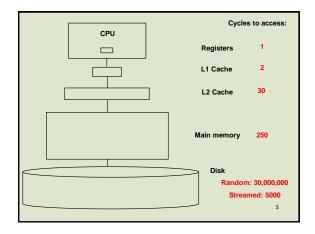
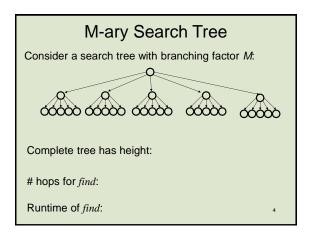
## CSE 332 Data Abstractions B-Trees

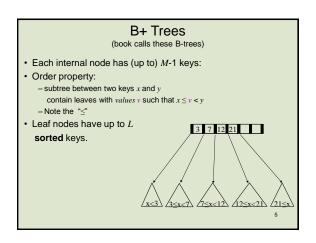
Richard Anderson Spring 2016

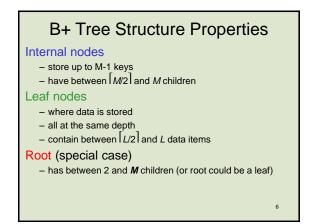
## Announcements

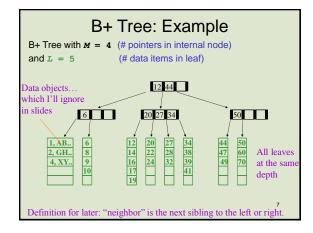
- · Next two weeks: Hashing and sorting
- Upcoming dates
- Friday, April 29. Midterm

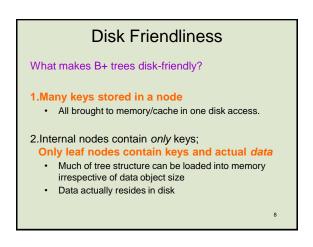




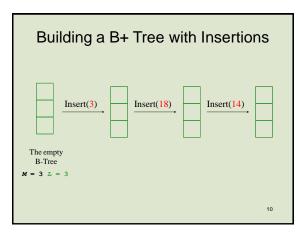


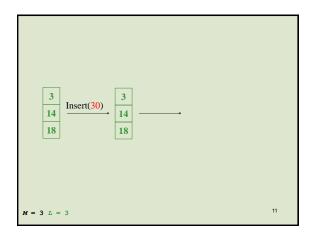


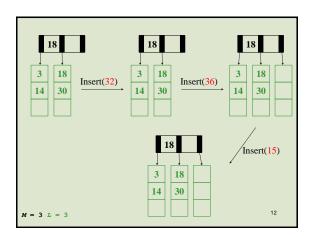


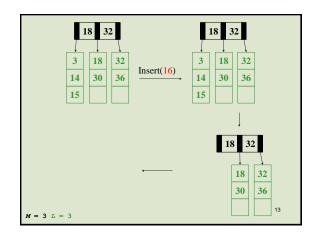


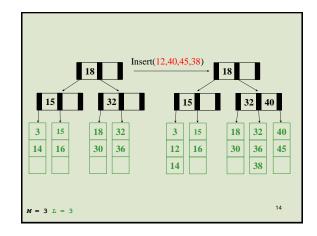
B+ trees vs. AVL trees
Suppose again we have n = 2<sup>30</sup> ≈ 10<sup>9</sup> items:
Depth of AVL Tree
Depth of B+ Tree with M = 256, L = 256
Great, but how to we actually make a B+ tree and keep it balanced...?

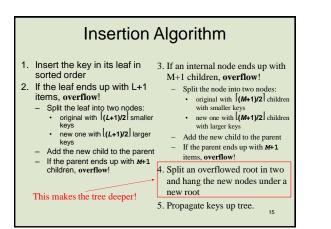


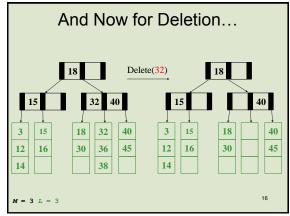


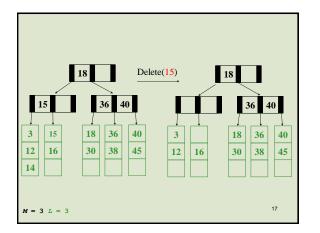


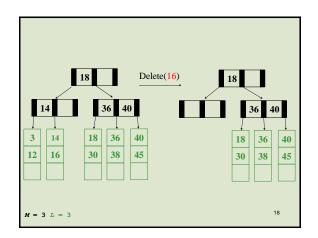


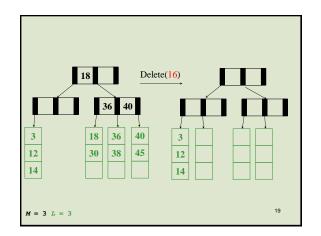


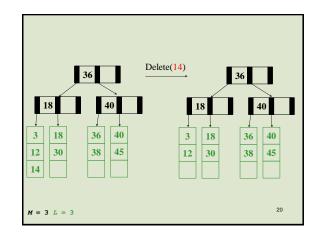


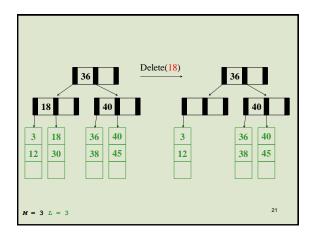


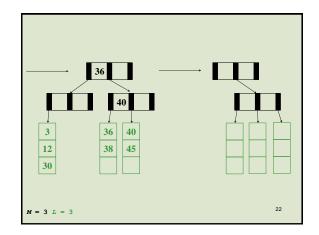


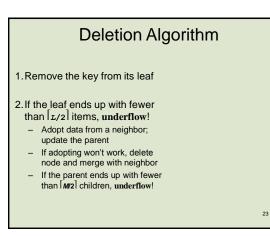


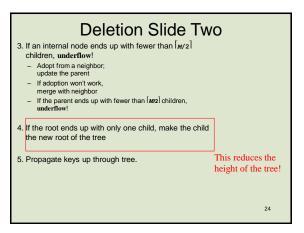












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## Thinking about B+ Trees

- B+ Tree insertion can cause (expensive) splitting and propagation up the tree
- B+ Tree deletion can cause (cheap) adoption or (expensive) merging and propagation up the tree
- Split/merge/propagation is rare if *M* and *L* are large (*Why*?)
- Pick branching factor *M* and data items/leaf *L* such that each node takes one full page/block of memory/disk.

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## Complexity

- Find:
- Insert:
- find:
- Insert in leaf:
- split/propagate up:
- Claim: O(M) costs are negligible

Tree Names You Might Encounter

- "B-Trees"

- More general form of B+ trees, allows data at internal nodes too
   Range of children is (key1,key2) rather than [key1, key2)
- B-Trees with M = 3, L = x are called 2-3 trees
- Internal nodes can have 2 or 3 children
- B-Trees with M = 4, L = x are called 2-3-4 trees
  - Internal nodes can have 2, 3, or 4 children

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