CSE 332: Data Abstractions Sorting I

Spring 2016

Announcements

Sorting

Input

- an array A of data records
- a key value in each data record
- a comparison function which imposes a consistent ordering on the keys
- Output
 - "sorted" array A such that
 - For any i and j, if i < j then A[i] ≤ A[j]

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Consistent Ordering

- The comparison function must provide a *consistent ordering* on the set of possible keys
 - You can compare any two keys and get back an indication of a < b, a > b, or a = b (trichotomy)
 - The comparison functions must be consistent
 If compare (a,b) says a<b, then compare (b,a) must say b>a
 - If compare (a,b) Says a<b, then compare (b,a) Hust say b>a
 If compare (a,b) Says a=b, then compare (b,a) Must say b=a
 - If compare (a,b) SAYS a=b, then equals (a,b) and equals (b,a) must say a=b

Why Sort?

- Provides fast search:
- Find kth largest element in:

Space

- How much space does the sorting algorithm require?
 - In-place: no more than the array or at most O(1) addition space
 - out-of-place: use separate data structures, copy back
 - External memory sorting data so large that does not fit in memory

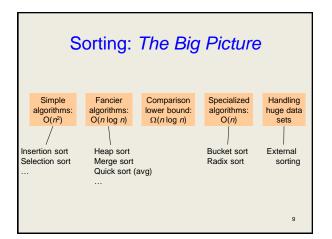
Stability

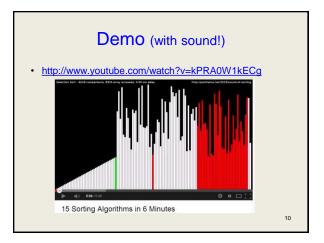
A sorting algorithm is stable if:

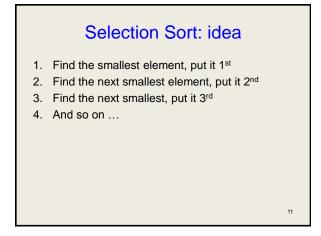
- Items in the input with the same value end up in the same order as when they began.

	Unstable so	nt	Stable Sor	τ
1	Adams	1	Adams	1
2	Smith	1	Smith	1
4	Washington	2	Black	2
2	Jackson	2	Jackson	2
4	Black	2	Washington	2
1	White	3	White	3
4	Wilson	3	Wilson	3
2	Thompson	4	Brown	4
3	Brown	4	Jones	4
3	Jones	4	Thompson	4
	4 2 4 1 4 2 3	2 Smith 4 Washington 2 Jackson 4 Black 1 White 4 Wilson 2 Thompson 3 Brown	2Smith14Washington22Jackson24Black21White34Wilson32Thompson43Brown4	2 Smith 1 Smith 4 Washington 2 Black 2 Jackson 2 Jackson 4 Black 2 Washington 1 White 3 White 4 Wilson 3 Wilson 2 Thompson 4 Brown 3 Brown 4 Jones

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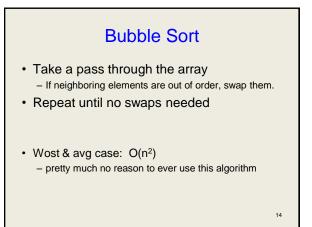


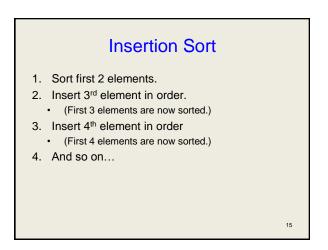


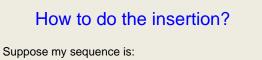




Selection S	Selection Sort: Code				
<pre>void SelectionSort (Arr for (i=0; i<n; ++i)<br="">j = Find index smalles Swap(a[i],a[j]) } }</n;></pre>	{ of st entry in a[in-1]				
Runtime: worst case best case : average case	:	13			



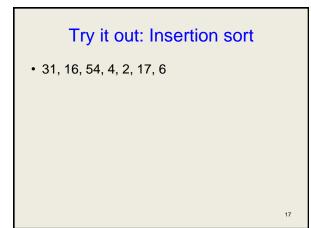


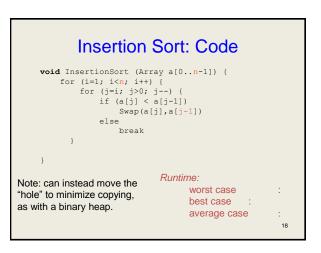


16, 31, 54, 78, 32, 17, 6

And I've already sorted up to 78. How to insert 32?

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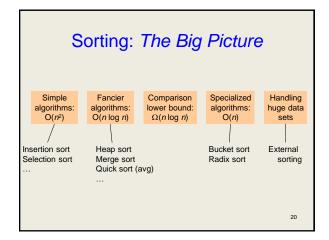




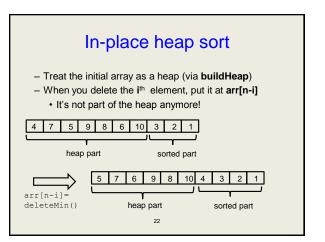
Insertion Sort vs. Selection Sort

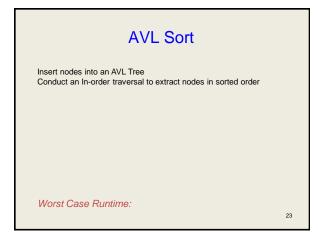
- Same worst case, avg case complexity
- · Insertion better best-case
 - preferable when input is "almost sorted"
 one of the best sorting algs for almost sorted case (also for small arrays)

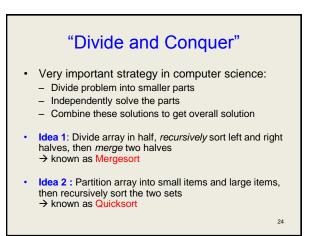
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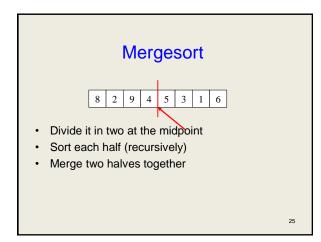


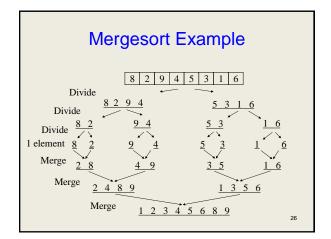


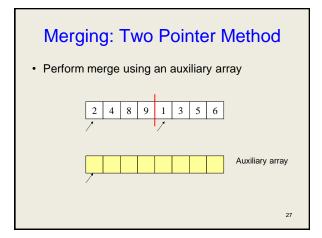




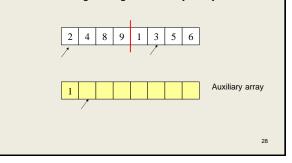


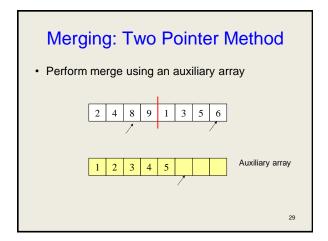


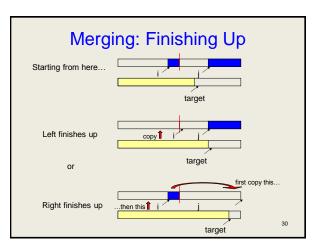


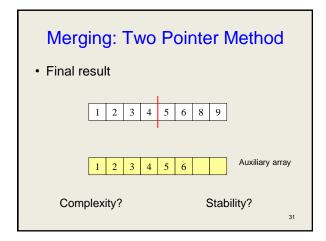




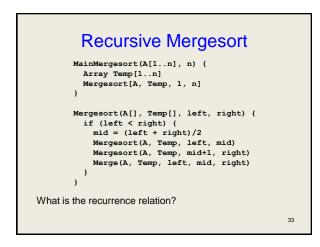


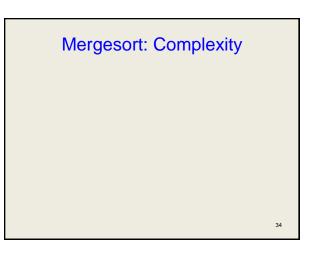


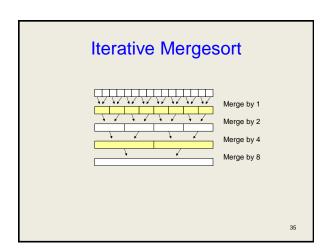


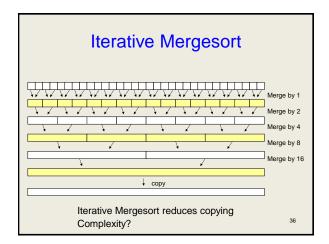


A[], Temp[], left, mid, right) {
: i, j, k, l, target
= left
= mid + 1
cget = left
le (i < mid && j < right) {
f(A[i] < A[j])
Temp[target] = A[i++]
alse
Temp[target] = A[j++]
arget++
-
(i > mid) //left completed//
for $(k = left to target-1)$
A[k] = Temp[k];
<pre>(j > right) //right completed//</pre>
x = mid
= right
while $(k \ge i)$
A[1] = A[k]
for $(k = left to target-1)$
A[k] = Temp[k] 32
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Properties of Mergesort

- In-place?
- Stable?
- Sorted list complexity?
- Nicely extends to handle linked lists.
- Multi-way merge is basis of big data sorting.
- Java uses Mergesort on Collections and on Arrays of Objects.

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