

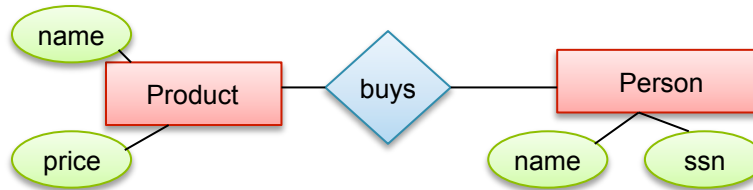
Introduction to Management

CSE 344

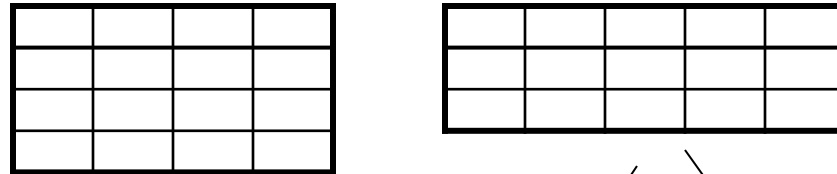
Lectures 16: Database Design

Relational Schema Design

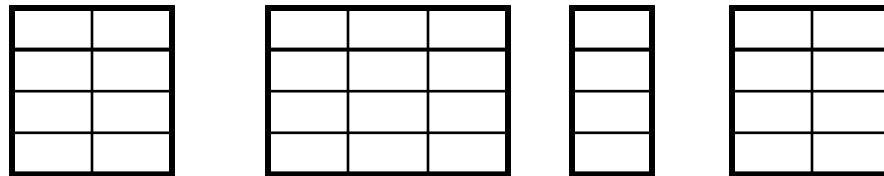
Conceptual Model:



Relational Model:
plus FD's



Normalization:
Eliminates **anomalies**



Relational Schema Design

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

Primary key is thus (SSN,PhoneNumber)

What is the problem with this schema?

Relational Schema Design

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield


Anomalies:

- **Redundancy** = repeat data
- **Update anomalies** = what if Fred moves to “Bellevue”?
- **Deletion anomalies** = what if Joe deletes his phone number?

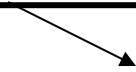
Relation Decomposition

Break the relation into two:

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield



Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield



<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121

Anomalies have gone:

- No more repeated data
- Easy to move Fred to “Bellevue” (how ?)
- Easy to delete all Joe’s phone numbers (how ?)

Relational Schema Design (or Logical Design)

How do we do this systematically?

- Start with some relational schema
- Find out its **functional dependencies** (FDs)
- Use FDs to **normalize** the relational schema

Functional Dependencies (FDs)

Definition

If two tuples agree on the attributes

$$A_1, A_2, \dots, A_n$$

then they must also agree on the attributes

$$B_1, B_2, \dots, B_m$$

Formally:

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

Functional Dependencies (FDs)

Definition $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$ holds in R if:

$\forall t, t' \in R,$

$(t.A_1 = t'.A_1 \wedge \dots \wedge t.A_m = t'.A_m \Rightarrow t.B_1 = t'.B_1 \wedge \dots \wedge t.B_n = t'.B_n)$

R		A_1	...	A_m		B_1	...	B_n		
t										
t'										

if t, t' agree here then t, t' agree here

Example

An FD holds, or does not hold on an instance:

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

EmpID → Name, Phone, Position

Position → Phone

but not Phone → Position

Example

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876 ←	Salesrep
E1111	Smith	9876 ←	Salesrep
E9999	Mary	1234	Lawyer

Position → Phone

Example

EmpID	Name	Phone	Position
E0045	Smith	1234 →	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234 →	Lawyer

But not Phone → Position

Example

name → color
category → department
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Black	Toys	99

Does this instance satisfy all the FDs ?

Example

name → color
category → department
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Black	Toys	99
Gizmo	Stationary	Green	Office-supp.	59

What about this one ?

An Interesting Observation

If all these FDs are true:

name \rightarrow color
category \rightarrow department
color, category \rightarrow price

Then this FD also holds:

name, category \rightarrow price

Why ??

Goal: Find ALL Functional Dependencies

- Anomalies occur when certain “bad” FDs hold
- We know some of the FDs
- Need to find *all* FDs
- Then look for the bad ones

Armstrong's Rules (1/3)

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

Is equivalent to

**Splitting rule
and
Combing rule**

$$\begin{array}{l} A_1, A_2, \dots, A_n \rightarrow B_1 \\ A_1, A_2, \dots, A_n \rightarrow B_2 \\ \dots \\ A_1, A_2, \dots, A_n \rightarrow B_m \end{array}$$

	A_1	...	A_m		B_1	...	B_m	

Armstrong's Rules (2/3)

$$A_1, A_2, \dots, A_n \rightarrow A_i$$

Trivial Rule

where $i = 1, 2, \dots, n$

Why ?

	A_1	...	A_m	

Armstrong's Rules (3/3)

Transitive Rule

If

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

and

$$B_1, B_2, \dots, B_m \rightarrow C_1, C_2, \dots, C_p$$

then

$$A_1, A_2, \dots, A_n \rightarrow C_1, C_2, \dots, C_p$$

Why ?

Armstrong's Rules (3/3)

Illustration

	A_1	...	A_m		B_1	...	B_m		C_1	...	C_p	

Example (continued)

Start from the following FDs:

1. name \rightarrow color
2. category \rightarrow department
3. color, category \rightarrow price

Infer the following FDs:

Inferred FD	Which Rule did we apply ?
4. name, category \rightarrow name	
5. name, category \rightarrow color	
6. name, category \rightarrow category	
7. name, category \rightarrow color, category	
8. name, category \rightarrow price	

Example (continued)

Answers:

1. name \rightarrow color
2. category \rightarrow department
3. color, category \rightarrow price

Inferred FD	Which Rule did we apply ?
4. name, category \rightarrow name	Trivial rule
5. name, category \rightarrow color	Transitivity on 4, 1
6. name, category \rightarrow category	Trivial rule
7. name, category \rightarrow color, category	Split/combine on 5, 6
8. name, category \rightarrow price	Transitivity on 3, 7

THIS IS TOO HARD ! Let's see an easier way.

Closure of a set of Attributes

Given a set of attributes A_1, \dots, A_n

The **closure**, $\{A_1, \dots, A_n\}^+$ = the set of attributes B
s.t. $A_1, \dots, A_n \rightarrow B$

Example:

1. name \rightarrow color
2. category \rightarrow department
3. color, category \rightarrow price

Closures:

$$\text{name}^+ = \{\text{name}, \text{color}\}$$

$$\{\text{name}, \text{category}\}^+ = \{\text{name}, \text{category}, \text{color}, \text{department}, \text{price}\}$$

$$\text{color}^+ = \{\text{color}\}$$

Closure Algorithm

$X = \{A_1, \dots, A_n\}$.

Repeat until X doesn't change do:
if $B_1, \dots, B_n \rightarrow C$ is a FD **and**
 B_1, \dots, B_n are all in X
then add C to X.

Example:

1. name \rightarrow color
2. category \rightarrow department
3. color, category \rightarrow price

$\{\text{name, category}\}^+ =$
 $\{\text{name, category, color, department, price}\}$

Hence: $\text{name, category} \rightarrow \text{color, department, price}$

Example

In class:

$R(A, B, C, D, E, F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute $\{A, B\}^+$ $X = \{A, B,$ $\}$

Compute $\{A, F\}^+$ $X = \{A, F,$ $\}$

Example

In class:

$R(A, B, C, D, E, F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute $\{A, B\}^+$ $X = \{A, B, C, D, E\}$

Compute $\{A, F\}^+$ $X = \{A, F, \quad \}$

Example

In class:

$R(A, B, C, D, E, F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute $\{A, B\}^+$ $X = \{A, B, C, D, E\}$

Compute $\{A, F\}^+$ $X = \{A, F, B, C, D, E\}$

Why Do We Need Closure

- With closure we can find all FD's easily
- To check if $X \rightarrow A$
 - Compute X^+
 - Check if $A \in X^+$

Practice at Home

Find all FD's implied by:

$$\begin{array}{l} A, B \rightarrow C \\ A, D \rightarrow B \\ B \rightarrow D \end{array}$$

Practice at Home

Find all FD's implied by:

$$\begin{array}{l} A, B \rightarrow C \\ A, D \rightarrow B \\ B \rightarrow D \end{array}$$

Step 1: Compute X^+ , for every X :

$$A^+ = A, \quad B^+ = BD, \quad C^+ = C, \quad D^+ = D$$

$$AB^+ = ABCD, \quad AC^+ = AC, \quad AD^+ = ABCD,$$

$$BC^+ = BCD, \quad BD^+ = BD, \quad CD^+ = CD$$

$$ABC^+ = ABD^+ = ACD^+ = ABCD \text{ (no need to compute— why ?)}$$

$$BCD^+ = BCD, \quad ABCD^+ = ABCD$$

Practice at Home

Find all FD's implied by:

$$\begin{array}{l} A, B \rightarrow C \\ A, D \rightarrow B \\ B \rightarrow D \end{array}$$

Step 1: Compute X^+ , for every X :

$$A^+ = A, \quad B^+ = BD, \quad C^+ = C, \quad D^+ = D$$

$$AB^+ = ABCD, \quad AC^+ = AC, \quad AD^+ = ABCD,$$

$$BC^+ = BCD, \quad BD^+ = BD, \quad CD^+ = CD$$

$$ABC^+ = ABD^+ = ACD^+ = ABCD \text{ (no need to compute— why ?)}$$

$$BCD^+ = BCD, \quad ABCD^+ = ABCD$$

Step 2: Enumerate all FD's $X \rightarrow Y$, s.t. $Y \subseteq X^+$ and $X \cap Y = \emptyset$:

$$AB \rightarrow CD, \quad AD \rightarrow BC, \quad ABC \rightarrow D, \quad ABD \rightarrow C, \quad ACD \rightarrow B$$

Keys

- A **superkey** is a set of attributes A_1, \dots, A_n s.t. for any other attribute B , we have $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
 - I.e. set of attributes which is a superkey and for which no subset is a superkey

Computing (Super)Keys

- Compute X^+ for all sets X
- If $X^+ =$ all attributes, then X is a superkey
- List only the minimal X 's to get the keys

Example

Product(name, price, category, color)

name, category → price
category → color

What is the key ?

Example

Product(name, price, category, color)

name, category \rightarrow price
category \rightarrow color

What is the key ?

$(\text{name, category})^+ = \{ \text{name, category, price, color} \}$

Hence (name, category) is a key

Key or Keys ?

Can we have more than one key ?

Given $R(A,B,C)$ define FD's s.t. there are two or more keys

Key or Keys ?

Can we have more than one key ?

Given $R(A,B,C)$ define FD's s.t. there are two or more keys

$A \rightarrow B$
$B \rightarrow C$
$C \rightarrow A$

or

$AB \rightarrow C$
$BC \rightarrow A$

or

$A \rightarrow BC$
$B \rightarrow AC$

what are the keys here ?

Eliminating Anomalies

Main idea:

- $X \rightarrow A$ is OK if X is a (super)key
- $X \rightarrow A$ is not OK otherwise

Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

SSN → Name, City

What is the key?

{SSN, PhoneNumber}

Hence SSN → Name, City
is a “bad” dependency

Boyce-Codd Normal Form

There are no
“bad” FDs:

Definition. A relation R is in BCNF if:

Whenever $X \rightarrow B$ is a non-trivial dependency,
then X is a superkey.

Equivalently:

Definition. A relation R is in BCNF if:

$\forall X$, either $X^+ = X$ or $X^+ = [\text{all attributes}]$

BCNF Decomposition Algorithm

Normalize(R)

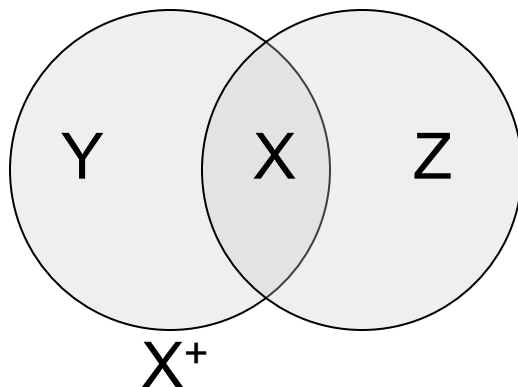
find X s.t.: $X \neq X^+ \neq$ [all attributes]

if (not found) **then** “R is in BCNF”

let $Y = X^+ - X$; $Z =$ [all attributes] - X^+

decompose R into $R_1(X \cup Y)$ and $R_2(X \cup Z)$

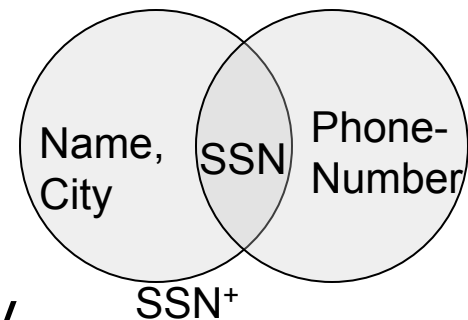
Normalize(R_1); Normalize(R_2);



Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

$SSN \rightarrow Name, City$



The only key is: $\{SSN, PhoneNumber\}$

Hence $SSN \rightarrow Name, City$ is a “bad” dependency

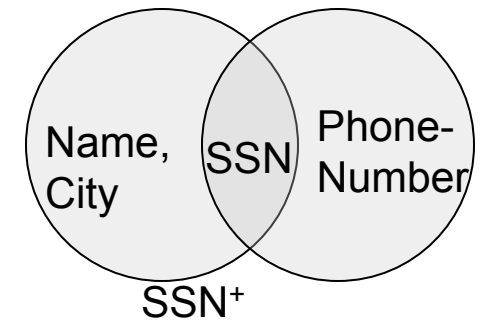
In other words:

$SSN^+ = Name, City$ and is neither SSN nor $All\ Attributes$

Example BCNF Decomposition

<u>Name</u>	<u>SSN</u>	<u>City</u>
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

SSN \rightarrow Name, City



<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

Let's check anomalies:

- Redundancy ?
- Update ?
- Delete ?

Find X s.t.: $X \neq X^+ \neq$ [all attributes]

Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN \rightarrow name, age

age \rightarrow hairColor



Find X s.t.: $X \neq X^+ \neq$ [all attributes]

Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

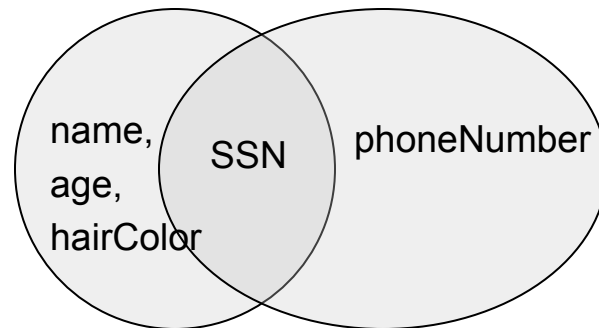
SSN \rightarrow name, age

age \rightarrow hairColor

Iteration 1: **Person**: SSN⁺ = SSN, name, age, hairColor

Decompose into: **P**(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)



Find X s.t.: $X \neq X^+ \neq$ [all attributes]

Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN \rightarrow name, age

age \rightarrow hairColor

What are
the keys ?

Iteration 1: **Person**: SSN⁺ = SSN, name, age, hairColor

Decompose into: **P**(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Iteration 2: **P**: age⁺ = age, hairColor

Decompose: **People**(SSN, name, age)

Hair(age, hairColor)

Phone(SSN, phoneNumber)

Find X s.t.: $X \neq X^+ \neq$ [all attributes]

Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN \rightarrow name, age

age \rightarrow hairColor

Note the keys!

Iteration 1: **Person**: SSN⁺ = SSN, name, age, hairColor

Decompose into: **P**(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Iteration 2: **P**: age⁺ = age, hairColor

Decompose: **People**(SSN, name, age)

Hair(age, hairColor)

Phone(SSN, phoneNumber)

R(A,B,C,D)

Practice at Home

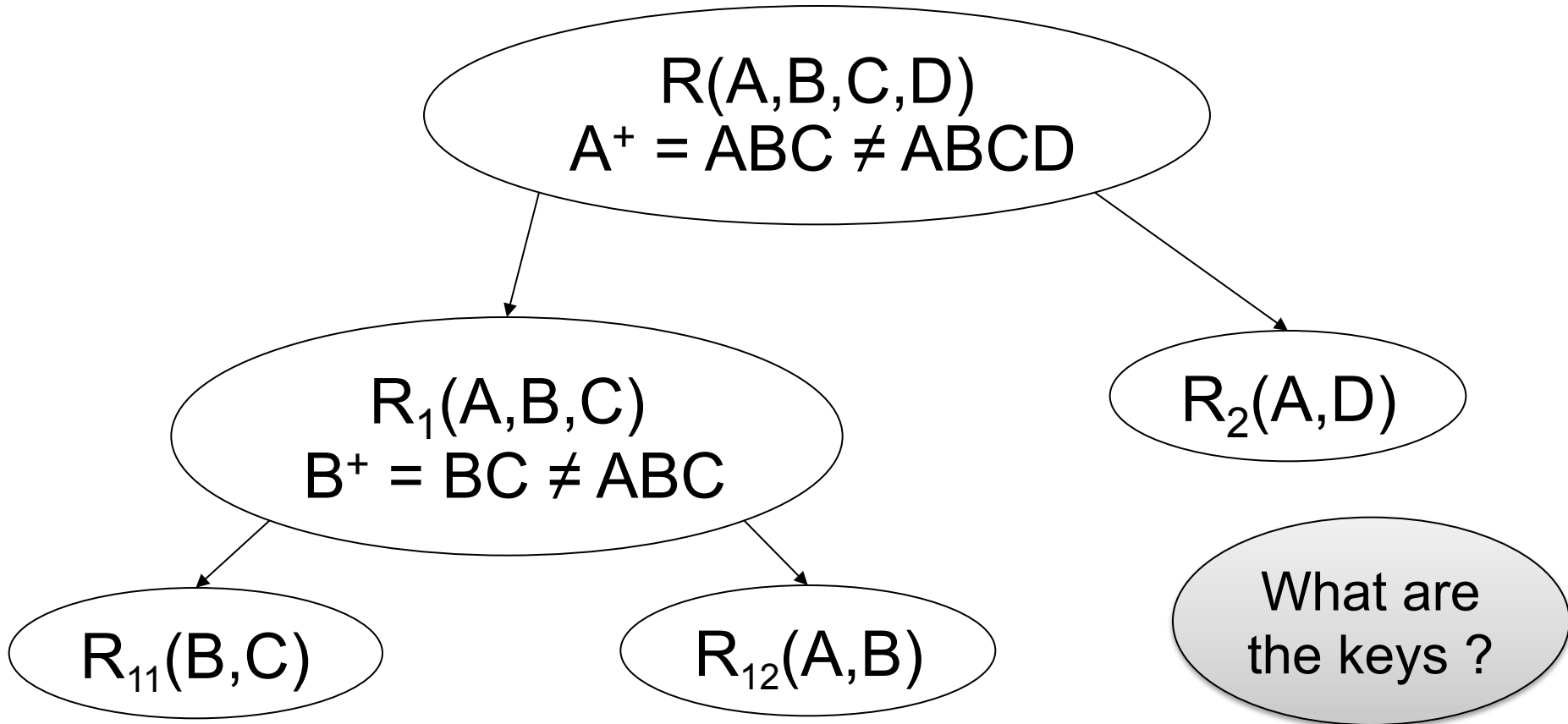
A	→	B
B	→	C

R(A,B,C,D)
 $A^+ = ABC \neq ABCD$

R(A,B,C,D)

A → B
B → C

Practice at Home



What happens if in R we first pick B^+ ? Or AB^+ ?

Schema Refinements = Normal Forms

- 1st Normal Form = all tables are flat
- 2nd Normal Form = obsolete
- Boyce Codd Normal Form = today
- 3rd Normal Form = see book