CSE 332 Autumn 2024 Lecture 25: Concurrency 3 & Minimum Spanning Trees

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Deadlock

- Occurs when two or more threads are mutually blocking each other
- T1 is blocked by T2, which is blocked by T3, ..., Tn is blocked by T1
 - A cycle of blocking

Bank Account

```
class BankAccount {
      synchronized void withdraw(int amt) {...}
    synchronized void deposit(int amt) {...}
      synchronized void transferTo(int amt, BankAccount a) {
            this.withdraw(amt);
            a.deposit(amt);
```

The Deadlock

Expected Behavior:

Thread 2 items from a stack are popped in LIFO order

Thread 1:

x.transferTo(1,y);

Thread 2:

y.transferTo(1,x);

acquire lock for account x b/c transferTo is synchronized

acquire lock for account y b/c deposit is synchronized

release lock for account y after depost

release lock for account x at end of transferTo

acquire lock for account y b/c transferTo is synchronized

acquire lock for account x b/c deposit is synchronized

release lock for account x after deposit

release lock for account y at end of transferTo

Resolving Deadlocks

- Deadlocks occur when there are multiple locks simultaneously needed to complete a task, and different threads may obtain them in a different order
- Option 1: Address the number of locks
 - Have a coarser lock granularity
 - E.g. one lock for ALL bank accounts
- Option 2: Address simultaneous need
 Have a finer critical section so that only one lock is needed at a time
 - E.g. instead of a synchronized transferTo, have the withdraw and deposit steps locked separately
- Option 3: Address order of acquisition
 - Force the threads to always acquire the locks in the same order
 - E.g. make transferTo acquire both locks before doing either the withdraw or deposit, make sure both threads agree on the order to aquire

Option 1: Coarser Locking

```
static final Object BANK = new Object();
class BankAccount {
        synchronized void withdraw(int amt) {...}
        synchronized void deposit(int amt) {...}
        void transferTo(int amt, BankAccount a) {
                `synchronized(BANK){
                        this.withdraw(amt);
                        a.deposit(amt);
```

Option 2: Finer Critical Section

```
class BankAccount {
       synchronized void withdraw(int amt) {...}
       synchronized void deposit(int amt) {...}
       void transferTo(int amt, BankAccount a) {
              synchronized(this){
                      this.withdraw(amt);
              synchronized(a){
                      a.deposit(amt);
```

Option 3: First Get All Locks In A Fixed Order

class BankAccount { synchronized void withdraw(int amt) {...} synchronized void deposit(int amt) {...} void transferTo(int amt, BankAccount a) { fif (this.acctNum < a.acctNum){</pre> synchronized(this){ synchronized(a){ this.withdraw(amt); a.deposit(amt); }}} else { synchronized(a){ synchronized(this){ this.withdraw(amt); a.deposit(amt); }}}

Parallel Code Conventional Wisdom

Memory Categories

All memory must fit one of three categories:

- 1. Thread Local: Each thread has its own copy
- 2. Shared and Immutable: There is just one copy, but nothing will ever write to it
- 3. Shared and Mutable: There is just one copy, it may change
 - Requires Synchronization!

Thread Local Memory

- Whenever possible, avoid sharing resources
- Dodges all race conditions, since no other threads can touch it!
 - No synchronization necessary! (Remember Ahmdal's law)
- Use whenever threads do not need to communicate using the resource
 - E.g., each thread should have its on Random object
- In most cases, most objects should be in this category

Immutable Objects

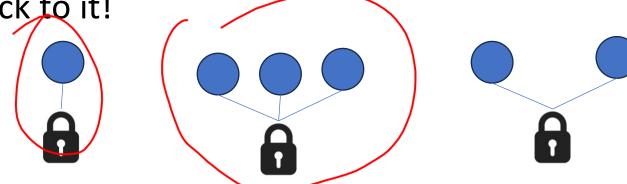
- Whenever possible, avoid changing objects
 - Make new objects instead
- Parallel reads are not data races
 - If an object is never written to, no synchronization necessary!
- Many programmers over-use mutation, minimize it

Shared and Mutable Objects

- For everything else, use locks
- Avoid all data races
 - Every read and write should be projected with a lock, even if it "seems safe"
 - Almost every Java/C program with a data race is wrong
- Even without data_races, it still may be incorrect
 - Watch for bad interleavings as well!

Consistent Locking

- For each location needing synchronization, have a lock that is always held when reading or writing the location
- The same lock can (and often should) "guard" multiple fields/objects
 - Clearly document what each lock guards!
 - In Java, the lock should usually be the object itself (i.e. "this")
- Have a mapping between memory locations and lock objects and stick to it!



Lock Granularity

- Coarse Grained: Fewer locks guarding more things each
 - One lock for an entire data structure
 - One lock shared by multiple objects (e.g. one lock for all bank accounts)
- Fine Grained: More locks guarding fewer things each
 - One lock per data structure location (e.g. array index)
 - One lock per object or per field in one object (e.g. one lock for each account)
- Note: there's really a continuum between them...

Example: Separate Chaining Hashtable

- Coarse-grained: One lock for the entire hashtable
- Fine-grained: One lock for each bucket
- Which supports more parallelism in insert and find?
- Which makes rehashing easier?
- What happens if you want to have a size field?

Tradeoffs

- Coarse-Grained Locking:
 - Simpler to implement and avoid race conditions
 - Faster/easier to implement operations that access multiple locations (because all guarded by the same lock)
 - Much easier for operations that modify data-structure shape
- Fine-Grained Locking:
 - More simultaneous access (performance when coarse grained would lead to unnecessary blocking)
 - Can make multi-location operations more difficult: say, rotations in an AVL tree
- Guideline:
 - Start with coarse-grained, make finer only as necessary to improve performance

Similar But Separate Issue: <u>Critical Section</u> Granularity

- Coarse-grained
 - For every method that needs a lock, put the entire method body in a lock
- Fine-grained
 - Keep the lock only for the sections of code where it's necessary
- Guideline:
 - Try to structure code so that expensive operations (like I/O) can be done outside of your critical section
 - E.g., if you're trying to print all the values in a tree, maybe copy items into an array inside your critical section, then print the array's contents outside.

Atomicity

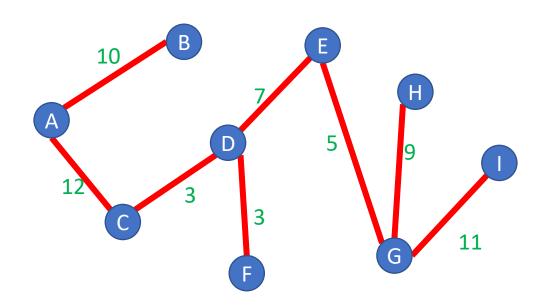
- Atomic: indivisible
- Atomic operation; one that should be thought of as a single step
- Some sequences of operations should behave as if they are one unit
 - Between two operations you may need to avoid exposing an intermediate state
 - Usually ADT operations should be atomic
 - You don't want another thread trying to do an insert while another thread is rotating the AVL tree
- Think first in terms of what operations need to be atomic
 - Design critical sections and locking granularity based on these decisions

Use Pre-Tested Code

- Whenever possible, use built-in libraries!
- Other people have already invested tons of effort into making things both efficient and correct, use their work when you can!
 - Especially true for concurrent data structures
 - Use thread-safe data structures when available
 - E.g. Java as ConcurrentHashMap

Definition: Tree

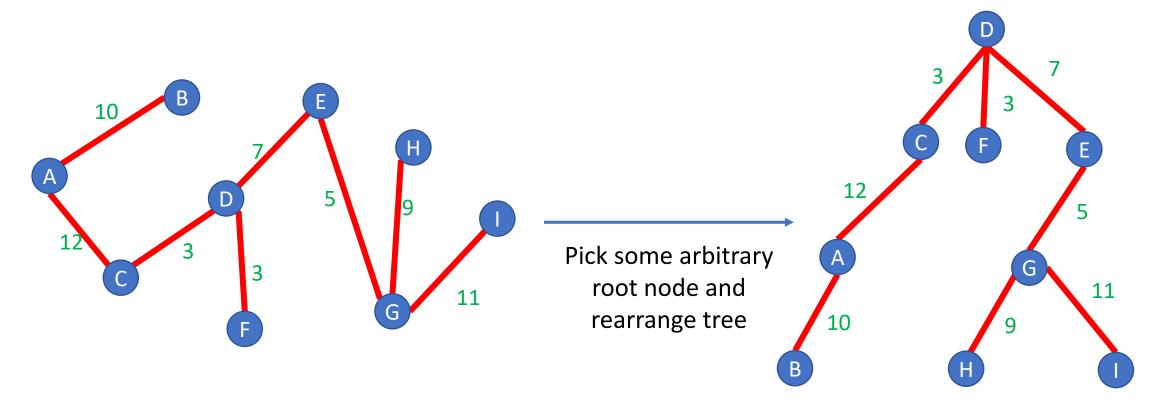
A connected graph with no cycles



Note: A tree does not need a root, but they often do!

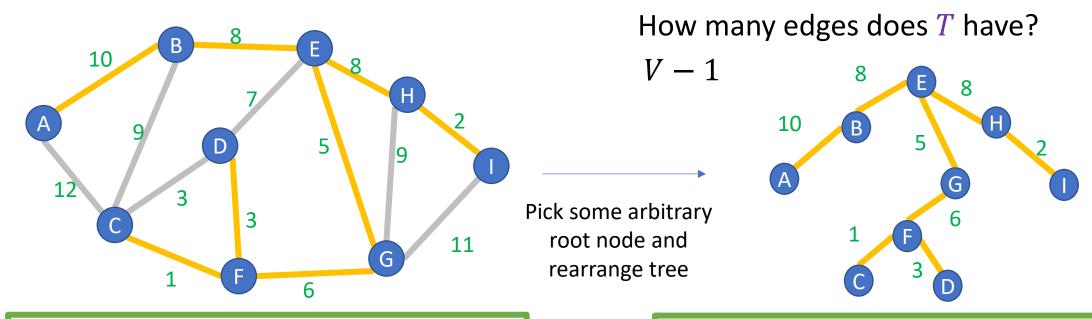
Definition: Tree

A connected graph with no cycles



Definition: Spanning Tree

A Tree $T = (V_T, E_T)$ which connects ("spans") all the nodes in a graph G = (V, E)

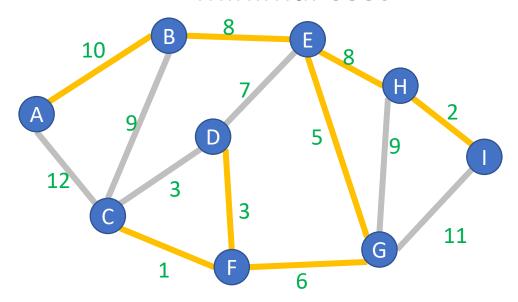


Any set of V-1 edges in the graph that doesn't have any cycles is guaranteed to be a spanning tree!

Any set of V-1 edges that connects all the nodes in the graph is guaranteed to be a spanning tree!

Definition: Minimum Spanning Tree

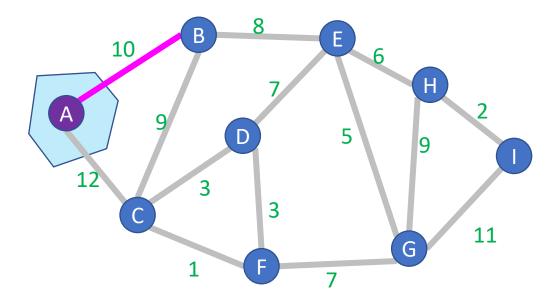
A Tree $T = (V_T, E_T)$ which connects ("spans") all the nodes in a graph G = (V, E), that has minimal cost



$$Cost(T) = \sum_{e \in E_T} w(e)$$

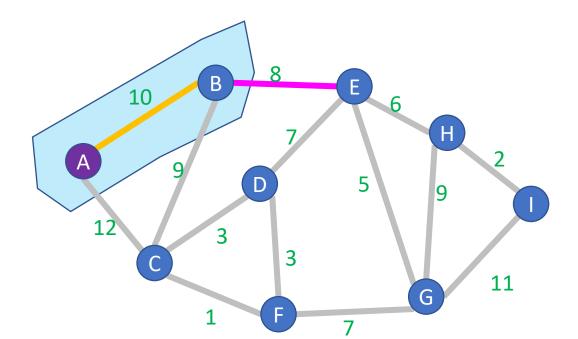
Pick a start node

Repeat V-1 times:



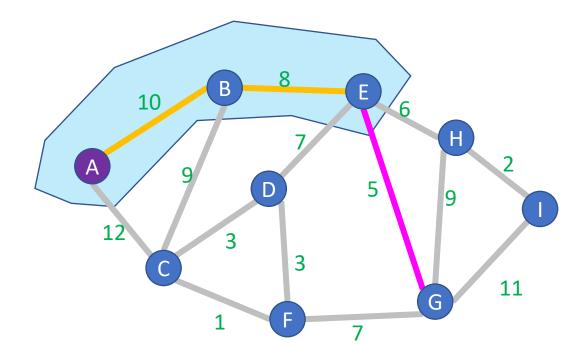
Pick a start node

Repeat V-1 times:



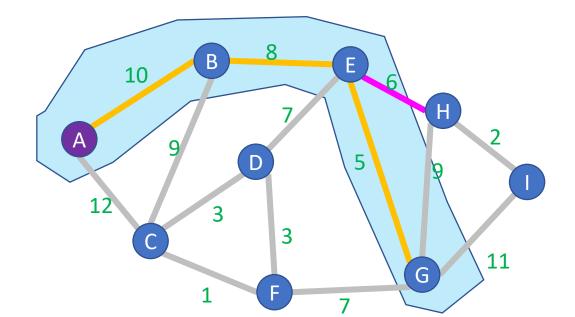
Pick a start node

Repeat V-1 times:



Pick a start node

Repeat V-1 times:



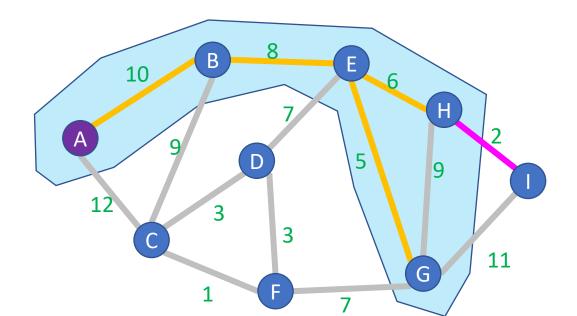
Prim's Algorithm

Start with an empty tree A

Pick a start node

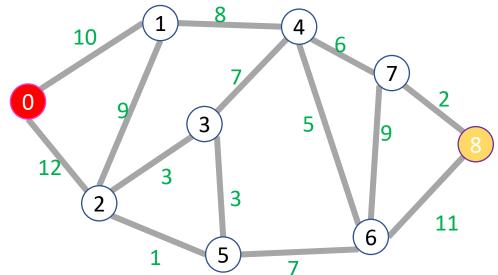
Repeat V-1 times:

Keep edges in a Heap $O(E \log V)$



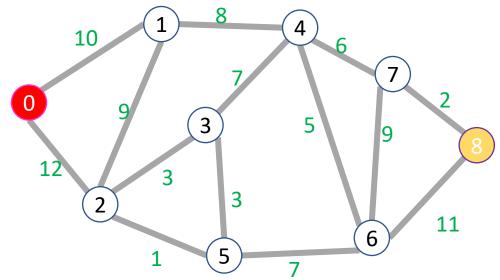
Dijkstra's Algorithm

```
int dijkstras(graph, start, end){
         PQ = new minheap();
         PQ.insert(0, start); // priority=0, value=start
         start.distance = 0;
         while (!PQ.isEmpty){
                  current = PQ.extractmin();
                  if (current.known){ continue;}
                  current.known = true;
                  for (neighbor : current.neighbors){
                           if (!neighbor.known){
                                    new_dist = current.distance + weight(current,neighbor);
                                    if(neighbor.dist != \infty){ PQ.insert(new_dist, neighbor);}
                                    else if (new_dist < neighbor. distance){</pre>
                                             neighbor. distance = new_dist;
                                             PQ.decreaseKey(new_dist,neighbor); }
         return end.distance;
```



Prim's Algorithm

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                  for (neighbor : current.neighbors){
                           if (!neighbor.known){
                                    new_dist = weight(current,neighbor);
                                    if(neighbor.dist != \infty){ PQ.insert(new_dist, neighbor);}
                                    else if (new_dist < neighbor. distance){</pre>
                                              neighbor. distance = new_dist;
                                              PQ.decreaseKey(new_dist,neighbor); }
         return end.distance;
```

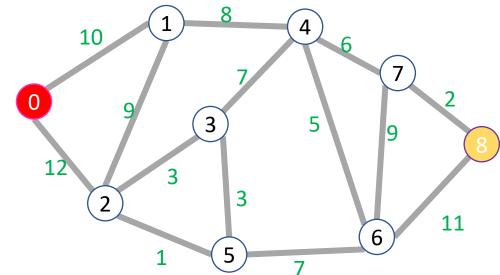


Dijkstra's Algorithm

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```

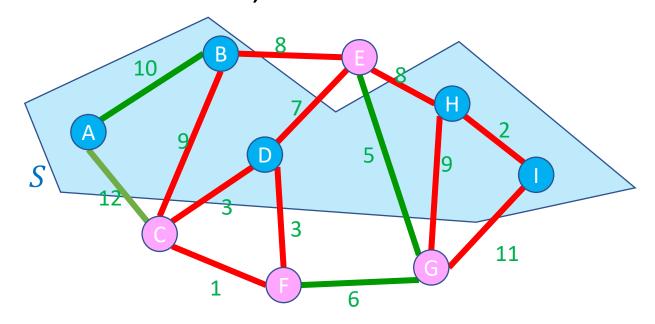
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         return end.distance;
```



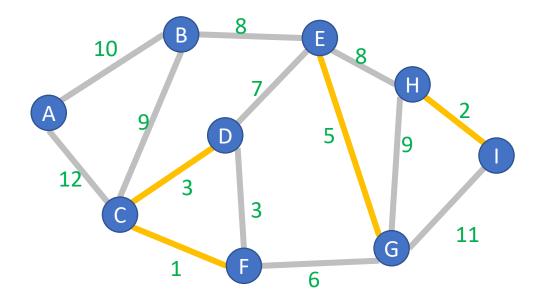
Definition: Cut

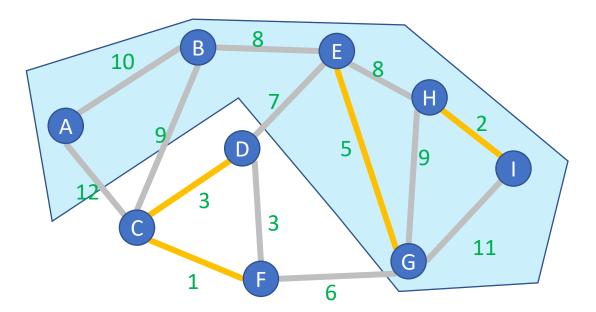
A Cut of graph G = (V, E) is a partition of the nodes into two sets, S and V - S

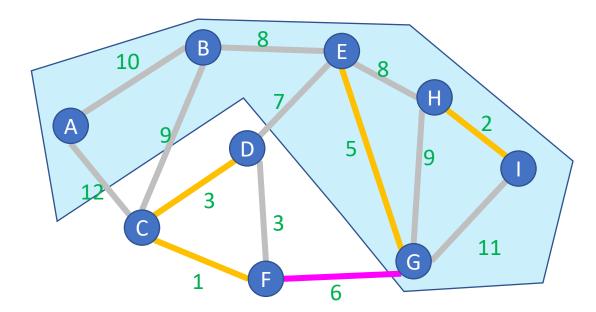


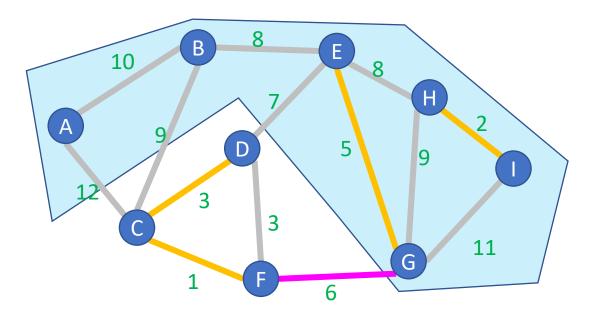
Edge $(v_1, v_2) \in E$ crosses a cut if $v_1 \in S$ and $v_2 \in V - S$ (or opposite), e.g. (A, C)

A set of edges R Respects a cut if no edges cross the cut e.g. $R = \{(A, B), (E, G), (F, G)\}$







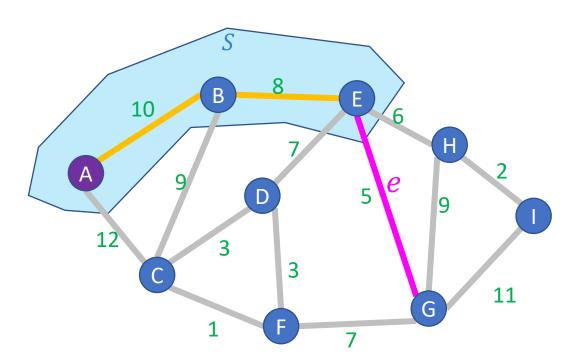


Proof of Prim's Algorithm

Start with an empty tree A

Repeat V-1 times:

Add the min-weight edge that connects to a node not currently in the tree



Proof: By Structural Induction

Suppose we have some arbitrary set of edges A that Prims's has already selected to include in the MST. e = (E, G) is the edge Prims's selects to add next

We know that there cannot exist a path from E to G using only edges in A because G has not been removed from the priority queue

We can cut the graph therefore into 2 disjoint sets:

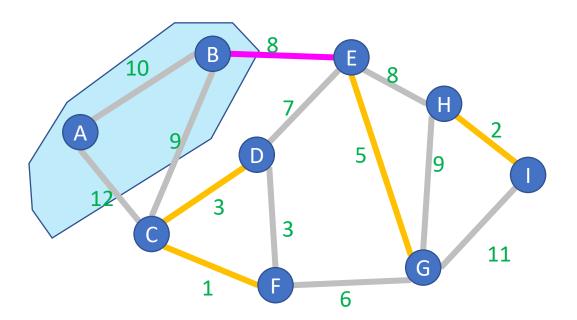
- Nodes that have been removed from the priority queue
- All other nodes

e is the minimum cost edge that crosses this cut, so by the Cut Theorem, Prim's only selects MST edges!
40

General MST Algorithm

Start with an empty tree ARepeat V-1 times:

> Pick a cut (S, V - S) which A respects (typically implicitly) Add the min-weight edge which crosses (S, V - S)



Prim's Algorithm

Start with an empty tree A

Repeat V-1 times:

Pick a cut (S, V - S) which A respects

Add the min-weight edge which crosses (S, V - S)

- S is all endpoint of edges in A
- e is the min-weight edge that grows the tree

