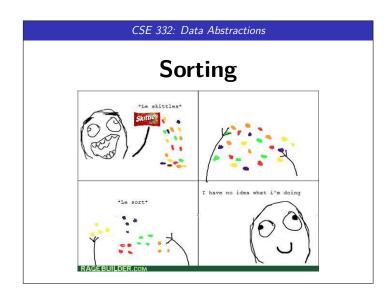
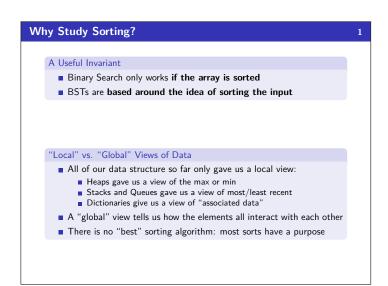
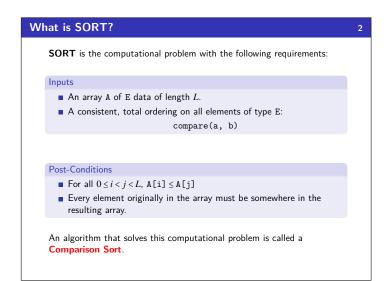
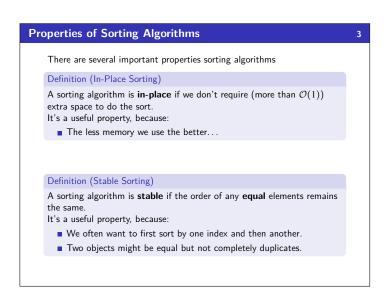
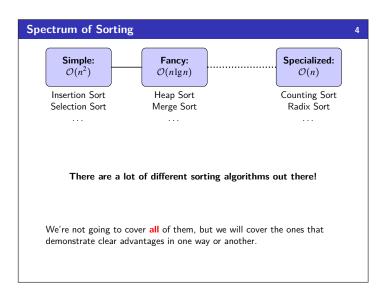
## Adam Blank Lecture 12 Autumn 2015 SE 332 Data Abstractions

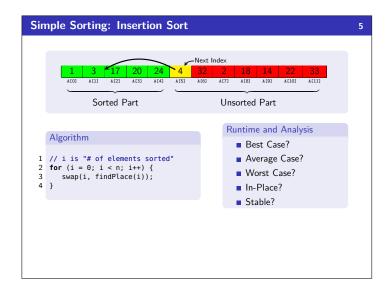


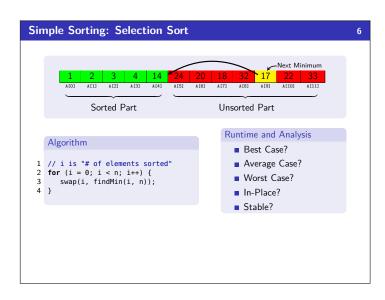


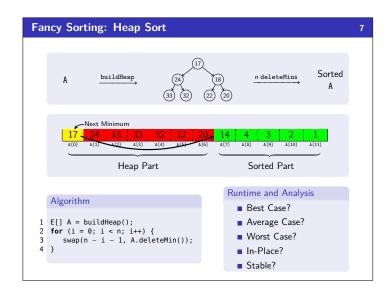










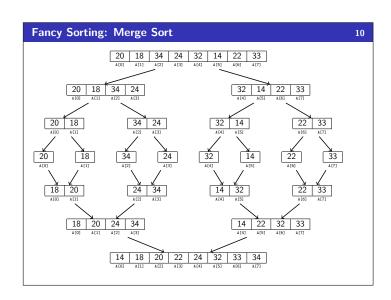


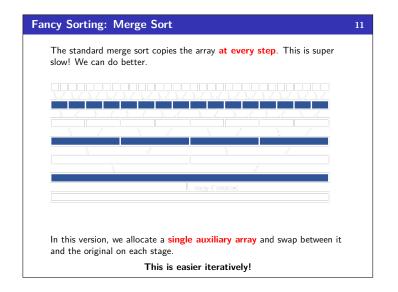
```
Divide and Conquer is a very useful algorithmic technique. It consists of multiple steps:

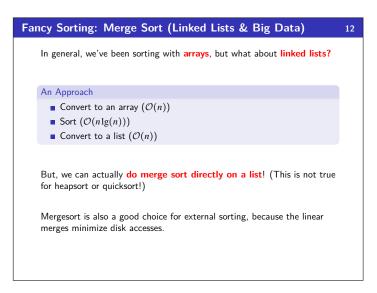
Divide the input into smaller pieces (recursively)
Conquer the individual pieces as base cases
Combine the finished pieces together (recursively)

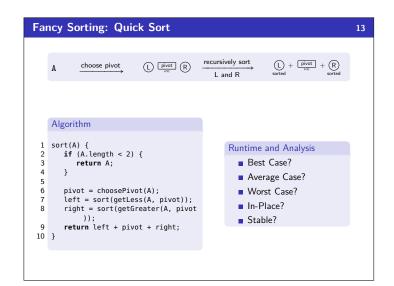
algorithm(input) {
 if (small enough) {
 return conquer(input);
 }
 pieces = divide(input);
 for (piece in pieces) {
 result = combine(result, algorithm(piece));
 }
 return result;
}
```

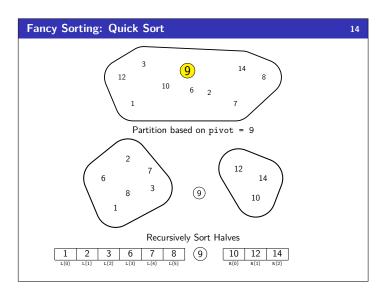
```
Fancy Sorting: Merge Sort
                                                                                   9
                                    Sorted
                  split
                                                        merge
    Α
                                                                           Α
    Algorithm
                                                 Runtime and Analysis
    sort(A) {
   if (A.length < 2) {</pre>
                                                    ■ Best Case?
           return A;
                                                    Average Case?
        return merge(
                                                    ■ Worst Case?
          sort(A[0, ..., mid]),
sort(A[mid + 1, ...])
                                                    ■ In-Place?
                                                    ■ Stable?
```

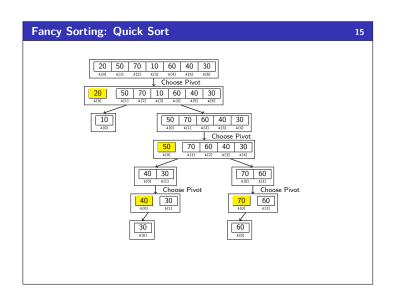


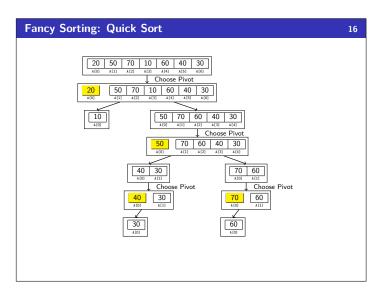


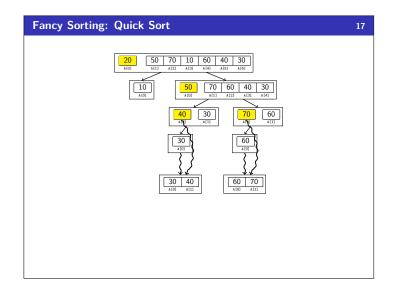


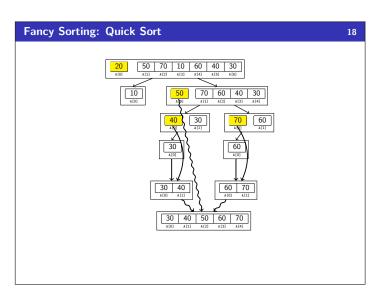


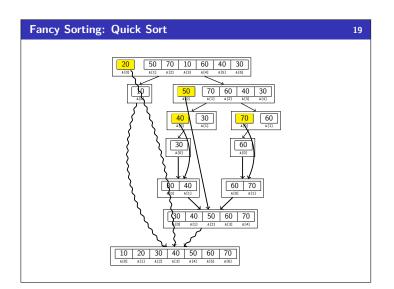












Fancy Sorting: Quick Sort

We now have the general idea of Quick Sort, but there are some remaining questions:

How do we choose the pivot?

How do we partition the array?

Possible), which one would the algorithm take as long as possible), which one would the problem each recursive call.

Worst Pivot?

If an adversary chose our pivot (to make the algorithm take as long as possible), which one would they choose?

Minimum or Maximum

This will decrease the problem size by only one each recursive call.

There are several "standard" strategies to choose a pivot:

1 Choose the first/last element of the array

• Very fast!

• Bad, because real-world data is usually "mostly sorted"

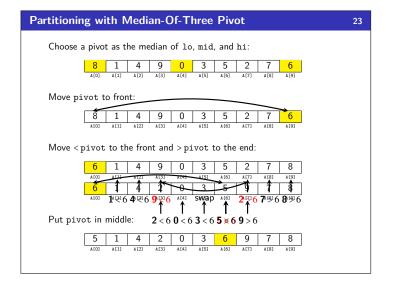
2 Random choice

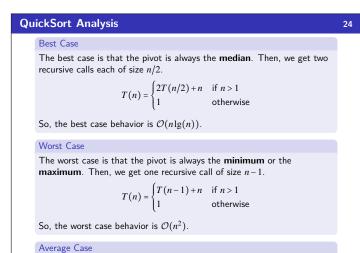
• Generation can be slow

• Good, because there's no easy worst case

3 Median of first, middle, and last elements

• Works well in practice





With a random pivot, on average we get  $\mathcal{O}(n\lg(n))$  behavior.

