

True or False?

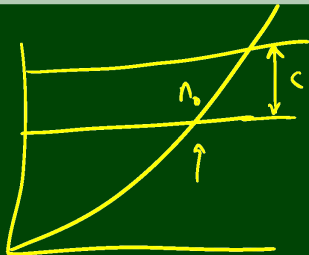
(1) $4 + 3n \in \mathcal{O}(n)$

(2) $4 + 3n = \mathcal{O}(1)$

(3) $4 + 3n$ is $\mathcal{O}(n^2)$

(4) $n + 2\log n \in \mathcal{O}(\log n)$

(5) $\log n \in \mathcal{O}(n + 2\log n)$



True or False?

- (1) $4 + 3n \in \mathcal{O}(n)$ True ($n = n$)
- (2) $4 + 3n = \mathcal{O}(1)$ False: ($n \gg 1$)
- (3) $4 + 3n$ is $\mathcal{O}(n^2)$ True: ($n \leq n^2$)
- (4) ~~$n + 2 \log n \in \mathcal{O}(\log n)$~~
- (5) $\log n \in \mathcal{O}(n + 2 \log n)$

Definition (Big-Oh)

We say a function $f : A \rightarrow B$ is **dominated by** a function $g : A \rightarrow B$ when:

$$\exists(c, n_0 > 0). \forall(n \geq n_0). f(n) \leq cg(n)$$

Formally, we write this as $f \in \mathcal{O}(g)$.

We want to prove $4 + 3n \in \mathcal{O}(n)$. That is, we want to prove:

$$\exists(c, n_0 > 0). \forall(n \geq n_0). 4 + 3n \leq cn$$

Proof Strategy

SW) $4 + 3n \leq cn$

$4 + 3n \leq 4n \leq cn$

$n_0 = 4$
 $c = 4$

Definition (Big-Oh)

We say a function $f : A \rightarrow B$ is **dominated by** a function $g : A \rightarrow B$ when:

$$\exists(c, n_0 > 0). \forall(n \geq n_0). f(n) \leq cg(n)$$

Formally, we write this as $f \in \mathcal{O}(g)$.

We want to prove $4 + 3n + 4n^2 \in \mathcal{O}(n^3)$.

$$4 + 3n + 4n^2 \leq 4n^3 + 3n^3 + 4n^3 \leq cn^3$$

$$n_0 = 1$$

$$c = 11$$

