

P3

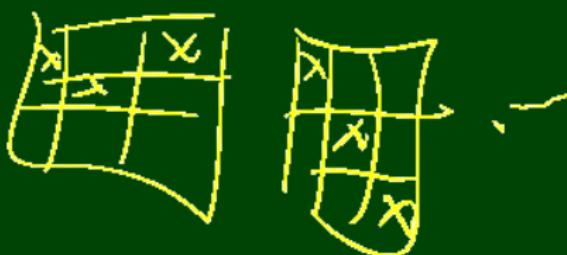
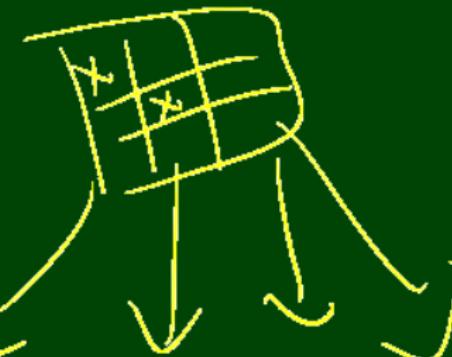
Yay!



Recursion To The Rescue

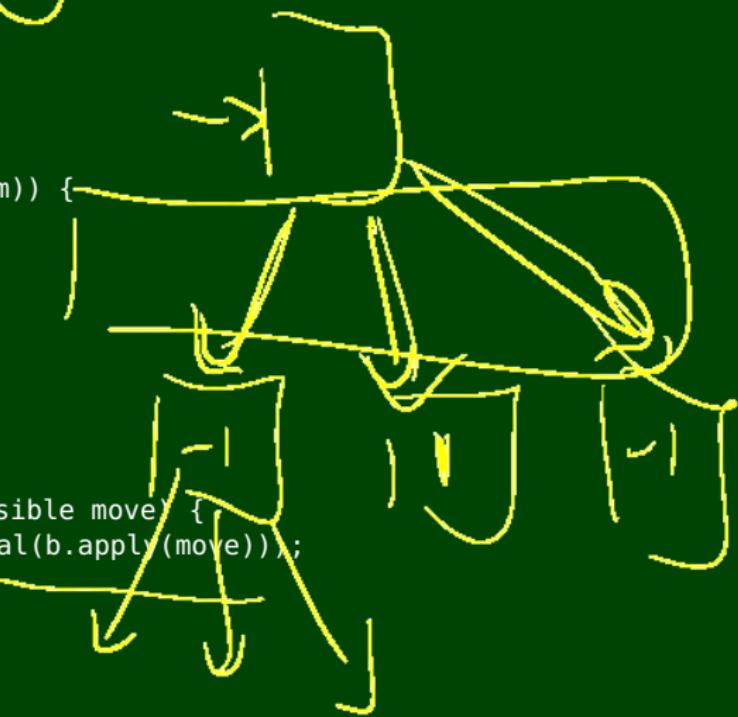
4

```
1 boolean win(Board b) {  
2     if (b.threeXs()) {  
3         return true;  
4     }  
5     else {  
6         for (Move m : every possible move) {  
7             if (win(b.do(move))) {  
8                 return true;  
9             }  
10        }  
11    }  
12 }
```



{ win \leftrightarrow opp loses

```
1 // +1 is a win; +0 is a draw; -1 is a loss
2 int eval(Board b) {
3     if (b.gameOver()) {
4         if (b.hasThree(me)) {
5             return 1;
6         }
7         else if (b.hasThree(them)) {
8             return -1;
9         }
10    else {
11        return 0;
12    }
13 }
14 else {
15     int best = -1;
16     for (Move m : every possible move) {
17         best = max(best, eval(b.apply(move)));
18     }
19     return best;
20 }
```



A Game of Tic-Tac-Toe

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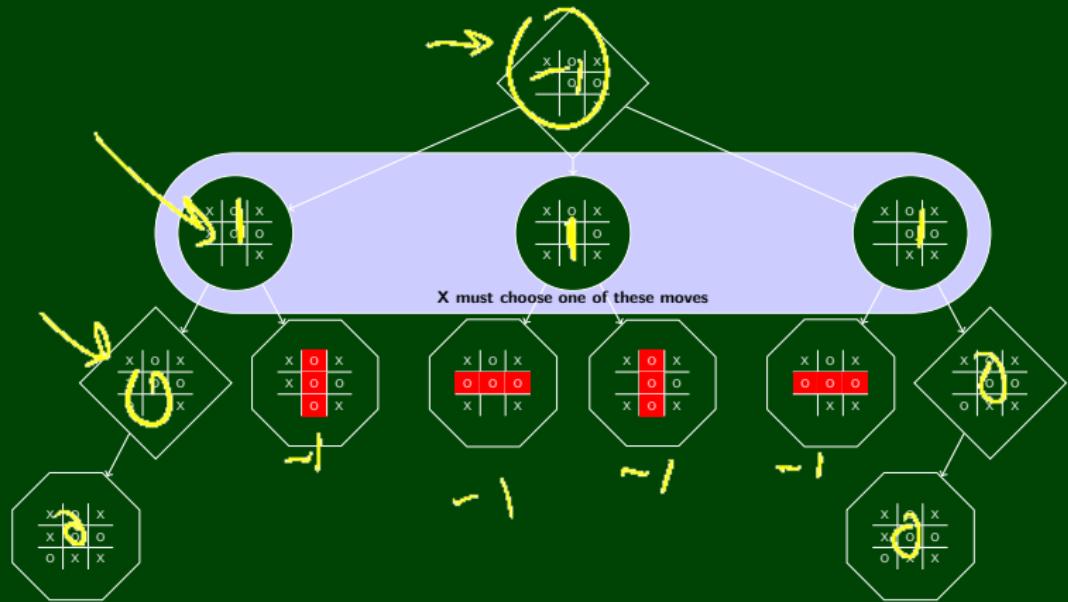
X's Turn

O's Turn

X's Turn

O's Turn

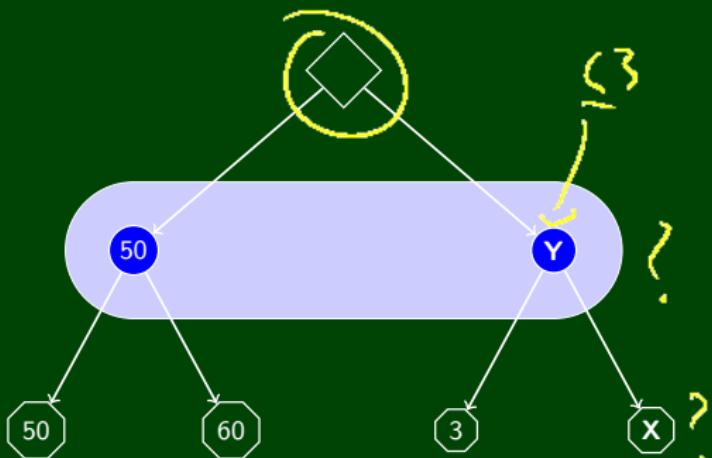
X must choose one of these moves



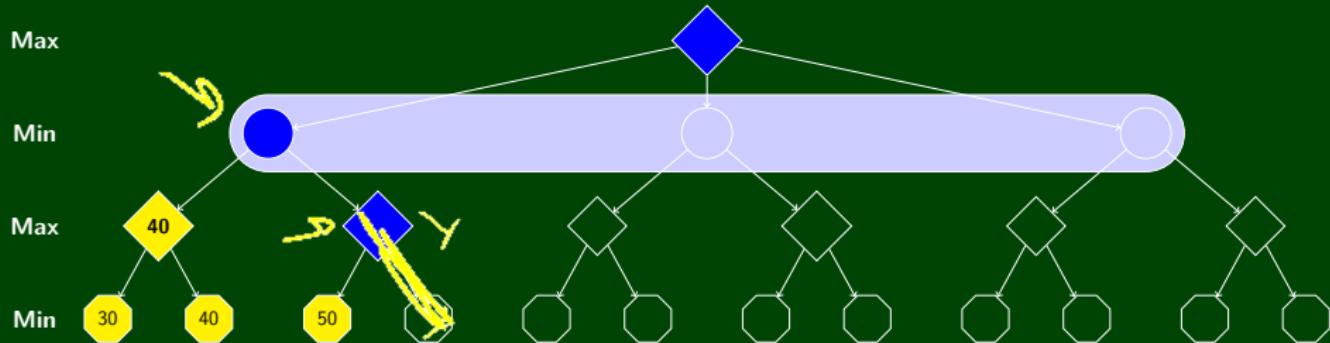
Max's Turn

Min's Turn

Max's Turn



$$Y = \min\{3, x\}$$



$$Y = \max(s_0, x)$$

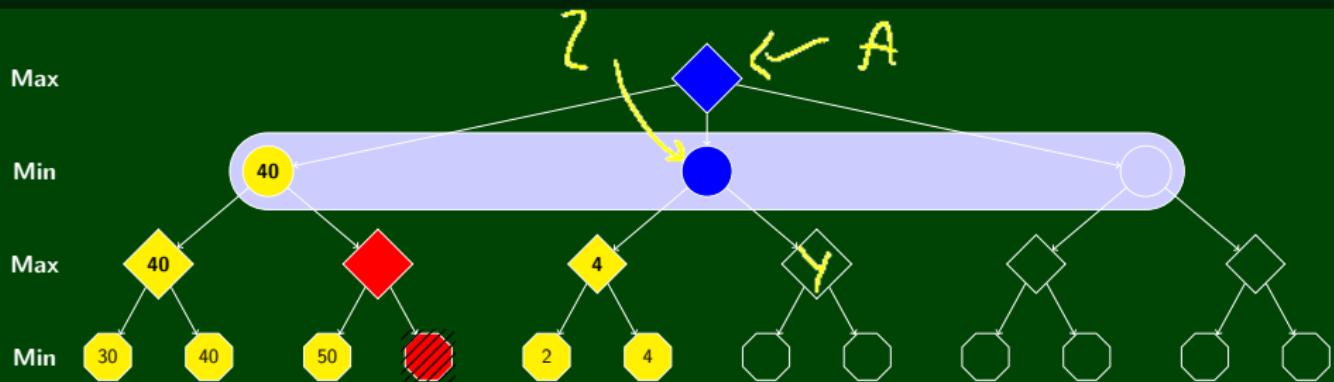
Do we check the next node?

Max will choose $x \geq 50$ which is already worse than the 40.

The current bounds are $[50, 40]$. Don't bother.

Pruning

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$$A = \max(40, \epsilon)$$

$$Z \leq 4$$

$$Z = \min(4, Y)$$

$$40 \leq A$$

$$Y$$