

## Mathematical Formulas

### Gauss' Summation

$$\sum_{i=0}^n i = \frac{n(n+1)}{2}.$$

### Infinite Geometric Series

$$\sum_{i=0}^{\infty} x^i = \frac{1}{1-x}, \text{ where } -1 < x < 1.$$

### Finite Geometric Series

$$\sum_{i=0}^n x^i = \left(\frac{1}{1-x}\right) - \left(\frac{x^{n+1}}{1-x}\right) = \frac{1-x^{n+1}}{1-x}$$

### Logs

$$x^{\log_x n} = n$$

$$a^{\log_b c} = c^{\log_b a}$$

$$\log_b a = \frac{\log_a a}{\log_a b}$$

### Summations

$$\sum_{i=0}^n i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{i=0}^n i^3 = \frac{n^2(n+1)^2}{4}$$