## CSE341 Autumn 2018, Midterm Examination October 29, 2018

## Please do not turn the page until 12:30.

Rules:

- The exam is closed-book, closed-note, etc. except for *one* side of one 8.5x11in piece of paper.
- Please stop promptly at 1:20.
- There are **100 points**, distributed **unevenly** among **6** questions (all with multiple parts):
- The exam is printed double-sided.

Advice:

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit. But clearly indicate what is your final answer.
- The questions are not necessarily in order of difficulty. Skip around. Make sure you get to all the questions.
- If you have questions, ask.
- Relax. You are here to learn.

1. (23 points) This problem uses this datatype binding, where a maze involves any number of "choices" on the way "forward" with each "path" ending either successfully (Finish) or not (DeadEnd). A maze can have more than one Finish. "Solving" a maze means following any path that leads to Finish.

```
datatype maze =
    Finish
    DeadEnd
    Forward of maze * maze (* a pair of ("if going left", "if going right") *)
```

- (a) Write a function has\_a\_solution of type maze -> bool that evaluates to true if and only if there is at least one path that ends with Finish.
- (b) Given the additional datatype binding datatype dir = Left | Right, write a function solve\_maze of type maze -> dir list option. As an example, solve\_maze (Forward(DeadEnd,Forward(Finish,Forward(DeadEnd,DeadEnd))) would evaluate to SOME [Right,Left] because the maze can be "solved" by going right at the first Forward and left at the second Forward. Return NONE only if the maze has no solution. If a maze has multiple solutions, evaluate to SOME xs where xs indicates any one way to solve the maze. Hint: You need 2 or 3 case expressions, preferably 3.
- (c) Give a value v such that the only correct result for solve\_maze v is SOME [Left,Left].
- (d) Consider this alternate datatype for representing a maze:

```
datatype maze2 =
    End of bool (* true means finish; false means dead-end *)
    | Branch of maze2 list (* any number of next paths *)
```

Write a function maze\_to\_maze2 of type maze -> maze2 that produces a maze2 that represents the same choices as the maze argument. Hint: All lists in the result will have length 2.

The next page is blank in case you need more room.

Name:\_\_\_

More room if needed for Problem 1.

Name:

2. (18 points) This problem considers the problem of writing a function of type 'a list \* 'a list -> bool that evaluates to true if and only if the first argument is longer-or-the-same-length-as the second argument. Here is a correct implementation:

- (a) For each of the following alternate orders of the branches, indicate one of the following: (A) The function would still be correct.
  - (B) The function would still type-check (no unreachable branch) but would no longer be correct.
  - (C) The function would no longer type-check (due to an unreachable branch).
    - i. line 2; then line 1; then line 3
  - ii. line 3; then line 1; then line 2
  - iii. line 3; then line 2; then line 1
  - iv. line 1; then line 3; then line 2
- (b) Now consider the original order again but consider adding a fourth branch | ([],[]) => true. For each of the following positions for this extra branch, indicate (A), (B), or (C) as in the previous problem:
  - i. before line 1 (ignore the syntax issue that the first branch has no | character and line 1 would need one)
  - ii. between lines 1 and 2
  - iii. between lines 2 and 3  $\,$
  - iv. after line 3
- (c) Reimplement longer with a one-line fun binding using List.length.

Name:

3. (13 points) For each of the following programs, if the program does not type-check answer "NO", else indicate what **ans** would be bound to after the program runs. Each part (a)-(d) is a separate program but (b), (c), and (d) all use this datatype binding:

datatype foo = A of int | B of string \* foo

```
(a) val y = 17
   fun f x =
     let
         val z = y
     in
         (fn q => z + q + x)
     end
   val y = 3
   val ans = (f 8) y
(b) fun g (x,b) =
     if b
     then A x
     else B (x, A 0)
   val ans = g (3,true)
(c) exception UhOh
   fun m x =
     case x of
         A i => if i=7 then raise UhOh else 34
       | B(_,r) => m r
   val ans = m (B("hi",B("bye", A 6))) handle UhOh => 19
(d) val x = 3
   fun h f = f x
   val ans = h (A o (fn x => x+2)) (* recall o is function composition *)
```

Name:

- 4. (**18** points)
  - (a) Write a function map\_index of type (int \* 'a -> 'b) -> 'a list -> 'b list (notice the arguments are curried but the first argument takes a pair). map\_index behaves like map except when the first argument is passed the *i<sup>th</sup>* element of the second argument, it is also passed *i* (starting with 1 for the first element of the list). Use one locally-defined helper function and no other helper functions.
  - (b) Use a val binding and a partial application of map\_index to define numbered, a function of type string list -> string list that puts each string's position, a colon, and a space at the beginning of it. For example, numbered ["hi", "bye", "Dan"] would evaluate to ["1: hi", "2: bye", "3: Dan"]. Hints: Int.toString, ^.
  - (c) Use a val binding and a partial application of map\_index to define redact\_evens, a function of type string list -> string list where the strings at odd-numbered list positions are in the output list unchanged and the strings at even-numbered list positions are replaced in the output list by the empty string "".

Name:\_\_\_

5. (8 points) Recall:

- List.foldl has type ('a \* 'b -> 'b) -> 'b -> 'a list -> 'b
- List.filter has type ('a -> bool) -> 'a list -> 'a list
- (a) Complete this function definition (by replacing the ... with some number of expressions) so that rev\_filter is like List.filter except the result list is in the reverse order. Do not use List.filter.

fun rev\_filter f = List.foldl ...

(b) In at most one sentence, give a reason your rev\_filter is likely to be faster than List.filter.

- 6. (20 points) This problem considers an ML module MinMaxList and a signature MINMAXLIST. They are on the next page. Separate that page from your exam and do *not* turn it in.
  - (a) Answer these questions about the min and max functions defined in MinMaxList.
    - i. What is the type of min inside the module?
    - ii. What is the type of min outside the module?
    - iii. What is the type of max inside the module?
    - iv. What is the type of max outside the module?
    - v. Which is faster, min or max?
  - (b) Given the signature MINMAXLIST:
    - i. Can a client cause min or max to raise an exception?
    - ii. Can a client cause max to return a number that isn't the maximum number in its argument?
    - iii. Can a client cause min to return a number that isn't the minimum number in its argument?
  - (c) Repeat part (b) but assuming we replace the line type my\_int\_list with type my\_int\_list = int list
    - i. Can a client cause min or max to raise an exception?
    - ii. Can a client cause max to return a number that isn't the maximum number in its argument?
    - iii. Can a client cause min to return a number that isn't the minimum number in its argument?
  - (d) Repeat part (b) but assuming we start with the original MINMAXLIST (not any changes from previous parts) and *add* this line to the signature:val empty : my\_int\_list
    - i. Can a client cause min or max to raise an exception?
    - ii. Can a client cause max to return a number that isn't the maximum number in its argument?
    - iii. Can a client cause min to return a number that isn't the minimum number in its argument?
  - (e) Repeat part (b) but assuming we start with the original MINMAXLIST (not any changes from previous parts) and add this line to the signature:
     val cons : int \* my\_int\_list -> my\_int\_list
    - i. Can a client cause min or max to raise an exception?
    - ii. Can a client cause max to return a number that isn't the maximum number in its argument?
    - iii. Can a client cause min to return a number that isn't the minimum number in its argument?

These definitions are used in Problem 6. Rip this page out from the rest of the exam. Do not put answers on this page and do not turn it in.

```
signature MINMAXLIST =
sig
type my_int_list
val new : int -> my_int_list
val add : int * my_int_list -> my_int_list
val max : my_int_list -> int
val min : my_int_list -> int
end
structure MinMaxList :> MINMAXLIST =
struct
type my_int_list = int list
exception Bad
val empty = []
fun cons (i,xs) = i::xs
fun new i = i::[]
fun add (i,xs) =
  case xs of
     [] => i::[]
   | j::ys => if i < j then j::i::ys else i::xs</pre>
fun min xs =
  case xs of
      [] => raise Bad
    | i::[] => i
    | i::ys => let val m = min ys in if i < m then i else m end
fun max xs =
  case xs of
      [] => raise Bad
   | i::_ => i
```

```
\operatorname{end}
```