CSE 332: Data Structures and Parallelism

Section 3: BSTs and Recurrences

0. Interview Question: Binary Search Trees

Write pseudo-code to perform an in-order traversal in a binary search tree without using recursion.

1. Recurrences and Closed Forms

For the following code snippet, find a recurrence for the worst case runtime of the function, and then find a closed form for the recurrence.

Consider the function f:

```
1 f(n) {
2    if (n == 0) {
3      return 1;
4    }
5    return 2 * f(n - 1) + 1;
6 }
```

• Find a recurrence for f(n).

• Find a closed form for f(n).

2. Recurrences and Big-Oh Bounds

Consider the function f. Find a recurrence modeling the worst-case runtime of this function and then find a Big-Oh bound for this recurrence.

```
if (n == 0) {
3
         return 0
5
      int result = 0
6
7
      for (int i = 0; i < n; i++) {
8
         for (int j = 0; j < i; j++) {
9
            result += j
10
         }
11
12
      return f(n/2) + result + f(n/2)
13
14 }
```

(a) Find a recurrence T(n) modeling the worst-case time complexity of f(n).

(b) Find a Big-Oh bound for your recurrence.

3. Recurrences and Closed Forms

Consider the function g. Find a recurrence modeling the worst-case runtime of this function, and then find a closed form for the recurrence.

```
g(n) {
      if (n <= 1) {
3
         return 1000
4
      if (g(n/3) > 5) {
5
         for (int i = 0; i < n; i++) {
6
7
            println("Yay!")
8
9
         return 5 * g(n/3)
10
      }
      else {
11
         for (int i = 0; i < n * n; i++) {
12
            println("Yay!")
13
14
15
         return 4 * g(n/3)
16
      }
17 }
```

(a) Find a recurrence T(n) modeling the worst-case time complexity of g(n).

(b) Find a closed form for the above recurrence.

4. Runtime Complexity

Consider the function h:

```
1 h(n) {
2    if (n <= 1) {
3      return 1
4    } else {
5      return h(n/2) + n + 2*h(n/2)
6    }
7 }</pre>
```

(a) Find a recurrence T(n) modeling the worst-case runtime complexity of h(n).

(b) Find a closed form to your answer for (a).