



PAUL G. ALLEN SCHOOL
OF COMPUTER SCIENCE & ENGINEERING

CSE 341: Section 6

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Agenda

- Memoization
 - Motivation
 - A quick detour...
 - Better fibonacci
- Streams
 - A quick refresher on thunks
 - Infinite lists!

Memoization

- Why is the following “natural” implementation of the Fibonacci sequence slow?

```
(define (fibonacci x)
  (if (or (= x 1) (= x 2))
      1
      (+ (fibonacci (- x 1))
         (fibonacci (- x 2))))))
```

- Tons of repeated work!
 - In fact, execution time grows with respect to 2^x

Memoization

Motivation

Remember the results of calls the first time we evaluate them, so we don't have to redo any work

A quick detour...

- An “associative list” is a list of pairs that you can think of as key/value pairs

```
(define my-list (list (cons 1 2) (cons 3 4) (cons 5 6) (cons "example" #t)))
```

```
(assoc 1 my-list) ; `(1 . 2)
```

```
(assoc 3 my-list) ; `(3 . 4)
```

```
(assoc "example" my-list) ; `("example" . #t)
```

- `assoc` is part of the standard library

How can we improve on Fibonacci?

Memoization Recap

- Take a problem that involves lots of repeated work
- Add the ability to “remember” results
 - Maybe using an associative list, maybe some other way
- Now we only do the repeated work once, and we can look it up after that

Streams

- A stream is basically an infinitely long list, with the added bonus that it doesn't take an infinite amount of time to construct
 - Good for us
 - I'm gonna show you an infinite list
 - I want to go home later
 - You probably need to eat

A stream is a *thunk* that, when evaluated, produces a pair whose first element is an element of the stream, and whose second element is the stream that will produce the rest of the elements.

The Simplest Stream

```
(define (ones) (cons 1 ones))
```

More complex behavior

- Instead of returning the *same* function each time, let's return a new function, which will produce the next value/function pair, etc...

Some slightly more complex examples