_2, ..., A_n$$

then they must also agree on the attributes

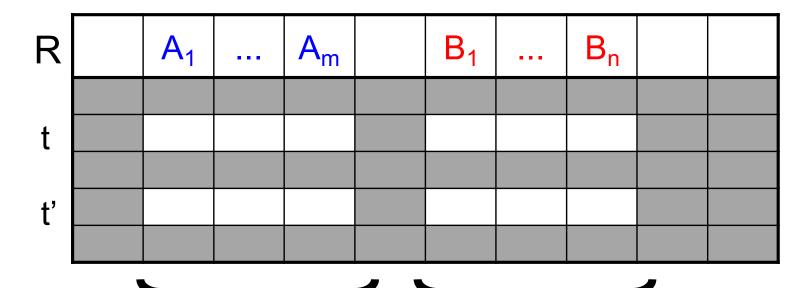
Formally:

$$A_1...A_n$$
 determines $B_1...B_m$

$$A_1, A_2, ..., A_n \rightarrow B_1, B_2, ..., B_m$$

Functional Dependencies (FDs)

<u>Definition</u> $A_1, ..., A_m \rightarrow B_1, ..., B_n$ holds in R if: $∀t, t' \in R,$ $(t.A_1 = t'.A_1 \land ... \land t.A_m = t'.A_m \rightarrow t.B_1 = t'.B_1 \land ... \land t.B_n = t'.B_n)$



if t, t' agree here then t, t' agree here

An FD holds, or does not hold on an instance:

EmplD	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

EmpID → Name, Phone, Position

Position → Phone

but not Phone > Position

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876 ←	Salesrep
E1111	Smith	9876 ←	Salesrep
E9999	Mary	1234	Lawyer

Position → Phone

EmpID	Name	Phone	Position
E0045	Smith	1234 →	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234 →	Lawyer

But not Phone → Position

name → color
category → department
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99

Do all the FDs hold on this instance?

Example name > color category → department color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	49
Gizmo	Stationary	Green	Office-supp.	59

Terminology

FD holds or does not hold on an instance

- If we can be sure that every instance of R will be one in which a given FD is true, then we say that R satisfies the FD
- If we say that R satisfies an FD F, we are stating a constraint on R
 - Recall constraints from lec 17 and sec 7

Why bother with FDs?

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

Anomalies:

- Redundancy = repeat data
- Update anomalies = what if Fred moves to "Bellevue"?
- Deletion anomalies = what if Joe deletes his phone number?

An Interesting Observation

If all these FDs are true:

name → color
category → department
color, category → price

Then this FD also holds:

name, category → price

If we find out from application domain that a relation satisfies some FDs, it doesn't mean that we found all the FDs that it satisfies!

There could be more FDs implied by the ones we have.

Closure of a set of Attributes

Given a set of attributes A₁, ..., A_n

The **closure** is the set of attributes B, notated $\{A_1, ..., A_n\}^+$ s.t. $A_1, ..., A_n \rightarrow B$

```
Example:
```

- 1. name → color
 - 2. category → department
 - 3. color, category → price

Closures:

```
name+ = {name, color}
{name, category}+ = {name, category, color, department, price}
color+ = {color}
```

Closure Algorithm

```
X={A1, ..., An}.
Repeat until X doesn't change do:
if B<sub>1</sub>, ..., B<sub>n</sub> → C is a FD and B<sub>1</sub>, ..., B<sub>n</sub> are all in X
then add C to X.
```

Example:

- 1. name → color
- 2. category → department
- 3. color, category → price

```
{name, category}<sup>+</sup> = { name, category, color, department, price }
```

Hence: name, category → color, department, price

$$\begin{array}{ccc} A, B \rightarrow C \\ A, D \rightarrow E \\ B \rightarrow D \\ A, F \rightarrow B \end{array}$$

Compute
$$\{A,B\}^+$$
 $X = \{A, B,$

$$=\{A,B,$$

Compute
$$\{A, F\}^+$$
 $X = \{A, F,$

$$\begin{array}{c} A, B \rightarrow C \\ A, D \rightarrow E \\ B \rightarrow D \\ A, F \rightarrow B \end{array}$$

Compute
$$\{A,B\}^+$$
 $X = \{A, B, C, D, E\}$

Compute
$$\{A, F\}^+$$
 $X = \{A, F,$

$$\begin{array}{c} A, B \rightarrow C \\ A, D \rightarrow E \\ B \rightarrow D \\ A, F \rightarrow B \end{array}$$

Compute
$$\{A,B\}^+$$
 $X = \{A, B, C, D, E\}$

Compute
$$\{A, F\}^+$$
 $X = \{A, F, B, C, D, E\}$

$$\begin{array}{ccc} A, B \rightarrow C \\ A, D \rightarrow E \\ B \rightarrow D \\ A, F \rightarrow B \end{array}$$

Compute
$$\{A,B\}^+$$
 $X = \{A, B, C, D, E\}$

Compute
$$\{A, F\}^+$$
 $X = \{A, F, B, C, D, E\}$

Practice at Home

Find all FD's implied by:

$$\begin{array}{ccc} A, B & \rightarrow & C \\ A, D & \rightarrow & B \\ B & \rightarrow & D \end{array}$$

Practice at Home

Find all FD's implied by:

$$\begin{array}{ccc} A, B & \rightarrow & C \\ A, D & \rightarrow & B \\ B & \rightarrow & D \end{array}$$

Step 1: Compute X⁺, for every X:

```
A+ = A, B+ = BD, C+ = C, D+ = D

AB+ = ABCD, AC+=AC, AD+=ABCD,
BC+=BCD, BD+=BD, CD+=CD

ABC+ = ABD+ = ACD+ = ABCD (no need to compute— why?)

BCD+ = BCD, ABCD+ = ABCD
```

Step 2: Enumerate all FD's X \rightarrow Y, s.t. Y \subseteq X⁺ and X \cap Y = \emptyset :

 $AB \rightarrow CD, AD \rightarrow BC, ABC \rightarrow D, ABD \rightarrow C, ACD \rightarrow B$

Keys

- A **superkey** is a set of attributes $A_1, ..., A_n$ s.t. for any other attribute B, we have $A_1, ..., A_n \rightarrow B$
- A key is a minimal superkey
 - A superkey and for which no subset is a superkey

Computing (Super)Keys

For all sets X, compute X⁺

If X⁺ = [all attributes], then X is a superkey

Try reducing to the minimal X's to get the key

Product(name, price, category, color)

name, category → price category → color

What is the key?

Product(name, price, category, color)

```
name, category → price category → color
```

```
What is the key?

(name, category) + = { name, category, price, color }

Hence (name, category) is a key
```

Key or Keys?

Can we have more than one key?

Given R(A,B,C) define FD's s.t. there are two or more distinct keys

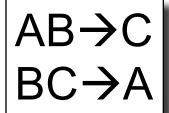
Key or Keys?

Can we have more than one key?

Given R(A,B,C) define FD's s.t. there are two or more distinct keys

$$\begin{array}{c} A \rightarrow B \\ B \rightarrow C \\ C \rightarrow A \end{array}$$

or



or

what are the keys here?

Eliminating Anomalies

Main idea:

- X → A is OK if X is a (super)key
- X → A is not OK otherwise
 - Need to decompose the table, but how?

Boyce-Codd Normal Form