

CSE341: Programming Languages

Lecture 7
First-Class Functions

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What is functional programming?

"Functional programming" can mean a few different things:

- Avoiding mutation in most/all cases (done and ongoing)
- 2. Using functions as values (this unit)

. . .

- Style encouraging recursion and recursive data structures
- Style closer to mathematical definitions
- Programming idioms using laziness (later topic, briefly)
- Anything not OOP or C? (not a good definition)

Not sure a definition of "functional language" exists beyond "makes functional programming easy / the default / required"

No clear yes/no for a particular language

First-class functions

- First-class functions: Can use them wherever we use values
 - Functions are values too
 - Arguments, results, parts of tuples, bound to variables, carried by datatype constructors or exceptions, ...

```
fun double x = 2*x
fun incr x = x+1
val a_tuple = (double, incr, double(incr 7))
```

- Most common use is as an argument / result of another function
 - Other function is called a higher-order function
 - Powerful way to factor out common functionality

Function Closures

- Function closure: Functions can use bindings from outside the function definition (in scope where function is defined)
 - Makes first-class functions much more powerful
 - Will get to this feature in a bit, after simpler examples
- Distinction between terms first-class functions and function closures is not universally understood
 - Important conceptual distinction even if terms get muddled

Onward

The next week:

- How to use first-class functions and closures
- The precise semantics
- Multiple powerful idioms

Functions as arguments

- We can pass one function as an argument to another function
 - Not a new feature, just never thought to do it before

```
fun f (g,...) = ... g (...) ...
fun h1 ... = ...
fun h2 ... = ...
... f(h1,...) ... f(h2,...) ...
```

- Elegant strategy for factoring out common code
 - Replace N similar functions with calls to 1 function where you pass in N different (short) functions as arguments

[See the code file for this lecture]

Example

Can reuse n_times rather than defining many similar functions

Computes f(f(...f(x))) where number of calls is n

```
fun n_times (f,n,x) =
   if n=0
   then x
   else f (n_times(f,n-1,x))
fun double x = x + x
fun increment x = x + 1
val x1 = n times(double, 4, 7)
val x2 = n_times(increment, 4, 7)
val x3 = n times(t1,2,[4,8,12,16])
fun double_n_times (n,x) = n_times(double,n,x)
fun nth tail (n,x) = n times(tl,n,x)
```

Relation to types

- Higher-order functions are often so "generic" and "reusable" that they have polymorphic types, i.e., types with type variables
- But there are higher-order functions that are not polymorphic
- And there are non-higher-order (first-order) functions that are polymorphic
- Always a good idea to understand the type of a function, especially a higher-order function

Types for example

```
fun n_times (f,n,x) =
   if n=0
   then x
   else f (n_times(f,n-1,x))
```

- val n_times : ('a -> 'a) * int * 'a -> 'a
 Simpler but less useful: (int -> int) * int * int -> int
 - Simpler but less useful: (int -> int) * int * int -> int
- Two of our examples instantiated 'a with int
- One of our examples instantiated 'a with int list
- This polymorphism makes n_times more useful
- Type is inferred based on how arguments are used (later lecture)
 - Describes which types must be exactly something (e.g., int) and which can be anything but the same (e.g., 'a)

Polymorphism and higher-order functions

- Many higher-order functions are polymorphic because they are so reusable that some types, "can be anything"
- But some polymorphic functions are not higher-order

```
- Example: len : 'a list -> int
```

- And some higher-order functions are not polymorphic
 - Example: times_until_0 : (int -> int) * int -> int

```
fun times_until_zero (f,x) =
  if x=0 then 0 else 1 + times_until_zero(f, f x)
```

Note: Would be better with tail-recursion

Toward anonymous functions

Definitions unnecessarily at top-level are still poor style:

```
fun trip x = 3*x
fun triple_n_times (f,x) = n_times(trip,n,x)
```

So this is better (but not the best):

```
fun triple_n_times (f,x) =
  let fun trip y = 3*y
  in
    n_times(trip,n,x)
  end
```

- And this is even smaller scope
 - It makes sense but looks weird (poor style; see next slide)

```
fun triple_n_times (f,x) =
  n_times(let fun trip y = 3*y in trip end, n, x)
```

Anonymous functions

• This does not work: A function binding is not an expression

```
fun triple_n_times (f,x) =
  n_times((fun trip y = 3*y), n, x)
```

 This is the best way we were building up to: an expression form for anonymous functions

```
fun triple_n_times (f,x) =
  n_times((fn y => 3*y), n, x)
```

- Like all expression forms, can appear anywhere
- Syntax:
 - fn not fun
 - => not =
 - no function name, just an argument pattern

Using anonymous functions

- Most common use: Argument to a higher-order function
 - Don't need a name just to pass a function
- But: Cannot use an anonymous function for a recursive function
 - Because there is no name for making recursive calls
 - If not for recursion, fun bindings would be syntactic sugar for val bindings and anonymous functions

```
fun triple x = 3*x

val triple = fn y => 3*y
```

A style point

Compare:

if x then true else false

With:

$$(fn x => f x)$$

So don't do this:

$$n_{times}((fn y => tl y),3,xs)$$

When you can do this:

Map

```
fun map (f,xs) =
   case xs of
   [] => []
   | x::xs' => (f x)::(map(f,xs'))
```

```
val map : ('a -> 'b) * 'a list -> 'b list
```

Map is, without doubt, in the "higher-order function hall-of-fame"

- The name is standard (for any data structure)
- You use it all the time once you know it: saves a little space,
 but more importantly, communicates what you are doing
- Similar predefined function: List.map
 - But it uses currying (coming soon)

Filter

```
val filter : ('a -> bool) * 'a list -> 'a list
```

Filter is also in the hall-of-fame

- So use it whenever your computation is a filter
- Similar predefined function: List.filter
 - But it uses currying (coming soon)

Generalizing

Our examples of first-class functions so far have all:

- Taken one function as an argument to another function
- Processed a number or a list

But first-class functions are useful anywhere for any kind of data

- Can pass several functions as arguments
- Can put functions in data structures (tuples, lists, etc.)
- Can return functions as results
- Can write higher-order functions that traverse your own data structures

Useful whenever you want to abstract over "what to compute with"

No new language features

Returning functions

- Remember: Functions are first-class values
 - For example, can return them from functions
- Silly example:

```
fun double_or_triple f =
   if f 7
   then fn x => 2*x
   else fn x => 3*x
```

```
Has type (int -> bool) -> (int -> int)
```

But the REPL prints (int -> bool) -> int -> int because it never prints unnecessary parentheses and t1 -> t2 -> t3 -> t4 means t1->(t2->(t3->t4))

Other data structures

- Higher-order functions are not just for numbers and lists
- They work great for common recursive traversals over your own data structures (datatype bindings) too
- Example of a higher-order predicate:
 - Are all constants in an arithmetic expression even numbers?
 - Use a more general function of type
 (int -> bool) * exp -> bool
 - And call it with (fn $x => x \mod 2 = 0$)