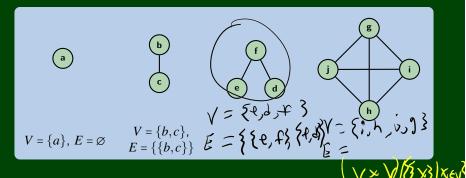
# A Graph is a Thingy...



We call the circles vertices and the lines edges.

#### Definition (Graph)

A **Graph** is a pair, G = (V, E), where:

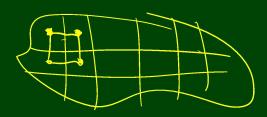
- V is a set of vertices, and
- *E* is a set of **edges** (pairs of vertices).

# **Modelling Problems with Graphs**

### To model a problem with a graph, you need to make two choices

- 1 What are the vertices?
- 2 What are the edges?
- Maps
- The Internet
- Social Networks
- A Running Program
- A Chess Game
- Telephone Lines
- CSE Courses

With these in mind, let's talk about more crucial definitions.



## **Modelling Problems with Graphs**

To model a problem with a graph, you need to make two choices

1 What are the vertices?

2 What are the edges?

Maps

Vertices: regions; Edges: "is next to"

The Internet

Vertices: websites; Edges: "has a link to"

Social Networks

Vertices: people; Edges: "is friends with"

A Running Program

Vertices: methods; Edges: "calls"

A Chess Game

Telephone Lines

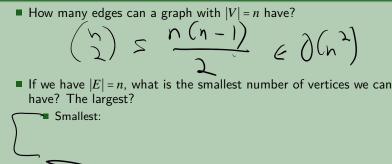
CSE Courses

With these in mind, let's talk about more crucial definitions.

## More Important Graphs



#### Some Questions



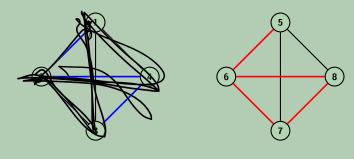
## Walks and Paths

### Definition (Walk)

A walk in a graph G = (V, E) is a list of vertices:  $v_0, v_1, \ldots, v_n$  such that  $\{v_i, v_{i+1}\} \in E$ . Intuitively, a path from u to v is a continuous line drawn without picking up your pencil.

### Definition (Path)

A **path** in a graph G = (V, E) is a walk with no repeated vertices.



## Definition (Connected Graph)

We say a graph is connected if for every pair of vertices,  $u, v \in V$ , there is a path from u to v.



# A "Worklist"

A very common type of algorithm on graphs is a worklist algorithm.

Recall the WorkList ADT:

WorkList ADT



add( <b>v</b> )	Notifies the worklist that it must handle <b>v</b>
next()	Returns the next vertex to work on
hasWork()	Returns true if there's any work left and false otherwise

Importantly, we **do not care how** the worklist manages the work. (Okay, we do, but not when coming up with the algorithm.)

Worklist algorithms will always look like the following:

```
1 worklist = /* add initial work to worklist */ {
2 while (worklist.hasWork()) {
3     v = worklist.next(); {
4     doWork(v); {
5 }
```