## CSE 332

## JULY 31st - ALPHA BETA

## ADMINISTRIVIA

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- Partners form filled out by noon today!
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- Considerations for final exam
- 1 hour is going to be difficult to cover all of the material


## MINIMAX REVIEW

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- Two players
- Zero sum
- Perfect information
- Works around a decision tree
- Let's look at a simple game... tic-toe
- Players assume that the other team is playing optimally
- Compute, what would I do if I was in the other persons shoes


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- How to parallelize minimax?
- Java uses the ForkJoinPool around RecursiveTasks, what are the important things the task needs to do and know?


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- Other lessons?
- The task should create other recursive tasks to find the results of the possible moves.


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- Could be multiple boards, or just taking the time to do multiple boards


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- Exercise due Friday involves you experimenting with the findPrimes parallel program we've given you, adding the forking cutoff and then running some experimentation
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- No, we can perform alpha-beta pruning


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- Therefore, alpha and beta need to be switching throughout the tree
- Cheating with Adam's slides
- https://courses.cs.washington.edu/courses/cse332/17wi/ lectures/p3/p3.pdf


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- All of the moves at this first level need to be calculated, you can't know for sure that you can/cannot improve
- Remember, then, the number of nodes alpha-beta can prune is dependent on the order that they are considered.
- Move ordering is a good heuristic for p3 to save some time


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- So, first try to run minimax/alphabeta at depth $k$, then if you have time, run minimax/alphabeta at depth $\mathrm{k}+1$.


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- One final topic about P3
- Chess is a timed game, so you want to balance time spent with how much computing you'll need
- So, first try to run minimax/alphabeta at depth $k$, then if you have time, run minimax/alphabeta at depth $\mathrm{k}+1$.
- We won't be having you compete against bots, but we will be having you compete against a timer, you can only have so much time per move.


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- Together, these are powerful tools of parallelism, but they may not be sufficient


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- Pack
- Filter the array subject to some conditions


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- How do you find the value of a particular node?


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- Think about applying a sum reduce!


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- What is the actual function?
- Value is going to be the presum + the current value
- These presum values are going to be reused!
- How would you apply a sum reduce!
- Scan trees!

