

CSE341: Programming Languages Lecture 2 Functions, Pairs, Lists

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Function definitions

Functions: the most important building block in the whole course

- Like Java methods, have arguments and result
- But no classes, this, return, etc.

Example function binding:

```
(* Note: correct only if y>=0 *)
fun pow (x:int, y:int) =
  if y=0
  then 1
  else x * pow(x,y-1)
```

Note: The body includes a (recursive) function call: pow(x,y-1)

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Example, extended

```
fun pow (x:int, y:int) =
   if y=0
   then 1
   else x * pow(x,y-1)

fun cube (x:int) =
   pow (x,3)

val sixtyfour = cube 4

val fortytwo = pow(2,2+2) + pow(4,2) + cube(2) + 2
```

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Some gotchas

Three common "gotchas"

- · Bad error messages if you mess up function-argument syntax
- The use of * in type syntax is not multiplication
 - Example: int * int -> int
 - In expressions, * is multiplication: x * pow(x,y-1)
- · Cannot refer to later function bindings
 - That's simply ML's rule
 - Helper functions must come before their uses
 - Need special construct for mutual recursion (later)

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Recursion

- If you're not yet comfortable with recursion, you will be soon $\ensuremath{\textcircled{\texttt{@}}}$
 - Will use for most functions taking or returning lists
- "Makes sense" because calls to same function solve "simpler" problems
- · Recursion more powerful than loops
 - We won't use a single loop in ML
 - Loops often (not always) obscure simple, elegant solutions

Function bindings: 3 questions

- Syntax: fun x0 (x1:t1, ..., xn:tn) = e
 (Will generalize in later lecture)
- Evaluation: A function is a value! (No evaluation yet)
 - Adds x0 to environment so later expressions can call it
 - (Function-call semantics will also allow recursion)
- · Type-checking:
 - Adds binding $x0 : (t1 * ... * tn) \rightarrow t if:$
 - Can type-check body e to have type t in the static environment containing:
 - "Enclosing" static environment (earlier bindings)
 - x1 : t1, ..., xn : tn (arguments with their types)
 - x0 : (t1 * ... * tn) -> t (for recursion)

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More on type-checking

fun x0 (x1:t1, ..., xn:tn) = e

- New kind of type: (t1 * ... * tn) -> t
 - Result type on right
 - The overall type-checking result is to give x0 this type in rest of program (unlike Java, not for earlier bindings)
 - Arguments can be used only in e (unsurprising)
- Because evaluation of a call to x0 will return result of evaluating ${\tt e}$, the return type of ${\tt x0}$ is the type of ${\tt e}$
- The type-checker "magically" figures out ${\tt t}$ if such a ${\tt t}$ exists
 - Later lecture: Requires some cleverness due to recursion
 - More magic after hw1: Later can omit argument types too

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Function Calls

A new kind of expression: 3 questions

Syntax: e0 (e1,...,en)

- (Will generalize later)
- Parentheses optional if there is exactly one argument

- e0 has some type (t1 * ... * tn) -> t
- el has type tl, ..., en has type tn

e0(e1,...,en) has type t

Example: pow(x,y-1) in previous example has type int

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Function-calls continued

e0(e1,...,en)

Evaluation:

- 1. (Under current dynamic environment,) evaluate e0 to a function fun x0 (x1:t1, ..., xn:tn) = e
 - Since call type-checked, result will be a function
- 2. (Under current dynamic environment,) evaluate arguments to values v1, ..., vn
- 3. Result is evaluation of e in an environment extended to map x1 to v1, ..., xn to vn
 - ("An environment" is actually the environment where the function was defined, and includes x0 for recursion)

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So far: numbers, booleans, conditionals, variables, functions

- Now ways to build up data with multiple parts
- This is essential

Tuples and lists

- Java examples: classes with fields, arrays

Now:

Tuples: fixed "number of pieces" that may have different types

Then:

Lists: any "number of pieces" that all have the same type

Later:

- Other more general ways to create compound data

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Pairs (2-tuples)

Need a way to build pairs and a way to access the pieces

Build:

• Syntax: (e1,e2)

- Evaluation: Evaluate e1 to v1 and e2 to v2; result is (v1,v2)
 - A pair of values is a value
- Type-checking: If e1 has type ta and e2 has type tb, then the pair expression has type ta * tb
 - A new kind of type

Pairs (2-tuples)

Need a way to build pairs and a way to access the pieces

Access:

• Syntax: #1 e and #2 e

- Evaluation: Evaluate e to a pair of values and return first or second piece
 - Example: If e is a variable x, then look up x in environment
- Type-checking: If e has type ta * tb, then #1 e has type ta and #2 e has type tb

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Examples

Functions can take and return pairs

```
fun swap (pr:int*bool) =
    (#2 pr, #1 pr)

fun sum_two_pairs (pr1:int*int, pr2:int*int) =
    (#1 pr1) + (#2 pr1) + (#1 pr2) + (#2 pr2)

fun div_mod (x:int, y:int) =
    (x div y, x mod y)

fun sort_pair (pr:int*int) =
    if (#1 pr) < (#2 pr)
    then pr
    else (#2 pr, #1 pr)</pre>
```

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Tuples

Actually, you can have tuples with more than two parts

- A new feature: a generalization of pairs

```
• (e1,e2,...,en)
• ta * tb * ... * tn
• #1 e, #2 e, #3 e, ...
```

Homework 1 uses triples of type int*int*int a lot

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Nesting

Pairs and tuples can be nested however you want

- Not a new feature: implied by the syntax and semantics

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Lists

 Despite nested tuples, the type of a variable still "commits" to a particular "amount" of data

In contrast, a list:

- Can have any number of elements
- But all list elements have the same type

Need ways to build lists and access the pieces...

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Building Lists

• The empty list is a value:

[]

 In general, a list of values is a value; elements separated by commas:

[v1,v2,...,vn]

 If e1 evaluates to v and e2 evaluates to a list [v1,...,vn], then e1::e2 evaluates to [v,...,vn]

```
el::e2 (* pronounced "cons" *)
```

Accessing Lists

Until we learn pattern-matching, we will use three standard-library functions

- null e evaluates to true if and only if e evaluates to []
- If e evaluates to [v1,v2,...,vn] then nd e evaluates to v1
 (raise exception if e evaluates to [])
- If e evaluates to [v1,v2,...,vn] then t1 e evaluates to [v2,...,vn]
 - (raise exception if e evaluates to [])
 - Notice result is a list

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Type-checking list operations

Lots of new types: For any type t, the type t list describes lists where all elements have type t

```
- Examples: int list bool list int list list
(int * int) list (int list * int) list
```

- So [] can have type t list list for any type
 - SML uses type 'a list to indicate this ("quote a" or "alpha")
- For e1::e2 to type-check, we need a t such that e1 has type t and e2 has type t list. Then the result type is t list

```
null: 'a list -> boolhd: 'a list -> 'at1: 'a list -> 'a list
```

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Example list functions

```
fun sum_list (xs:int list) =
  if null xs
  then 0
  else hd(xs) + sum_list(tl(xs))

fun countdown (x:int) =
  if x=0
  then []
  else x :: countdown (x-1)

fun append (xs:int list, ys:int list) =
  if null xs
  then ys
  else hd (xs) :: append (tl(xs), ys)
```

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Recursion again

Functions over lists are usually recursive

- Only way to "get to all the elements"
- · What should the answer be for the empty list?
- · What should the answer be for a non-empty list?
 - Typically in terms of the answer for the tail of the list!

Similarly, functions that produce lists of potentially any size will be recursive

- You create a list out of smaller lists

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Lists of pairs

Processing lists of pairs requires no new features. Examples:

```
fun sum_pair_list (xs:(int*int) list) =
   if null xs
   then 0
   else #1(hd xs) + #2(hd xs) + sum_pair_list(tl xs)

fun firsts (xs:(int*int) list) =
   if null xs
   then []
   else #1(hd xs) :: firsts(tl xs)

fun seconds (xs:(int*int) list) =
   if null xs
   then []
   else #2(hd xs) :: seconds(tl xs)

fun sum_pair_list2 (xs:(int*int) list) =
   (sum_list (firsts xs)) + (sum_list (seconds xs))
```

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