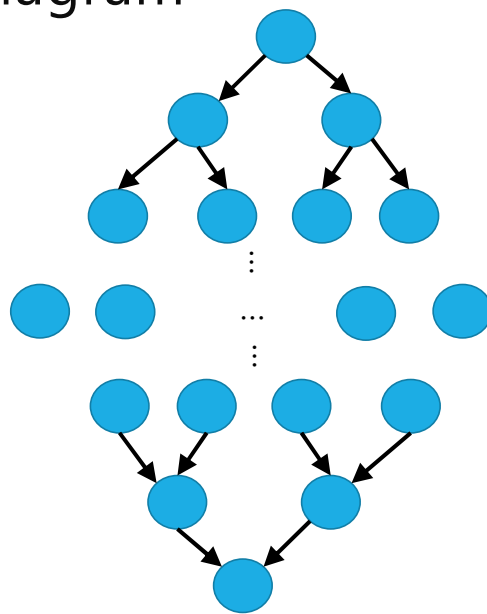


## Useful Diagram

One node per  
 $O(1)$  operation



Divide to create  
threads.

Base Case  
computations

Join and  
combine to  
create final  
answer.

2

## Definitions

$T_P$  is running time with  $P$  Processors, so span is "you always have a processor available"

**Work:**  $T_1$

Total computation required.

**Span:**  $T_\infty$

Longest path in graph of computation. "critical path"

**Speedup:** for  $P$  processors:  $\frac{T_1}{T_P}$

ideally: speedup will be close to  $P$  ("perfect linear speedup")

**Parallelism:**  $\frac{T_1}{T_\infty}$

the speedup when you have as many processors as you can use (there's a point at which another one won't actually help).

65

## Amdahl's Law

Suppose our program takes 100 seconds.  
And  $S$  is 1/3 (i.e. 33 seconds).

What is the running time with

3 processors

6 processors

22 processors

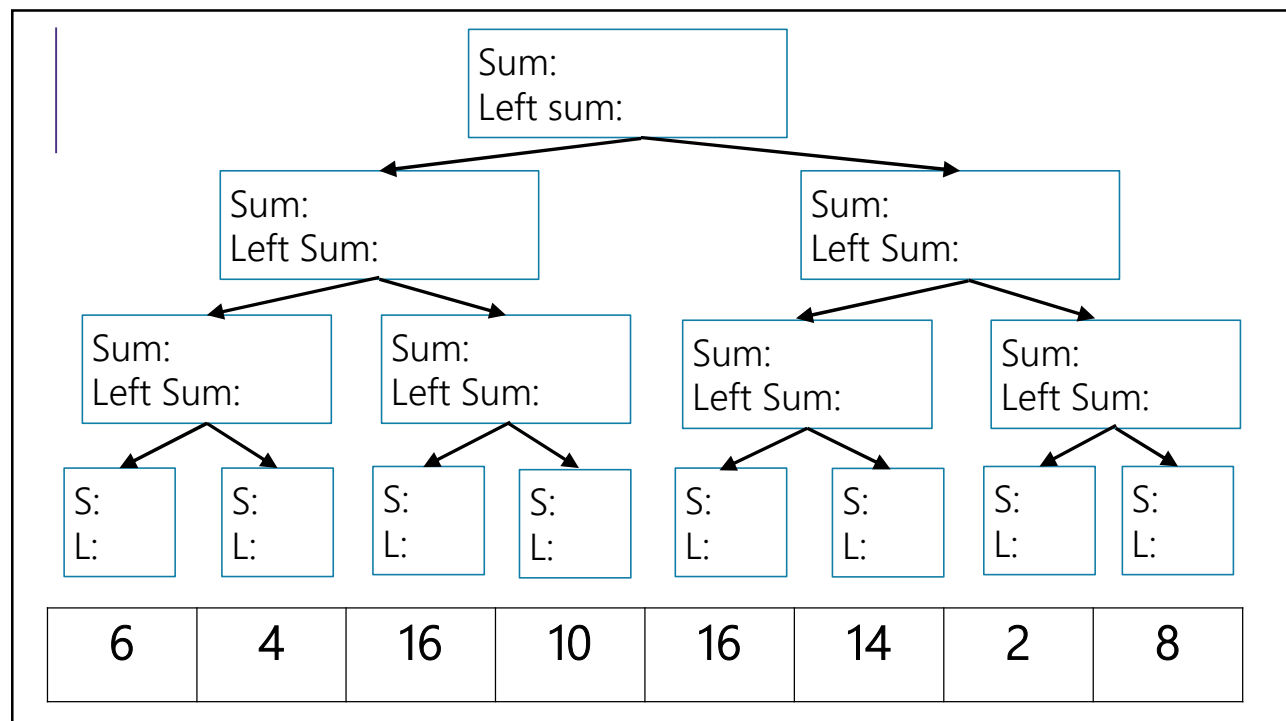
67 processors

1,000,000 processors (approximately).

### Amdahl's Law

$$\frac{T_1}{T_P} \leq \frac{1}{S + \frac{1-S}{P}}$$

66



67