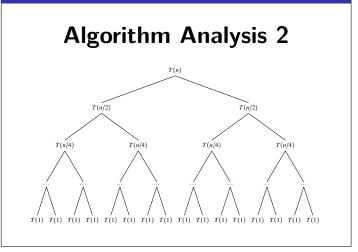
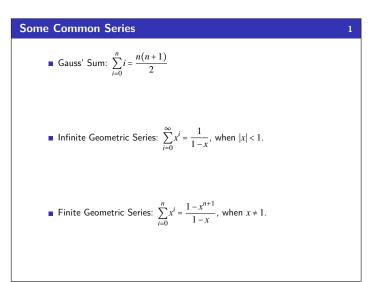
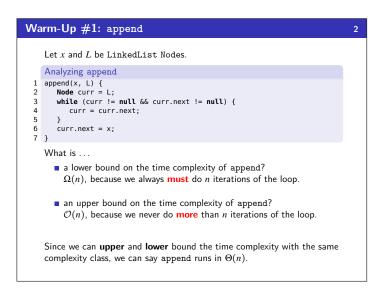


CSE 332: Data Structures and Parallelism



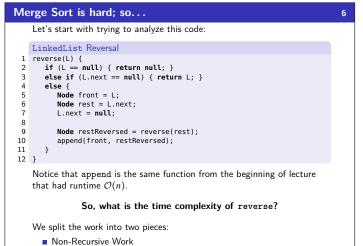




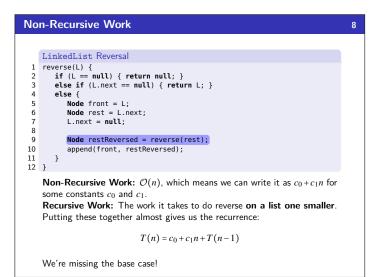


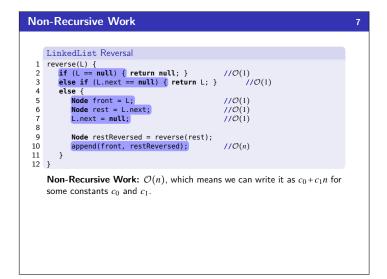
Merge		
	Pre-Condition: <i>L</i> ₁ and <i>L</i> ₂ are sorted. Post-Condition: Return value is sorted.	
1 2 3 4 5 6 7 8	<pre>Merge merge(L₁, L₂) { p1, p2 = 0; While both lists have more elements: Append the smaller element to L. Increment p1 or p2, depending on which had the smaller element Append any remaining elements from L₁ or L₂ to L return L }</pre>	
	 What is the(remember the lists are Nodes) best case # of comparisons of merge? Ω(1). Consider the input: [0], [1, 2, 3, 4, 5, 6]. 	
	 worst case # of comparisons of merge? O(n). Consider the input: [1, 3, 5], [2, 4, 6]. worst case space usage of merge? O(n), because we allocate a constant amount of space per element. 	

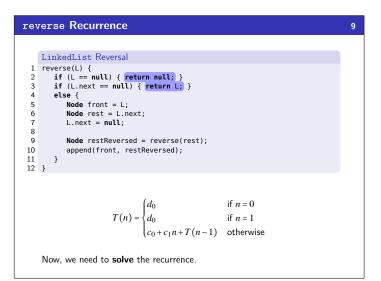
Well, we did merge, what did you think was next? 4	Recurrences	
Consider the following code:	What is a recurrence?	
Merge Sort		
<pre>sort(L) { if (L.size() < 2) { return L; } else { int mid = L.size() / 2; return merge(sort(L.subList(0, mid)), sort(L.subList(mid, L.size()))); } }</pre>	In CSE 311, you saw a bunch of questions like:	
	Induction Problem	
	Let $f_0 = 0, f_1 = 1, f_n = f_{n-1} + f_{n-2}$ for all $n \ge 2$. Prove $f_n < 2^n$ for all $n \in \mathbb{N}$.	
	(Remember the Fibonacci Numbers? You'd better bet they're going to show up in this course!)	
12 }	That's a recurrence. That's it.	
What is the worst case/best case # of comparisons of sort?	Definition (Recurrence)	
Yeah, yeah, it's $\mathcal{O}(n \lg n)$, but why?	A recurrence is a recursive definition of a function in terms of smaller values.	

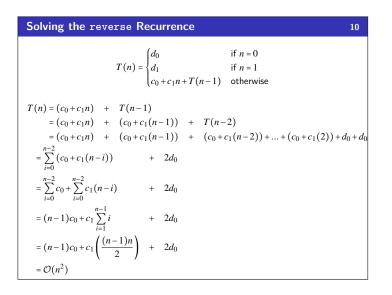


- Recursive Work









Today's Takeaways!

- Understand that Big-Oh is just an "upper bound" and Big-Omega is just a "lower bound"
- Know how to make a recurrence from a recursive program
- Understand what a linear recurrence is
- Be able to find a closed form linear recurrences
- Know the common summations

