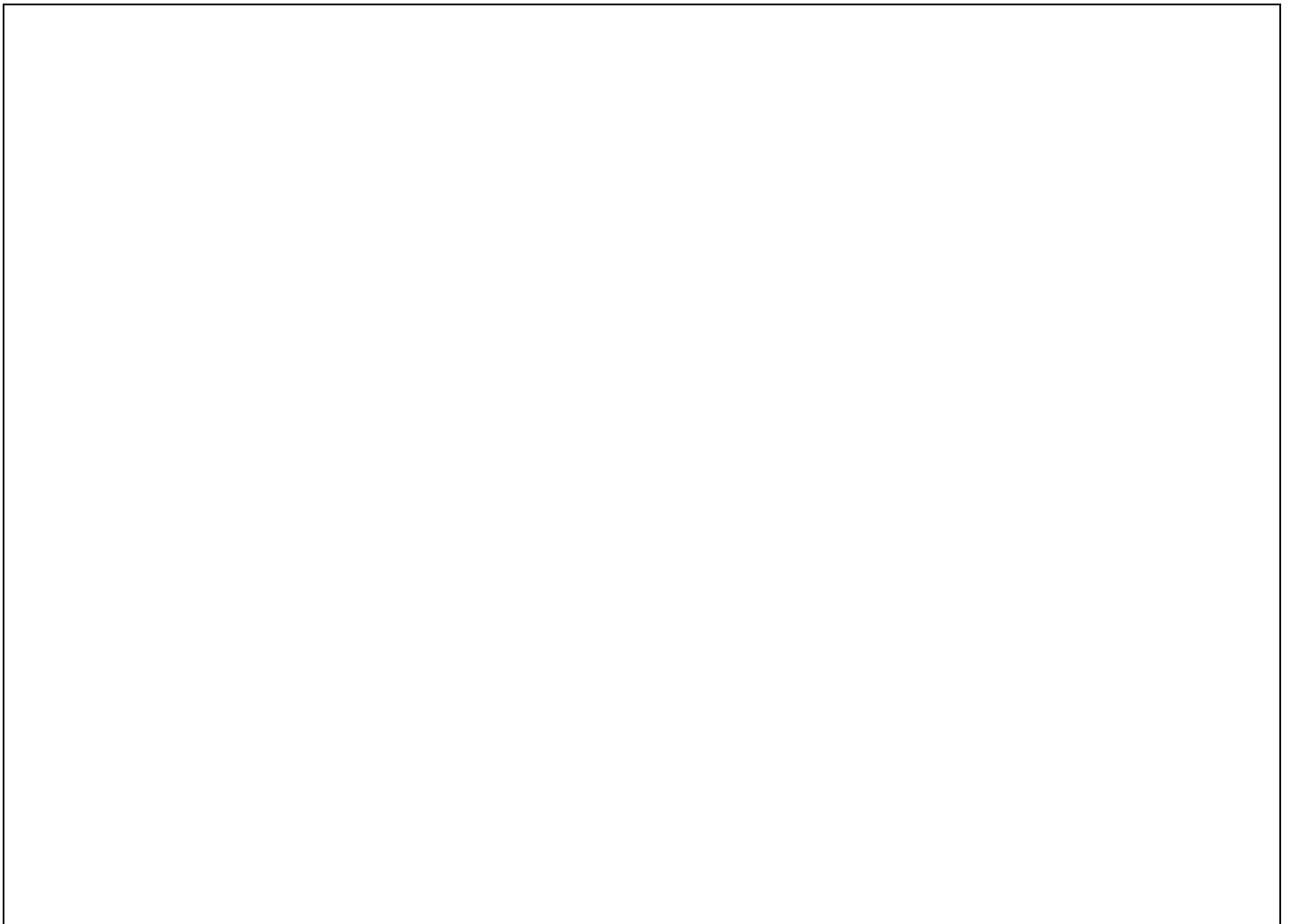


Section 7: Parallel Primitives & Concurrency Solutions

0. Parallel Prefix Sum

Given input array `[8, 9, 6, 3, 2, 5, 7, 4]`, output an array such that each `output[i] = sum(array[0], array[1], ..., array[i])`.

Use the [Parallel Prefix Sum](#) algorithm from lecture. Show the intermediate steps. Draw the input and output arrays, and for each step, show the tree of the recursive task objects that would be created (where a node's child is for two problems of half the size) and the fields each node needs. Do not use a sequential cut-off.

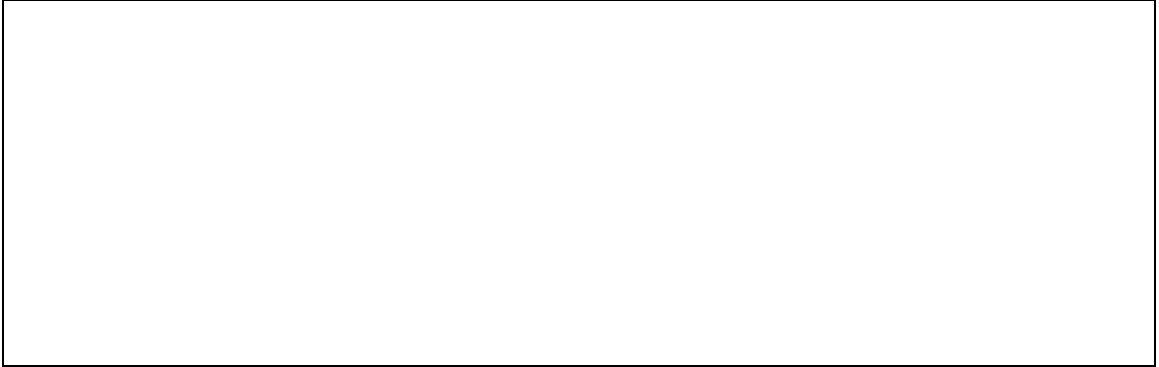


1. Parallel Prefix FindMin

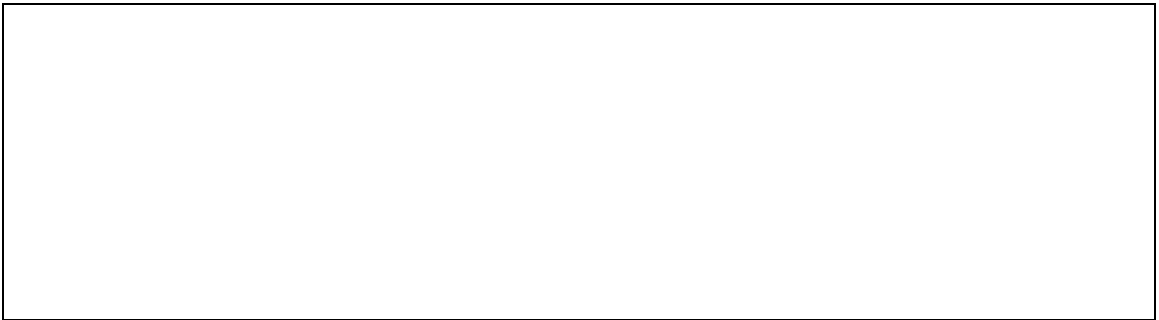
Given input array $[8, 9, 6, 3, 2, 5, 7, 4]$, output an array such that each $\text{output}[i] = \min(\text{array}[0], \text{array}[1], \dots, \text{array}[i])$. Show all steps, as above.

2. Work it Out [the Span]

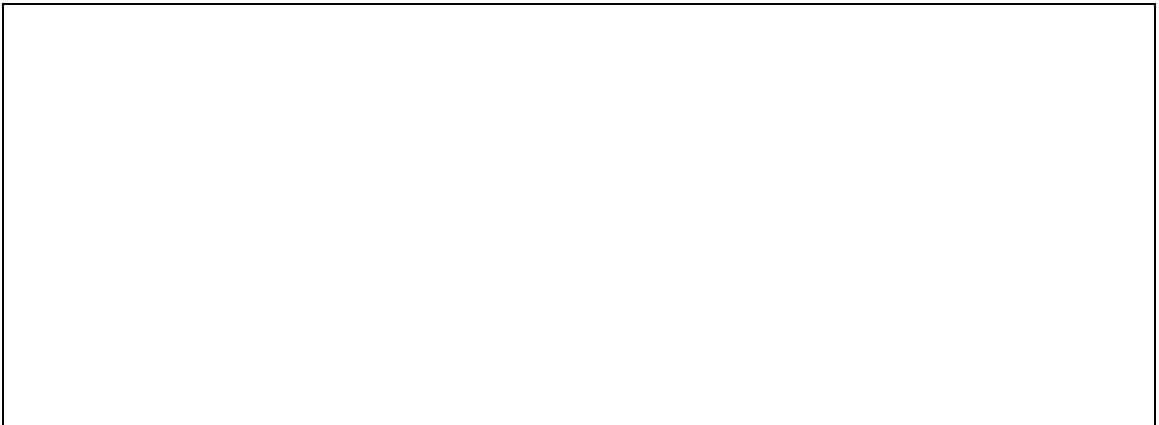
a) Define work and span



b) How do we calculate work and span?



c) Does adding more processors affect the work or span?

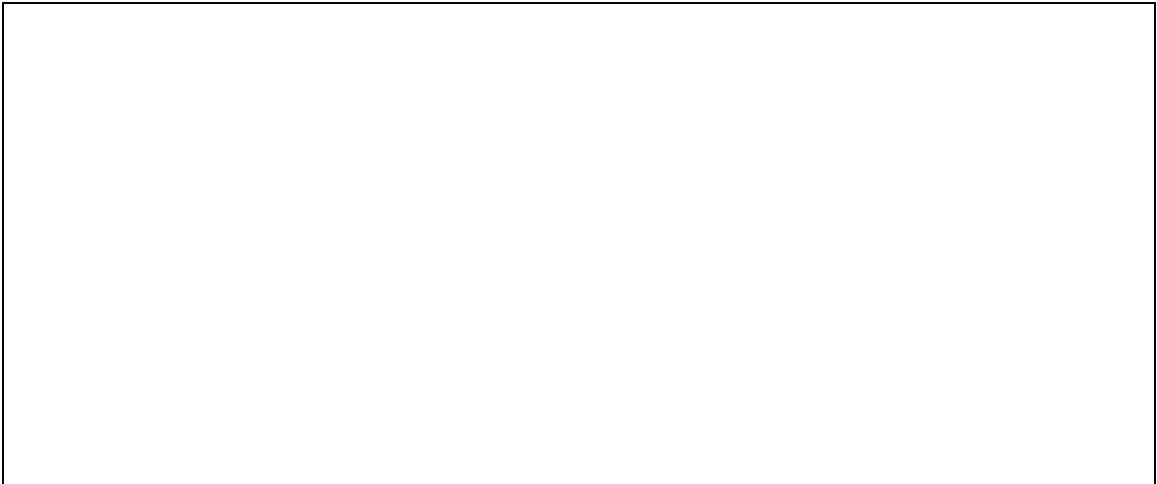


3. User Profile

You are designing a new social-networking site to take over the world. To handle all the volume you expect, you want to support multiple threads with a fine-grained locking strategy in which each user's profile is protected with a different lock. At the core of your system is this simple class definition:

```
1 class UserProfile {
2     static int id_counter;
3     int id; // unique for each account
4     int[] friends = new int[9999]; // horrible style
5     int numFriends;
6     Image[] embarrassingPhotos = new Image[9999];
7
8     UserProfile() { // constructor for new profiles
9         id = id_counter++;
10        numFriends = 0;
11    }
12
13    synchronized void makeFriends(UserProfile newFriend) {
14        synchronized(newFriend) {
15            if(numFriends == friends.length
16                || newFriend.numFriends == newFriend.friends.length)
17                throw new TooManyFriendsException();
18            friends[numFriends++] = newFriend.id;
19            newFriend.friends[newFriend.numFriends++] = id;
20        }
21    }
22
23    synchronized void removeFriend(UserProfile frenemy) {
24        ...
25    }
26 }
```

- a) The constructor has a concurrency error. What is it and how would you fix it? A short English answer is enough - no code or details required.



- b) The `makeFriends` method has a concurrency error. What is it and how would you fix it? A short English answer is enough no code or details required.



4. Bubble Tea

The `BubbleTea` class manages a bubble tea order assembled by multiple workers. Multiple threads could be accessing the same `BubbleTea` object. Assume the `Stack` objects are thread-safe, have enough space, and operations on them will not throw an exception.

```
1 public class BubbleTea {
2     private Stack<String> drink = new Stack<String>();
3     private Stack<String> toppings = new Stack<String>();
4     private final int maxDrinkAmount = 8;
5
6     // Checks if drink has capacity
7     public boolean hasCapacity() {
8         return drink.size() < maxDrinkAmount;
9     }
10
11    // Adds liquid to drink
12    public void addLiquid(String liquid) {
13        if (hasCapacity()) {
14            if (liquid.equals("Milk")) {
15                while (hasCapacity()) {
16                    drink.push("Milk");
17                }
18            } else {
19                drink.push(liquid);
20            }
21        }
22    }
23
24    // Adds newTop to list of toppings to add to drink
25    public void addTopping(String newTop) {
26        if (newTop.equals("Boba") || newTop.equals("Tapioca")) {
27            toppings.push("Bubbles");
28        } else {
29            toppings.push(newTop);
30        }
31    }
32 }
```


5. Phone Monitor

The `PhoneMonitor` class tries to help manage how much you use your cell phone each day. Multiple threads can access the same `PhoneMonitor` object. Remember that `synchronized` gives you reentrancy.

```
1 public class PhoneMonitor {
2     private int numMinutes = 0;
3     private int numAccesses = 0;
4     private int maxMinutes = 200;
5     private int maxAccesses = 10;
6     private boolean phoneOn = true;
7     private Object accessesLock = new Object();
8     private Object minutesLock = new Object();
9
10    public void accessPhone(int minutes) {
11        if (phoneOn) {
12            synchronized (accessesLock) {
13                synchronized (minutesLock) {
14                    numAccesses++;
15                    numMinutes += minutes;
16                    checkLimits();
17                }
18            }
19        }
20    }
21
22    private void checkLimits() {
23        synchronized (minutesLock) {
24            synchronized (accessesLock) {
25                if (numAccesses >= maxAccesses
26                    || numMinutes >= maxMinutes) {
27                    phoneOn = false;
28                }
29            }
30        }
31    }
32 }
```


a) Does the `PhoneMonitor` class as shown above have (circle all that apply):

a race condition potential for
 deadlock a data race none of these

If there are any problems, give an example of when those problems could occur. Be specific!

b) Suppose we made the `checkLimits` method public, and changed nothing else in the code. Does this modified `PhoneMonitor` class have (circle all that apply):

a race condition potential for
 deadlock a data race none of these

If there are any FIXED problems, describe why they are FIXED. If there are any NEW problems, give an example of when those problems could occur. Be specific!