



CSE 332: Data Abstractions

Dictionaries & Trees

P1 De-Brief

- You did something substantial!
- You worked with "real world software"
- You honed your debugging skills
- You "transitioned" from 143 to 332
- You enjoyed it?? (okay, not the debugging, but...)

Oh, some presents...

- tokens++
- EX06, EX07, EX08 Now Due Thursday

While we're here...

- Proofs review session?
- Overwhelmed?

ADT's So Far

Where We've Been So Far

- Stack (Get LIFO)
- Queue (Get FIFO)
- Priority Queue (Get By Priority)

 $\sqrt{1}$

2 Vanilla BSTs

A New ADT: "Dictionaries" (Also called "Maps") 3 Dictionary ADT Data Set of (key, value) pairs insert(key, val) Places (key, val) in map (overwrites existing val entry) find(key) Returns the \boldsymbol{val} currently associated to \boldsymbol{key} delete(key) deletes any pair relating key from the map Keys Values "such strings' "goodbye /ery $\texttt{find}(\texttt{``such strings''}) \rightarrow 12$

Today, we begin discussing Maps. This ADT is hugely important.

Sets and Maps

Dictionaries are the more general structure, but, in terms of implementation, they're nearly identical.

In a Set, we store the key directly, but conceptually, there's nothing different in storing an Item:

class Item { 1 Data key; 2 3 4 } Data value:

The Set ADT usually has our favorite operations: intersection, union, etc.

Notice that union, intersection, etc. still make sense on maps!

As always, depending on our usage, we might choose to $\operatorname{add}/\operatorname{delete}$ things from out ADT.

Bottom Line: If we have a set implementation, we also have a valid dictionary implementation (and vice versa)!

Dictionaries Are The BEST!

It turns out dictionaries are super useful. They're a natural generalization of arrays. Instead of storing data at an index, we store data at anything.

- Networks: router tables
- Operating Systems: page tables
- Compilers: symbol tables
- Databases: dictionaries with other nice properties
- \blacksquare Search: inverted indexes, phone directories, \ldots
- Biology: genome maps

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Dictionary Implementations, Take # 1

For each of the following potential implementations, what is the worst case runtime for insert, find, delete?

- Unsorted Array **Insert** by searching for existence and inserting which is O(n)**Find** by linear search which is $\mathcal{O}(n)$ **Delete** by linear search AND shift which is $\mathcal{O}(n)$
- Unsorted Linked List **Insert** by searching for existence and inserting which is $\mathcal{O}(n)$ **Find** by linear search which is $\mathcal{O}(n)$ **Delete** by linear search AND shift which is $\mathcal{O}(n)$
- Sorted Linked List **Insert** by searching for existence and inserting which is O(n)**Find** by linear search which is $\mathcal{O}(n)$ **Delete** by linear search AND shift which is $\mathcal{O}(n)$

 Sorted Array List **Insert** by binary search AND shift which is $\mathcal{O}(n)$ **Find** by binary search which is $O(\lg n)$ **Delete** by binary search AND shift which is $\mathcal{O}(n)$

Where The Idea Comes From

Binary Search is great! It's the only thing that was even sort of fast in that table. But insert and delete are really bad into a sorted array. Store the data in a structure where most of the data isn't accessed.

Interestingly, this is very similar to what made heaps useful!

To put it another way, by storing the data in an array, we're paying for the constant-time access that we're never even using!

It's okay that it takes more time to access certain elements.

... as long as it's never too bad.

Definition (Vanilla BST)

A binary tree is a BST when an in-order traversal of the tree yields a sorted list.

To put it another way, a binary tree is a BST when:

- All data "to the left of" a node is less than it
- All data "to the right of" a node is greater than it
- All sub-trees of the binary tree are also BSTs

Dictionary Implementations, Take # ?? It turns out there are many different ways to do much better. But they all have their own trade-offs!

So, we'll study many of them:

- "Vanilla BSTs" today (vanilla because they're "plain")
- "Balanced BSTs" there are many types: we'll study AVL Trees
- "B-Trees" another strategy for a lot of data
- "Hashtables" a completely different strategy (lack data ordering)
- We already saw another strategy: the amortized array dictionary

























Balance Condition?

- Left and right subtrees \u03c6f/th/e//00t recursively have the same number of nodes
- Left and right subtrees $\phi f/t h e/t \phi \phi t$ recursively have the same height

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These ideas suffer from the same problem:

They're way too strong. Only **perfect** trees satisfy them.

AVL Balance Condition! 22 Left and right subtrees recursively have heights differing by at most one. Definition (balance) balance(n) = abs(height(n.left) - height(n.right)) Definition (AVL Balance Property) An AVL tree is balanced when: For every node n, balance(n) ≤ 1 ■ This ensures a small depth (we'll prove this next time)

This ensures a small depth (we'll prove this next time)
 It's relatively easy to maintain (we'll see this next time)